Amplifier-Based Tuneable RF Predistortion for

Radio-over-Fibre Systems

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ABSTRACT

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Semiconductor laser diodes (LDs) have been extensively employed for directly transporting wideband multicarrier signals in radio-over-fibre (RoF) systems. However, an inherent characteristic of LDs, the nonlinearity, always has been a fundamental problem in fibre-optic systems. When optical subcarrier modulation (SCM) is used, nonlinear characteristics will induce harmonic and intermodulation distortion (IMD) products that degrade the system's performance significantly. Therefore, it is essential to improve the linearity of RoF systems.

An amplifier-based tuneable radio frequency (RF) predistortion circuit for RoF systems is proposed to linearize the distributed feedback laser diode (DFB-LD) in the range of $0.7 \sim 2.5 \, GHz$. Instead of conventional insertion loss linearization techniques, in this work, a high gain amplifier-based tuneable predistortion circuit was designed. The designed amplifier-based predistortion circuit consists of an impedance matching network and a distortion generation block. To match the distortion generator to the 50 Ω characteristic impedance of an RF source, a capacitively cross-coupled common gate (CCC-CG) broadband matching network is designed. The tuneability of the predistortion circuit is achieved by adjusting the bias current of the triplet-core circuit in the predistortion generation block. The predistortion integrated circuit (IC) is designed with TSMC90nm technology. Performance of the investigated predistortion is simulated with Cadence Virtuoso Hspice/Spectre circuit simulator. Compared with free running LDs,

this predistortion circuit achieves more than 10 dB third-order IMD (IMD3) suppression over the operating frequency range. The proposed scheme is suitable for broadband RF optical transmission applications.

Theoretical analysis of the nonlinear transfer function of the predistortion circuit and DFB-LD has been performed. The nonlinearity of transistors under different configurations is analyzed.

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LIST OF ACRONYMS

ADC	Analog-to-Digital Converter
BS	Base Station
CAD	Computer-aided Design
CCC-CG	Capacitive Cross-coupled Common Gate
CG	Common Gate
CMOS	Complementary Metal-oxide-semiconductor
СМС	Canadian Microelectronics Corporation
CS	Common Source
СТВ	Composite Triple Beat Distortion
DC	Direct Current
DFB-LD	Distributed Feedback Laser Diode
DUT	Device-Under-Test
EAM	Electro-absorption Modulator
E/O	Electrical-to-Optical
GSM	Global System for Mobile Communication
HB	Harmonic Balance
IC	Integrated Circuit
IIP3	Input Referred Third-order Intercept Point
IMD	Intermodulation distortion
IMD3	Third-order Intermodulation distortion
IP3	Third-order Intercept Point

LD	Laser diode
LNA	Low Noise Amplifier
MOS	Metal-oxide-semiconductor
MOSFET	Metal-oxide-semiconductor Field-effect Transistor
MZM	Mach-Zehnder Modulator
NF	Noise Figure
O/E	Optical-to-Electrical
OSSB	Optical Single Side Band
РСВ	Printed Circuit Board
PCCCS	Polynomial Current Control Current Source
PD	Photo Detector
PMOS	P-channel MOSFET
PSS	Periodic Steady-State
RAP	Radio Access Point
RF	Radio Frequency
RFIC	Radio Frequency Integrated Circuit
RoF	Radio-over-Fibre
SCM	Subcarrier Modulation
SISO	Single Input Single Output
S/N	Signal-to-Noise
TE	Transverse Electric
ТМ	Transverse Magnetic
TSMC	Taiwan Semiconductor Manufacturing Company

UMTS	Universal Mobile Telecommunication Systems
UWB	Ultra-Wideband
VCO	Voltage Controlled Oscillators
VLSI	Very Large Scale Integration
WLAN	Wireless Local-area Network

List of Principal Symbols

I_0	DC bias current
I _{th}	Threshold current of laser diode
<i>i</i> th	<i>i</i> -th order
<i>m</i> _i	Modulation index of i^{th} carrier
$arphi_i$	Phase of i^{th} carrier
L(t)	Output power of laser diode
L_0	Power at the DC bias current
$P_{optical}$	Power received by power meter
I _{output}	Current photodetected by PD
R	Responsivity of a PD
<i>i</i> _{pd.}	RF signal current output of the predistortion circuit
k _i	Transfer function coefficients of DFB-LD
a_i	Transfer function coefficients of the predistortion circuit
V _{in}	Input RF signal provided to the predistortion circuit
g_m	Transconductance of MOSFET transistor
g_i	The n^{th} order transconductance of MOSFET transistor
W	Width of MOSFET transistor
L	Length of MOSFET transistor
I_{SS}	Bias current of the differential pair

V_{GS}	Gate-source voltage
V _{DS}	Drain-source voltage
V _{gs}	Small signal gate-source voltage
V _{ov}	Overdrive voltage of MOSFET transistor
V _{TH}	Threshold voltage of MOSFET transistor
V _{os}	Offset voltage
V _{ov}	Thermal voltage
F_n	Noise figure of n^{th} device
G_n	Power gain of n^{th} device
C_{c}	Cross-coupled capacitor
C_{gs}	Parasitic capacitor
Y _{in}	Input admittance
A_V	Voltage gain
R_{L}	Load resistance
R_{S}	Source resistance
μ_n	Channel mobility
C_{ox}	Capacitance per unit area
λ	Channel-length modulation factor
mA	Milli Ampere
mS	Milli siemens

μm	Micrometre		
nm	Nanometre		
mV	Milli Voltage		
mW	Milli Walt		

CHAPTER 1 INTRODUCTION

1.1 Introduction

Mobile and wireless communications have experienced tremendous growth in the last three decades. So far, three mobile standards have been successfully launched. Mobile communications have evolved from the first-generation (1G) of analog systems in the 1980s to the second-generation (2G) of digital mobile systems in the 1990s. The Global System for Mobile communication (GSM) standard which was developed in the 2G systems provides national and international coverage. Current 2G and third-generation (3G) systems are commonly used in mobile communication systems. The fourthgeneration (4G) of systems is under development and is expected to be available in the near future. Apart from the mobile telephone communication, wireless networking is also rapidly growing. The first Wireless Local-area Network (WLAN) developed in 1990 is limited to low speed and narrow band operation. After that, various studies have been devoted to broaden its operation bandwidth and boost the transmission data rate. During the last 20 years, due to the fast evolution of wireless network services, broadband communication and high-speed transmission are widely available for military and commercial uses.

The rapid growth of mobile and wireless communications accelerates the evolution of radio-over-fibre (RoF) technologies. To increase the bandwidth or, to enhance the signal handling capability of a wireless access network, high carrier frequencies or smaller cells (i.e. micro-cells and pico-cells) can be used. However, if smaller cells are used, a larger number of Base Stations (BSs) or Radio Access Points

(RAPs) are needed to satisfy wide coverage and hence, increase the system cost. Although a wired network offers broad bandwidth, it limits the overall convenience and reduces the cost efficiency of systems. The RoF technology with low cost, high carrier frequency and high bandwidth can have compatible properties of wired and wireless network by arranging suitable locations of RAPs through the network along with mesh routers.

In RoF systems, radio frequency (RF) signals are transmitted by using lasers and optical fibre links [1]: the optical light generated from a laser source is modulated by an RF signal and then transported over optical fibre links. This technology is widely used in multi-service domains, like GSM, WLAN, and Universal Mobile Telecommunication Systems (UMTS). Compared with other transmission media, optical fibre as the backbone in RoF technology has unique properties, such as light weight, low attenuation loss, small size, broad bandwidth and insensitivity to electromagnetic radiation. These advantages make it as the optimal solution for transmitting RF signals efficiently in wireless networks.



Figure 1.1 Radio-over-fibre system [1].

A typical RoF system is depicted in Figure 1.1. When a modulated signal (i.e. GSM) is transmitted between the central site and base station, semiconductor lasers and photo detectors (PDs) are employed as electrical-to-optical (E/O) converters and optical-to-electrical (O/E) converters before and after the signal are distributed over optical fibre, respectively. Generally, direct modulation of semiconductor lasers is the most cost effective solution in comparison to other modulators, such as an Electro-absorption Modulator (EAM) and a Mach-Zehnder modulator (MZM).

1.2 Motivation and Review of Technologies

Although these superior characteristics of optical fibre enable RoF technology as an attractive approach in wireless communication, it is necessary to enhance the linearity in optical links to improve the signal transmission quality. When multiple subcarrier modulation (SCM) RF signals are introduced simultaneously in RoF links, undesired harmonics and intermodulation distortion (IMD) products are generated due to the nonlinearity of optical components, such as laser diodes (LDs), MZMs EAMs, and PDs. These undesired products distort the received signals and degrade the overall system's performance. In RoF systems, it is required to keep the distortion below certain levels in order to satisfy the quality of service provided to the users. Each user's provided service has required characteristics specified by the corresponding communication standard. For example, the UMTS standard requires keeping the distortion 45dB lower than signal carrier [2-3] for the down link.

In RoF systems, both modulation and photo-detection devices contribute to the link distortion. Modulation devices usually are the main contributors to distortion generation. Hence, it is critical to suppress the nonlinear distortion produced by modulators. In general, even order distortion terms and harmonics fall far away from the carrier frequency and can easily be filtered out, but third-order IMD (IMD3) terms are close to carrier frequencies and are difficult to filter out. In order to minimize spectral regrowth in the adjacent channels, the odd-order IMD products must be effectively suppressed. Since distortion terms beyond 3rd order are negligible, most linearization work is focused on IMD3 cancellation.

Until now, many linearization technologies have been studied to improve the linearity of optical components using optical or electrical techniques, such as mixed polarization techniques [4], light injection techniques [5], feedforward linearization [6], and analog predistortion techniques [2, 7-11].



Figure 1.2 Mixed polarization linearization of MZM for OSSB modulation [4].

A linearized Optical Single-sideband (OSSB) Mach-Zehnder modulator (MZM) is given in [4]. The linearizer includes a linear polarizer with an angle of α with respect to the z-axis, a dual-electrode z-cut LiNbO₃ MZM, and a second linear polarizer with an angle of β with respect to the z-axis, as shown in Figure 1.2. The anisotropic characteristic of the z-cut LiNbO₃ MZM enables the RF signal to be simultaneously modulated in both orthogonal polarized states, Transverse Electric (TE) and Transverse Magnetic (TM), by different modulation depth. When the optical signal exits the first polarizer, z-(TM) axis will carry more IMD3 while the x-(TE) axis will carry less IMD3. Followed by the MZM, the optical signal enters the second polarizer. Since the two angles α and β are related to each other, therefore, the combined IMD3 from the two arms of MZM can be suppressed by carefully selecting α and β of the two linear polarizes. This mixed-polarization based linearization technique is mainly dependent on choosing α and β , thus this linearization technique is limited to polarization dependent modulators. However, this linearization method cannot be used to linearize LDs, which are known as polarization independent components. On the other hand, high insertion loss is another disadvantage of this technique. In the mixed polarization method, the signal carrier is attenuated by more than 10 *dB* which decreases the transmitted signal significantly.



Figure 1.3 Diagram of a feedforward system [6].

A feedforward linearization technique is given in Figure 1.3. This system consists of two loops: signal cancellation loop (the first loop) and distortion cancellation loop (the second loop). In the first loop, the RF signal is split into two paths, where one modulates the primary laser L_1 and the other is the error-free reference path. Due to the nonlinearity of laser L₁, the signal at the output of the variable gain amplifier A₁ contains carrier and IMD products. Signal cancellation is achieved at the output of the 180^{0} hybrid coupler C₂, in which the output products of A_1 are subtracted from the error-free reference path. Ideally, only IMD3 distortion is left at the output of C_2 . The error signal at the output of coupler C_2 is shifted by 180^0 and then injected into the second loop. The optical coupler K_2 combines the output signal of laser L_2 and the signal transmitted from the optical fibre. Distortion cancellation is realized at the output of the PD, since the PD functions as a broadband in-phase microwave combiner. Furthermore, intensity laser noise can also be reduced by this architecture. However, the feedforward technology requires accurate amplitude and phase matching between the signal cancellation loop and the distortion cancellation loop, which makes this technique difficult to achieve in practice, thus limiting the amount of distortion reduction. In addition, the feedforward linearization method requires extra LDs and PDs and hence, increases the cost and complexity of the whole system.

Compared to the feedforward linearization method mentioned above, predistortion techniques have become an attractive solution due to their lower cost, less complexity and easy implementation. Predistortion circuits are designed which operate at 1350 *MHz* and 5800 *MHz* are reported in [8] and [9], respectively. In [7, 10], the predistortion circuits are designed with CMOS 0.18 μm technology and operate in 1850 ~

2150 *MHz* and 50 ~ 500 *MHz*, respectively. In [2], they designed a predistortion prototype using discrete diodes that can operate at $370 \sim 480$ *MHz*, $820 \sim 960$ *MHz* and $1710 \sim 1980$ *MHz*. Two predistortion prototypes reported in [7] and [11] are reviewed in detail.



Figure 1.4 Predistortion block diagram [7].

An adaptive CMOS predistortion linearizer is proposed in [7]. In this predistortion prototype, shown in Figure 1.4, the input RF signal is firstly split into three paths: one goes through the time delay path, the other two paths go through the nonlinearity generation (second- and third-order distortion) circuits, and then these three paths are combined after the power combiner. In this predistortion configuration, the power budget and the complexity of the overall system are increased by additional phase-adjust and gain-adjust blocks. To achieve a constant suppression over the bandwidth, it is required to ensure that the correction tones produced by the predistortion circuit experience the same delay and equal gain. Otherwise, linearity improvement will be hard to achieve.



Figure 1.5 Schematic diagram of anti-parallel diodes predistortion [11].

Recently, our group proposed a broadband predistortion of an EAM [11]. As shown in Figure 1.5, the predistortion circuit consists of two power splitters/combiners, anti-parallel diodes in two paths with push-pull bias and $\lambda/4$ impedance transformer matching networks. In this circuit configuration, the input RF signal is equally converted to two paths by a power splitter and transmitted through a pair of anti-parallel diodes. Subsequently, the separated signals are recombined at the output of another power combiner. The anti-parallel diode structure cancels the even order nonlinear products and only the odd order distortions are left after the combiner. By tuning the bias current of the diodes, the magnitude and phase of the carrier and IMD3 of this predistortion circuit can be adjusted. Compared to current predistortion techniques, this design provides the simplest approach and is suitable to linearize LDs. However, the $\lambda/4$ impedance transformer networks occupy a large board area and introduce some signal losses.

1.3 Objective

The focus of this research work is on designing a simple and economical amplifier-based tuneable RF integrated predistortion circuit to linearize distributed feedback laser diodes (DFB-LDs) in the application of GSM, WLAN, and UMTS systems, which covers $0.7 \sim 2.5 \, GHz$. The designed predistortion circuit will extend the output power of the DFB-LD for which IMD3 is $45 \, dB$ lower than the carrier signal. This will enhance the signal transmission capability of RoF systems significantly. In contrast to traditional lossy predistortion, the proposed predistortion circuit predistorts and amplifies the signal using a single path instead of the conventional two-path approach. The low noise and high gain characteristics of the predistortion circuit make it able to process the signal received from antenna without using additional amplifiers. The entire predistortion system is single-input and single-output (SISO). This will significantly reduce the complexity and cost of RoF systems.

1.4 Thesis Scope and Contributions

This thesis developed a gain boosting integrated circuit (IC) solution to suppress IMD3 distortion in optical fibre access communication systems. The predistortion circuit is designed with TSMC90nm technology, which is supported by Canadian Microelectronics Corporation (CMC). The proposed amplifier-based predistortion circuit has an equivalent transconductance of 0.64 *S* over a bandwidth of 1.8 *GHz*. The simulated noise figure (NF) of the entire predistortion circuit is 6.65 *dB* maximum.

The main challenges in this design are the broad operational bandwidth, which covers $0.7 \sim 2.5 GHz$ and high modulation current generation, typically up to 25 mA. In order to achieve the specified bandwidth, modulation current requirements and NF minimization, 1.3V supply is selected (instead of the recommended 1.2V) with slight increase in power dissipation.

The main contributions of this thesis are:

- 1. An amplifier-based tuneable RF predistortion for RoF systems was designed, which covers the most significant frequency band of wireless access application from 0.7 to 2.5 *GHz*.
- 2. The principle of the predistortion topology was analyzed. The transfer functions of the predistortion linearizer were derived. The nonlinearity of a common-source (CS) transistor, differential pairs and Gilbert cells were studied. A novel distortion generation method based on existing linearization techniques was developed.
- 3. A capacitively cross-coupled (CCC-CG) low noise amplifier (LNA) was used for broadband matching of the proposed triplet-core circuit to the 50 Ω characteristic impedance of the RF chain. The noise performance of the matching network and predistortion circuit were analyzed and simulated. The nonlinearity of the normal common gate (CG) and the CCC-CG LNA were investigated.
- 4. Different types of current mirror were designed to bias and process the signal. The current injection technique was used to improve the conversion gain and reduce system power dissipation. The entire predistortion circuit supplies both DC current and modulation signal to the DFB-LD.

1.5 Thesis Outline

The rest of the thesis is organized as follows:

The principle of predistortion linearization is discussed in Chapter 2. The nonlinear transfer function of a DFB-LD is measured experimentally and modeled with the 4th order polynomial equation. To linearize the DFB-LD, the transfer function of

predistortion circuit is derived. The nonlinear characteristics of a single transistor, differential pairs and Gilbert cells are discussed. After a review of the *Multi-tanh* principle of Gilbert cells, the triplet-core circuit is proposed and its nonlinear characteristic is analyzed and computed using Cadence Virtuoso Hspice/Spectre circuit simulators.

Chapter 3 describes the matching network design of the proposed triplet-core circuit. A g_m -boosting CCC-CG topology is analyzed. A differential test bench is studied and applied to simulate the matching behavior and noise performance of the designed LNA. The nonlinearity of the matching network is simulated.

Chapter 4 begins with the architecture of the whole system design. From the system point of view, a 180⁰ coupler is used to convert the single input to differential inputs in the printed circuit board (PCB) design process. The matching network has a fully differential configuration while the distortion generator converts the differential input to a single ended output. Therefore, the matching stage and distortion generator can be connected to one another. This chapter explains the detailed design work. Various current mirrors are described, such as basic current mirrors, cascode current mirrors and active current mirrors. The current injection technique is also described. The designed IC supplies both bias current and modulation current to directly drive the DFB-LD. Finally, simulation results are presented and discussed.

Chapter 5 gives concluding remarks, the progress that has been accomplished and suggests some future work.

CHAPTER 2 THE PRINCIPLE OF PREDISTORTION

2.1 Introduction to Distributed Feedback Laser Diode

Nowadays, semiconductor LDs are one of the most common electro-optic devices used in RoF systems due to their advantages, such as small size, cost-effectiveness, simplicity and ease of monolithic integration with other E/O components. Like other modulators, LDs are the main nonlinear contributors in RoF systems. The nonlinear characteristics of an LD introduce many harmonics and IMD products if SCM is used, and these nonlinear products degrade the performance and sensitivity of RoF systems. Therefore, it is highly desirable to develop linearization techniques to compensate the nonlinear distortion.

A DFB-LD is a semiconductor LD, in which a diffraction grating is etched close to the p-n junction of the diode in order to achieve the selectivity of lasing wavelength. The optical grating acts like an optical filter, where all these small reflections are added in phase. Ideally, only one wavelength is selected by the optical grating and fed back to the gain region and lases. Figure 2.1 shows one possible way to incorporate a grating within a diode laser cavity. In a DFB-LD, the intensity of the laser output will be changed directly by the modulation signal. Also, the optical output power of the LD and its lasing frequencies are fluctuating with the modulation signal. Therefore, DFB-LD is a frequency dependant direct modulator.



Figure 2.1 Diagram of a DFB-LD with Bragg grating on the top [12].

2.2 Mathematical Analysis of Predistortion

To linearize the DFB-LD, it is necessary to study its nonlinear characteristics. There are two approaches in evaluating the nonlinear distortion of a DFB-LD in multichannel transmission: one is based on dynamic modeling of the rate equations [13], while the other is based on static modeling of the light-current characteristics (typically, *L-I* curve) [14]. Compared with rate-equations-based modeling, *L-I* curve modeling is an easier approach to evaluate the nonlinear characteristics of a DFB-LD. In this work, the nonlinearity of the DFB-LD is studied with its static *L-I* curve. The modulation current provided to the laser is described in [14] as

$$I(t) = I_0 + (I_0 - I_{th}) \sum_{i=1}^{N} m_i \cos(2\pi f_i t + \varphi_i)$$
(2.2.1)

 I_0 is the DC bias current, I_{th} is the threshold current of the laser, m_i is the modulation index of the i^{th} carrier, and φ_i is the phase of i^{th} carrier. In response to the modulation, the light output L(t) is given by

$$L(t) = L_0 + \sum_{i=1}^{N} \frac{d^n L / dI^n}{n!} [I(t) - I_0]^n$$
(2.2.2)

where L_0 is the power at the DC bias current.

2.2.1 Modeling of Nonlinear Transmission Characteristics of a DFB-LD in RoF Systems

To accurately analyze the nonlinearity of the DFB-LD, we first perform the experiment to measure its nonlinear transmission characteristics. The experimental setup consists of a current source, a DFB-LD and an optical power meter. During the experiment, the bias current supplied to the DFB-LD is adjusted from 1 to $125 \ mA$, with a step of $1 \ mA$ and the optical power is measured at each step. The DFB-LD starts lasing when operating beyond its threshold current. The threshold current of the tested DFB-LD is $8 \ mA$. The measured *L-I* curve on a linear scale is shown in Figure 2.2.



Figure 2.2 Measured nonlinear characteristics of a DFB-LD.

 $P_{optical}$ is the power received by the power meter. Converting $P_{optical}$ to the current photodetected by PD, I_{output} , we have

$$I_{output} = P_{optical}R \tag{2.2.1.1}$$

Where R is the responsivity of the PD. Typically, R is 0.6, which refers to the optical to electrical conversion efficiency of the PD.

To investigate the nonlinearity of the DFB-LD, we fit the *I-I* curve (bias current of DFB-LD versus current detected by PD) by a polynomial using curve fitting functions in Kaleidagraph. The model is built by writing the nonlinear equation to a Polynomial Current Control Current Source (PCCCS), which is available in the Analog Library of Cadence. The proposed predistortion circuit is designed and simulated based on the PCCCS model.

The considered modulation and bias current of the DFB-LD are 25 mA and 35 mA, respectively. Therefore, the photodetected current I_{output} in terms of bias current is obtained by polynomial curve fitting within the operation range, i.e. $10 \sim 70 \text{ mA}$. Some bias currents that are below or close to threshold are ignored. The fitted curve with bias current of the DFB-LD is plotted in Figure 2.3. A 4th order polynomial curve fitting is well matched with the measured nonlinear transmission characteristics. The nonlinear characteristic of the DFB-LD is described in equation (2.2.1.2). Table 2.1 gives the value of transfer function coefficients.

$$I_{output}(I) = f(I) = M_0 + M_1 I + M_2 I^2 + M_3 I^3 + M_4 I^4$$
(2.2.1.2)

Where M_i (i = 0, 1, 2, ..., 4) are the transfer function coefficients of the *I-I* curve.



Figure 2.3 Measured nonlinear characteristics of the DFB-LD.

Table 2.1 Transfer function coefficients of the 4th order polynomial curve fitting of the DFB-LD transmission characteristics.

Transfer Function Coefficients (DC)	M_0	M_{I}	M_2	M_3	M_4
Value	-0.00008	0.00754	0.06321	-0.61371	0.34454

After defining the polynomial model of the DFB-LD, we expand equation (2.2.1.2) into a Taylor series to investigate its nonlinear transfer function at a given bias, 35 mA in this condition. When the modulation signal i_{rf} is supplied to a DFB-LD, the current I in equation (2.2.1.2) is expressed as $I = I_b + i_{rf}$, where I_b is the bias current and i_{rf} is the RF modulation current. Considering the small signal approximation, i.e. $i_{rf} \ll I_b$, we expand the nonlinear transfer function in (2.2.1.2) into a Taylor series, yielding

$$I_{output}(I) = f(i_{rf}) = k_0 + k_1 i_{rf} + k_2 i_{rf}^2 + k_3 i_{rf}^3 + \dots + k_n i_{rf}^n + \dots$$
(2.2.1.3)

Where $k_i (i = 1, 2, 3, ..., n, ...)$ are the Taylor series coefficients $k_1 = \frac{f'(I_b)}{1!}$, $k_2 = \frac{f''(I_b)}{2!}$

..., $k_n = \frac{f^n(I_b)}{n!}$,... The transfer function coefficients in terms of i_{rf} are shown in Table 2.2.

Table 2.2 Transfer function coefficients of the DFB-LD transmission characteristics.

Transfer Function Coefficients (AC)	k_0	k_I	k_2	k_3	k_4
Value	0.0002	0.0098	0.0013	-0.5655	0.3445

2.2.2 Mathematical Analysis of Predistortion

The block diagram of the predistortion circuit followed with a DFB-LD is depicted in Figure 2.4.



Figure 2.4 Block diagram of predistortion circuit and DFB-LD.

The proposed predistortion circuit is transconductance based and the DFB-LD is modeled by a PCCCS and hence, the output of predistortion circuit and input of DFB-LD are expressed in current mode. In this work, we are only concerned about the IMD3 compensation. Since even distortions terms of the DFB-LD do not contribute to IMD3 generation, the transfer function of the DFB-LD is simplified as

$$I_{out} = k_1 i_{pd.} + k_3 i_{pd.}^3$$
(2.2.2.1)

Where i_{pd} is the RF signal current output of the predistortion circuit, k_i (i = 1 and 3) are the transfer function coefficients of the DFB-LD.

The even order products of the predistortion circuit are eliminated due to its differential configuration (more details are given in Section 2.3.1). The transfer coefficients of distortion products above 3rd order decrease rapidly. Hence higher order terms are neglected with little loss in accuracy. Therefore, the RF signal current output of the predistortion circuit is expressed as:

$$I_{pd.} = a_1 v_{in} + a_3 v_{in}^3 \tag{2.2.2.2}$$

where v_{in} is the input RF signal provided to the predistortion circuit and a_i (*i* = 1 and 3) are the transfer function coefficients of the predistortion circuit.

Considering the carrier and third-order nonlinear terms only, the current photodetected by the PD is derived by substituting (2.2.2.2) into (2.2.2.1).

$$I_{out} = k_1 a_1 v_{in} + (k_1 a_3 + k_3 a_1^3) v_{in}^3$$
(2.2.2.3)

To suppress the third-order nonlinear distortions of the DFB-LD, the transfer function coefficient of IMD3 should be minimized. Ideally, it can be reduced to zero. Therefore, the correlated transfer function of the predistortion circuit and the DFB-LD satisfies the following condition:

$$\frac{k_1}{k_3} = -\frac{a_1^3}{a_3} \tag{2.2.2.4}$$
Normally, in nonlinear devices, such as optical modulators and amplifiers, carrier and IMD3 terms are out of phase, which is known as a gain compression characteristic. Consequently, to achieve IMD3 compensation, the carrier and IMD3 of the predistortion circuit should be in phase, which is known as a gain expansive characteristic. The proposed predistortion is voltage input and current output. With the transfer function coefficients k_1 and k_3 given in Table 2.2 and equation (2.2.2.4), the normalized transconductance g_m curve of the predistortion circuit in terms of input voltage is plotted in Figure 2.5.



Figure 2.5 Desired g_m curve of the predistortion circuit.

Assuming the photodetected output current of the DFB-LD is fed to a 50 Ω load, the nonlinear characteristics of the DFB-LD without predistortion and theoretical analysis of the compensated DFB-LD with predistortion circuit are plotted in Figure 2.6. As shown in Figure 2.6, the free-running DFB-LD cannot fulfill the requirement of keeping the IMD3 45 *dB* lower than the signal carrier when the processed signal is greater than 11mA (corresponding to -35.4 dBm output RF power in Figure 2.6). The third-order nonlinearity is suppressed as can be seen from the slope of 5 in IMD3 when using the predistortion circuit. From a system point of view, the amplifier-based predistortion circuit enhanced the power transmission capability and increase the signal-to-noise (S/N) ratio of RoF systems. Therefore, the power boosting predistortion circuit minimized the system cost and power consumption of the entire system. Ideally, with the predistortion circuit, the DFB-LD can handle 21mA signal current (corresponding to -30.3 dBm output RF power in Figure 2.6) within the system linearity requirement.



Figure 2.6 Nonlinear characteristic of DFB-LD with theoretical predistortion cancellation.

2.3 Triplet-Core Circuit

To build a CMOS predistortion circuit, nonlinear characteristics of three different circuit configurations are studied: a single CS transistor, a differential pair and Gilbert cells. Based on the *Multi-tanh* linearization technique, a novel distortion generation method is developed.

2.3.1 Nonlinear Transconductance of a Single Transistor and Differential Circuits

Consider a single CS MOSFET biased in saturation. The small-signal output current depends on the gate-source (V_{GS}) and drain-source voltages (V_{DS}), but the dependence on V_{DS} for a transistor in saturation can be ignored here with little loss in accuracy [15]. Expanding its output drain current into a one-dimensional Taylor series in terms of the small-signal gate-source voltage (v_{gs}) around the bias point, we get

$$i_d(v_{gs}) = g_1 v_{gs} + g_2 v_{gs}^2 + g_3 v_{gs}^3 + \dots$$
(2.3.1.1)

where g_1 is the small-signal transconductance, g_2 , g_3 , ... are the higher-order coefficients which define the intensity of the corresponding nonlinearity. Of all these coefficients, g_3 is particularly important because it controls the third-order nonlinear distortion, hence determining the input referred Third-order Intercept Point (*IIP3*) [16-17]. The first three coefficients g_i (i = 1, 2, and 3) can be found by taking the i^{th} derivative of equation (2.3.1.1) in terms of v_{gs}

$$g_1 = \frac{\partial I_D}{\partial V_{GS}}$$
 $g_2 = \frac{1}{2} \frac{\partial^2 I_D}{\partial V_{GS}^2}$ $g_3 = \frac{1}{6} \frac{\partial^3 I_D}{\partial V_{GS}^3}$ (2.3.1.2)

In the simulation, by sweeping V_{GS} of a CS NMOSFET with a dimension of W/L (10 µm/100 nm) and a fixed V_{DS} , the first three derivatives of drain current in terms of V_{GS} are plotted in Figure 2.7. As depicted in Figure 2.7, when V_{GS} transitions from the weak to moderate inversion region or the strong inversion region, the dependence of g_3 on V_{GS} is such that g_3 changes from positive to negative (contrasting to g_1). Figure 2.8 depicts the corresponding absolute value of g_2 / g_1 and g_3 / g_1 on a log scale. As shown

in Figure 2.8, the nonlinearity of a transistor varies with the overdrive voltage. In the strong inversion region, transistor always has higher linear transconductance and lower second-/third-order distortion coefficients.



Figure 2.7 Simulated DC characteristics of a W/L (10 µm/100 nm) NMOSFET.



Figure 2.8 Simulated g_2/g_1 and g_3/g_1 ratio of a W/L (10 µm/100 nm) NMOSFET.

Some efficient linearization methods based on the DC characteristics of a CS transistor are described in [15-17]. The nonlinearity of a single CS transistor can be improved by using multiple gate transistors: the main transistor operates in the saturation region while an auxiliary transistor with different size operates in the weak inversion region which nulls the negative 3^{rd} order derivative g_3 of the main transistor. This is known as derivative superposition method [16]. However, with this linearization topology, it is hard to build a widely tuneable and high gain predistortion circuit due to its low signal handling capability and high tuning sensitivity in the weak inversion region.

Numerous linearization techniques have been developed with differential pairs. Compared to a single CS transistor, it demonstrates an "odd-symmetric" input/output characteristic and correspondingly exhibits much less distortion [18-19]. A schematic diagram of a basic differential pair is shown in Figure 2.9.



Figure 2.9 Basic differential pair.

Assuming transistors M_1 and M_2 are identical long channel MOSFET, biased in the saturation or strong inversion region. The output current is developed as:

$$I_0 = I_1 - I_2 = \sqrt{2I_{SS}K}V_{in}\sqrt{1 - \frac{K}{2I_{SS}}V_{in}^2} \qquad |V_{in}| \le \sqrt{\frac{I_{SS}}{K}} \qquad (2.3.1.3)$$

where $K = \frac{1}{2} \mu_n c_{ox}(\frac{W}{L})$ and I_{SS} is the bias current of the differential pair.

Expanding (2.3.1.3) into a Maclaurin series, yields

$$I_{0} = \sqrt{2I_{SS}K}V_{in} - \frac{1}{2\sqrt{2}}\frac{K^{3/2}}{\sqrt{I_{SS}}}V_{in}^{3} - \dots \qquad |V_{in}| \le \sqrt{\frac{I_{SS}}{K}}$$

$$= 2KV_{ov}V_{in} - \frac{1}{4}\frac{K}{V_{ov}}V_{in}^{3} - \dots \qquad |V_{in}| \le \sqrt{2}V_{ov}$$
(2.3.1.4)

We have

$$V_{ov} = V_{GS} - V_{TH}$$
(2.3.1.5)

Where V_{ov} is the overdrive voltage and V_{TH} is the threshold voltage of M_1 and M_2 . Equation (2.3.1.4) indicates that the nonlinearity decreases with increasing V_{ov} . With a fixed transistor size of M_1 and M_2 , increasing V_{ov} , the first-order transfer function coefficient increases while the third-order's decreases. Consequently, the amplitude of signal carrier is increased and third-order distortion terms are reduced and hence, the nonlinearity of the differential pair is reduced. However, increasing V_{ov} leads to large power dissipation. Thus, it is necessary to tradeoff transistor size and power dissipation.

The DC characteristic of the differential pair is simulated in Hspice. By sweeping V_{in} , the desired output current I_1 and I_2 can be obtained from the differential pair circuit. As illustrated in Figure 2.10, the output currents I_1 and I_2 are odd functions of V_{in} . $I_1 - I_2$ falls to zero when $V_{in} = 0$. Beyond $V_{in} = \sqrt{2}V_{ov}$, one transistor carries the entire I_{SS} while the other is turned off. The equivalent transconductance of M_1 in the differential pair is plotted in Figure 2.11.



Figure 2.10 Voltage-current (V-I) characteristic of the differential pair.



Figure 2.11 g_m of transistor M_l .

The g_m of M_l in terms of V_{in} is developed as:

$$g_{m} = \frac{\sqrt{I_{SS}K} [1 - \frac{2KV_{in}^{2}}{I_{SS}}]}{\sqrt{1 - \frac{KV_{in}^{2}}{I_{SS}}}} = \frac{\sqrt{2}KV_{ov} [1 - \frac{V_{in}^{2}}{V_{ov}^{2}}]}{\sqrt{1 - \frac{V_{in}^{2}}{2V_{ov}^{2}}}}$$
(2.3.1.6)

As shown in Figure 2.11, the transconductance g_m is a symmetric function of V_{in} .

The shape of the transconductance g_m curve in Figure 2.11, along with its relationship with the overdrive voltage V_{ov} can be used to evaluate the nonlinearity of differential pairs. Generally, with fixed transistor sizes, higher I_{SS} contributes to a higher V_{ov} and hence expands the g_m curve. High linearity in differential pairs is obtained at $V_{in} = 0$, but degrades with large input signal.

With MOSFETs scaling down below 100 *nm*, the square-law model is no longer accurate [20]. However, the basic observations made in this section about the large-signal operation of the MOS differential pair are still valid. In particular, the differential pair still gives rise to a compressive nonlinearity.

2.3.2 Introduction of Gilbert Cell and the *Multi-tanh* Principle

The Gilbert cell was first described by Barrie Gilbert in 1968. Gilbert cell is built by connecting the input and output of differential pairs in parallel [21]. The *Multi-tanh* principle of Gilbert cell is named based on its topological and mathematical aspects. If $n (n \ge 2)$ differential pairs are connected in parallel, their individual nonlinear transconductance can be expanded along the input-voltage axis by applying input offset voltages. Offset voltage can also be supplied by selecting the emitter area ratio of differential pairs. The *Multi-tanh* configuration enhances the large signal handling capability of individual differential pairs. If the overall transconductance is extended to a wider region, it can provide a low-distortion scheme. Such a cell gives a highly linear transconductance, hence it is widely used to build linear amplifiers, mixer, voltage controlled oscillators (VCOs), tuneable filters, or other active elements.

The doublet, in which two differential pairs are connected in parallel, is the simplest form of a Gilbert cell. To illustrate the *Multi-tanh* principle, the doublet is discussed as an example. A bipolar transistor based doublet is shown in Figure 2.12.



Figure 2.12 Basic Multi-tanh doublet [21].

In Figure 2.12, differential pairs Q_1 - Q_2 and Q_3 - Q_4 , are biased with equal tail current I_T . The offset voltages are provided by making the emitters' area ratio of Q_1 and Q_4 "A" times of Q_2 and Q_3 . The emitter area ratio "A" shifts the peak of each g_m by an equivalent offset voltage V_{os} . The relationship between A and V_{os} satisfies

$$V_{os} = V_T \ln A \tag{2.3.2.1}$$

where V_T is the thermal voltage.

The overall g_m is much more linear compared with each individual transconductance, as illustrated in Figure 2.13. In the doublet circuit, the original g_m is reduced by a factor of $4A/(1+A)^2$ [21]. In order to reach the same conversion gain, I_{SS} and the diffusion area should be multiplied by $(1+A)^2/4A$. From this point of view, the

linearity of the Gilbert cell is achieved at the expense of increasing the system power dissipation and using large transistors.



Figure 2.13 Dual g_m components for the doublet.

2.3.3 Proposed Triplet-Core Circuit

The *Multi-tanh* principle can also be applied to MOSFETs, since MOS transistors operating in the sub-threshold and saturation region behave almost exactly like bipolar transistors. The concept that works in strong inversion: the width ratio of transistors gives an input offset voltage which shifts the peak of the g_m curve away from $V_{in} = 0$. In the doublet circuit, if the peak of each individual g_m is shifted further with higher offset voltage, a valley appears at the center of the g_m curve. Therefore, the g_m curve of the doublet circuit has the similar shape with the desired transconductance of predistortion circuit, as depicted in Figure 2.14. The g_m curve of MOSFET based doublet and the desired g_m curve are shown in Figure 2.14. The doublet circuit has a simple architecture

which is suitable to linearize specific gain compression component. As shown in the region outlined in rectangular in Figure 2.14, the g_m curve of the doublet circuit and the desired g_m curve are matched to each other when $-42.7 \ mV \le V_{in} \le 42.7 \ mV$. However, the expansive region of the g_m curve has a limited range. Simulation results shown that the g_m curve compresses if operating beyond 104 mV peak-to-peak. Another disadvantage of the doublet circuit is that it is hard to tune it to generate the required amount of distortion if any nonlinear variation of components occurs due to temperature variation or measurement errors of LDs. Also, it is necessary to increase the bias currents of doublet circuit to produce high signal current in order to drive the DFB-LD with high modulation current. These disadvantages make the doublet circuit is unsuitable in tuneable prsdistortion generation design.



Figure 2.14 Transconductance of the proposed doublet circuit.

Instead of the Gilbert doublet circuit, a triplet cell is utilized to extend the expansive region. Although it is possible to have a high order (n>3) Gilbert cell, it increases the system complexity and power dissipation since more differential pairs are

involved. The triplet cell is designed to generate the desired g_m to compensate the nonlinearity of the DFB-LD rather than to make a linear g_m curve. There are two ways to implement the triplet cell. One is to shift the two peaks of g_m further and add another differential pair, which has a smaller transconductance. The other approach is to make a doublet cell with a wider linear region, which can be obtained with higher overdrive voltage. By subtracting the extra g_m curve of the third additional differential pair, we obtained the desired curve. Comparing these two approaches, the second option provides wider expansive region and hence, is used to build the proposed triplet-core circuit. The triplet-core circuit and the corresponding g_m curves are shown in Figure 2.15 and Figure 2.16.



Figure 2.15 Schematic diagram of the proposed triplet-core circuit.



Figure 2.16 g_m curves of proposed triplet-core circuit.

As explained in Section 2.3.1, the nonlinearity of the differential pair depends on the tail current, given by I_1 , I_2 and I_3 of the triplet-core circuit. Consequently, tuning I_1 , I_2 and I_3 shifts g_m the curves and hence varies the nonlinearity of the triplet-core circuit. In this work, the offset voltage of the outer differential pairs are provided with a transistor width ratio "A", "A" is equal to 8 and K is equal to 0.33 in this design. No offset voltage is applied to the inner pair. The current subtraction is achieved if the output of the inner differential pair (M_{2A}/M_{2B}) is cross-coupled with the outer pairs (M_{1A}/M_{1B} and M_{3A}/M_{3B}). Obviously, this triplet-core circuit has a fully differential configuration. Since the outer differential pairs have a symmetrical structure, I_1 and I_3 can be controlled by one current mirror. Therefore, two current sources I_{b2} and I_{b3} are used to adjust tail currents: I_{b2} controls I_1 and I_3 while I_{b3} controls I_2 . The detailed schematic diagram of the triplet-core circuit is given in Figure 4.2. The nonlinearity of the triplet-core is tuneable. As depicted in Figure 2.17 and Figure 2.18, when the tail currents of the outer pairs I_1 and I_3 are increased from 2.4 mA to 3.0 mA, the nonlinearity of triplet-core is decreased; while tuning the tail current of inner pair I_2 from 0.8 mA to 2.0 mA, the nonlinearity at higher level, beyond 100 mV peak-to-peak, is reduced. DC sweeps also indicate how to tune the nonlinearity of the triplet-core circuit to get the desired g_m curve: tuning I_1 and I_3 to fit the overall g_m with low signal input and tuning I_2 to fit the overall g_m with high signal input.



Figure 2.17 Overall g_m curves by tuning I_1 and I_3 .



Figure 2.18 Overall g_m curves by tuning I_2 .

2.4 Conclusion

In this chapter, we studied and measured the nonlinear transfer characteristic of the DFB-LD. The nonlinear polynomial model of the DFB-LD is defined with PCCCS in Cadence and is suitable for predistortion circuit design and simulation. Based on the desired transcondutance of the predistorter derived from mathematical analysis, various distortion characteristics of a single CS transistor, differential pairs and Gilbert cells are reviewed. The nonlinearity of the proposed triplet-core circuit can be tuned by adjusting bias currents I_1 , I_2 and I_3 . The highly tuneability enhanced the linearization and nonlinearity variation handling capabilities of the proposed predistortion circuit.

CHAPTER 3 INPUT IMPEDANCE MATCHING NETWORK Design of The Proposed Triplet-core Circuit

3.1 Introduction

Impedance matching is an essential part of RF circuit design for maximum power transmission and is therefore discussed in detail in numerous sources [22-25]. As we know, the Gilbert cell configuration is usually noisy because of the current subtraction of differential pairs [24]. Input matching condition and NF are figures of merit to measure the matching network. Since impedance matching and NF are correlated [25], it is necessary to come up with a solution to match the triplet-core circuit and reduce its affect on the NF of systems.

When *n* blocks are cascaded, the NF of the entire system is given by [26]

$$F = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 G_2} + \dots$$
(3.1.1)

Where F_n (n = 1, 2, 3, ...) is the NF for the n^{th} block and G_n (n = 1, 2, 3, ...) is the linear power gain of the n^{th} block.

This is known as the Friis formula and typical results show that the most critical stage is usually the first stage. Hence, the NF of the first stage usually dominates the sensitivity of the entire system. Consequently, it is promising to design an impedance matching network and diminish the NF of the triplet-core circuit by cascading an LNA which provides enough gain and low NF in front.

Many LNAs presented in other works (i.e. [27-28]) have achieved a good matching and high gain. In this work, a g_m -boosting CCC-CG topology [28-29] is selected to match to triplet-core circuit to 50 Ω . Noise performance and the gain of the proposed CCC-CG matching network are analyzed. S11 and NF are performed with S-parameter simulation using the Spectre simulator in Cadence. The capacitively cross-coupled g_m -boosting technology is a power reduction approach, which also indicates that the same signal current will be modulated on the reduced DC current. The increased signal density would degrade the nonlinearity of system. Based on this consideration, the nonlinearity of CG with and without capacitively cross-coupled structures are simulated.

3.2 Capacitively Cross-coupled Common Gate LNA

The basic CS LNA topology is widely used because it provides good noise performance and high gain. In a CS configuration, source degeneration inductors are usually applied to the source of the active transistors in order to make a 50 Ω input matching network. However, using this approach it is hard to meet the broadband matching and gain flatness requirements. A three-section band-pass Chebyshev filter [22] or a two-section LC ladder [23] can achieve broadband matching and good noise performance. However, extra elements involved in the matching network increase the area and the complexity of the chip. Additionally, a CS LNA consumes high power. These disadvantages make the CS LNA a non-optimal choice in low power LNA design.

In contrast to CS LNA, CG LNA is a simpler approach due to its superior broadband input matching, linearity and low power consumption advantages. However,

the shortcoming of a CG LNA is that it presents a relatively high NF. A basic CG LNA is shown in Figure 3.1.



Figure 3.1 Basic CG LNA.

The dominant noise sources of the basic CG LNA are the noise current i_{ns} of the source resistance R_s , and the drain current noise source i_{nd} as shown in Figure 3.2, while the NF contributed by the gate noise of transistor M is usually negligible. The NF of the CG LNA is

$$F = 1 + \frac{\overline{i_{nd}^2} (\frac{1}{1 + g_m R_s})^2}{\overline{i_{ns}^2} (\frac{g_m R_s}{1 + g_m R_s})^2}$$
(3.2.1)

With $\overline{i_{nd}^2} = 4kT\gamma g_{d0}\Delta f$ and $\overline{i_{ns}^2} = 4kTR_s^{-1}\Delta f$, where g_{d0} is the zero bias drain conductance of transistor M. R_s is the source resistance. With an input matching condition of $g_m R_s \approx 1$, equation (3.2.1) reduces to

$$F = 1 + \frac{4kT\gamma g_{d0}\Delta f}{4kTR_S^{-1}\Delta f} \left(\frac{1}{g_m R_s}\right)^2$$

$$= 1 + \frac{\gamma g_{d0}}{g_m^2 R_s} = 1 + \frac{\gamma}{\alpha}$$
(3.2.2)

Where γ is the channel thermal noise coefficient (γ is typically 2/3 for long channel transistors and 2 for short channel transistors) and $\alpha = g_m / g_{d0}$. It is reported in [27] that the minimum NF of a CG-LNA is limited to 3 *dB*.



Figure 3.2 Dominant noise sources in the basic CG LNA [29].

To improve the noise performance of a CG LNA, a capacitively cross-coupled g_m boosting scheme is introduced in [27-29]. The presented CCC-CG LNA in [28] is inductively degenerated which occupies a large chip area and increases the cost of the chip. In this design work, current source transistors are used to achieve broadband matching with slightly increased NF. The designed CCC-CG LNA which is fully differential is shown in Figure 3.3.



Figure 3.3 Proposed fully differential CCC-CG LNA.

The inverting amplification value "*A*" in half circuit analysis in Figure 3.4 is approximately equal to the capacitor voltage division ratio

$$A = \frac{1/C_{gs}}{1/C_c + 1/C_{gs}} = \frac{1}{1 + C_{gs}/C_c}$$
(3.2.3)

Where C_C is the cross-coupled capacitor and C_{gs} is the parasitic capacitance of transistor M_1 and M_2 . Thus, the effective transconductance is expressed as

$$g_{m1,ef.f} = \frac{C_{gs} + 2C_c}{C_{gs} + C_c} g_{m1}$$
(3.2.4)

Usually, $C_C >> C_{gs}$, yielding $A \approx 1$ and

$$g_{m1,eff.} \approx (1+A)g_{m1} = 2g_{m1}$$
 (3.2.5)

The overall input admittance is

$$Y_{in} = g_{m1,eff.} + 1/r_{o2} + sC_{gs1}$$
(3.2.6)

The voltage gain with g_m -boosting is calculated as

$$A_{v} = g_{m1,eff} R_{L}$$
(3.2.7)



Figure 3.4 CG stage with g_m -boosting feedback [28].

In the designed CCC-CG LNA, the effective $g_{m1,eff.}$ is boosted to $2g_{m1}$. To satisfy the matching condition $g_{m1,eff.}R_s = 1$, the designed g_{m1} is equal to 10 mS. Contrast to the normal CG matching network shown in Figure 3.5, in which $g_{m1S} = 20 \text{ mS}$ and $i_{1s} = 2i_1$, the CCC-CG matching structure reduces half of the current flows in transistor M_{IS} and hence decrease the power consumption. Therefore, the CCC-CG LNA can load a higher resistance R_L and increase the gain of the matching network with 1.3 V supply.



Figure 3.5 A normal CG LNA.

3.2.1 Noise Analysis of the CCC-CG LNA

Generally, thermal noise and flicker noise are two typical significant noise sources of a MOSFET, but the dominant sources of noise at RF come from the transistors' thermal noise. The dominant noise sources in the normal CG LNA in Figure 3.5 are the noise current i_{ns} of the source resistance, drain current noise i_{nd1} and i_{nd2} of M_1 and M_2 , and i_L of the load resistor. Ignoring the gate current noise, the small-signal analysis reveals the NF of the normal CG LNA is

$$F = 1 + \frac{\overline{i_{nd1S}^2}(\frac{1}{1+g_{m1S}R_S})^2}{\overline{i_{ns}^2}(\frac{g_{m1S}R_S}{1+g_{m1S}R_S})^2} + \frac{\overline{i_{nd2S}^2}}{\overline{i_{ns}^2}} + \frac{\overline{i_L^2}}{\overline{i_{ns}^2}(\frac{g_{m1S}R_S}{1+g_{m1S}R_S})^2}$$
(3.2.1.1)

With $\overline{i_{nd1S}^2} = 4kT\gamma g_{d01S}\Delta f$, $\overline{i_{nd2S}^2} = 4kT\gamma g_{d02S}\Delta f$, $\overline{i_L^2} = 4kTR_L^{-1}\Delta f$ and $\overline{i_s^2} = 4kTR_S^{-1}\Delta f$, equation

(3.2.1.1) reduces to

$$F = 1 + \frac{\gamma g_{d01S}}{g_{m1S}^2 R_s} + \gamma g_{d02S} R_s + \frac{R_s}{R_L} \left(\frac{1 + g_{m1S} R_s}{g_{m1S} R_s}\right)^2$$
(3.2.1.2)

For a matched condition, we have $g_{m1S}R_s = 1$. Then equation (3.2.1.2) reduces to

$$F = 1 + \frac{\gamma}{\alpha} \left(1 + \frac{g_{d02S}}{g_{d01S}}\right) + \frac{4R_s}{R_L}$$
(3.2.1.3)

In the designed CCC-CG matching network, the matching condition of the CCC-CG satisfies

$$(1+A)g_{m1}R_s = 1 \tag{3.2.1.4}$$

The half circuit noise analysis of the CCC-CG is similar to the normal CG LNA. Combining (3.2.1.2) and (3.2.1.4), the NF of the CCC-CG matching network becomes

$$F = 1 + \frac{\gamma g_{d01}}{(1+A)^2 g_{m1}^2 R_s} + \frac{\gamma g_{d02}}{\alpha g_{d01}} g_{m1} R_s + \frac{R_s}{R_L} \left(\frac{1 + (1+A)g_{m1} R_s}{(1+A)g_{m1} R_s}\right)^2$$

$$= 1 + \frac{\gamma}{2\alpha} \left(1 + \frac{g_{d02}}{g_{d01}}\right) + \frac{4R_s}{R_L}$$
(3.2.1.5)

Comparing (3.2.1.3) to (3.2.1.5), the capacitively cross-coupled structure reduces the noise generated by M_{1S} and M_{2S} by a factor of 2.

3.2.2 S-parameter Test Setup of Fully Differential Circuit

The test setup illustrated in Figure 3.6 is the most commonly used simulation setup for a differential device-under-test (DUT) [30-31]. The DUT can be driven with a single source or differentially from both sources. The other differential terminal can be connected with a source resistance if using a single source. However, this traditional configuration cannot reject undesired common-mode signals and hence, has some potential errors and significantly reduce the reliability of circuits' performance.



Figure 3.6 Traditional test setup for simulating a differential amplifier [30].

To improve the test bench setup, an ideal_balun in the Analog Library of Cadence is used to perform differential- and common-mode simulations. In this case, v_d and v_c are the differential- and common-mode of the unbalanced pair of signals, and v_p and v_n are the balanced pair of signals. Thus, we have

differential-mode voltage	$v_d = v_p - v_n$
common-mode voltage	$v_c = (1/2)(v_p + v_n)$
positive voltage	$v_p = v_c + 1/2v_d$
negative voltage	$v_p = v_c - 1/2v_d$

The current flowing in/out of the ideal_balun are:

differential-mode current	$i_d = i_p - i_n$
common-mode current	$\dot{i}_c = (1/2)(\dot{i}_p + \dot{i}_n)$
positive current	$i_p = i_c + 1/2i_d$
negative current	$i_n = i_c - 1/2i_d$

S-parameter and noise analysis of the designed CCC-CG LNA is simulated with the test bench set-up shown in Figure 3.7. Since the system characteristic impedance is 50 Ω , the impedances with each port are 50 Ω . Therefore, the differential impedance seen by the DUT is 100 Ω and the common-mode impedance is 25 Ω . Hence, the reference resistance of ports P_{id} , P_{od} , and ports P_{ic} , P_{oc} are set to 100 Ω and 25 Ω , respectively.



Figure 3.7 Improved test setup of designed circuit [31].

3.2.3 Design and Simulation Results

In this design, transistor M_1 and M_3 are biased and sized with $1/(2g_{m1/3}) = 50 \Omega$. Two 1 *pF* capacitors (C_C) are used to cross-couple M_1 and M_3 . Transistors M_2 and M_4 are biased and sized for minimum NF contribution. As illustrated in Figure 3.8, the designed CCC-CG LNA achieves a simulated input match of -16 dB over the band and 16.4 dB gain with a 0.2 dB ripple.



Figure 3.8 Simulated gain and S11from 0.7 to 2.5 GHz.

The simulated NF of the normal CG LNA and the designed CCC-CG LNA are shown in Figure 3.9. For fair comparison, the CG LNA and the CCC-CG LNA are designed with an equivalent transconductance and load resistance and hence, they have the same matching condition and gain. The designed CCC-CG matching network achieves a minimum NF of 3.0 *dB* and reduces the NF of the normal CG around 0.8 *dB*.



Figure 3.9 Simulated NF from 0.7 to 2.5 GHz.

The designed predistortion circuit has a differential input and single ended output configuration (the details of the design work are described in Chapter 4). The noise performance of the predistortion circuit is simulated by using the test bench depicted in Figure 3.7 but with a single port at its output. The maximum NF of the entire predistortion circuit is 6.65 dB as illustrated in Figure 3.10.



Figure 3.10 Simulated NF of the predistortion circuit from 0.7 to 2.5 GHz.

3.3 Nonlinearity Analysis of the CG LNA and CCC-CG LNA

The 1 dB compression point and IP_3 are figures of merit to evaluate the nonlinearity of an LNA. Pure frequency-domain simulators (e.g. harmonic balance tools) can be used to compute input referred IIP_3 . In Figure 3.11 and Figure 3.12, the simulated values of input and output powers are plotted with bold lines and the asymptotes with expected slope are plotted with dash lines. The nonlinearity comparison of the CG LNA and the CCC-CG LNA keeps the equivalent transconductance and load resistance. As shown in Figure 3.11 and Figure 3.12, the IIP_3 of the CCC-CG LNA is 4.7 *dB* lower than CG LNA.



Figure 3.11 Third-order input intercept point of the CG LNA when $f_0=0.7$ GHz.

Periodic Steady State Response



Figure 3.12 Third-order input intercept point of the CCC-CG LNA when $f_0 = 0.7$ GHz.

The triplet-core circuit requires pure RF tones as its input. Otherwise, distortion terms in the distorted output of the matching network are recognized as signal inputs to the triplet-core and hence, generate distortion products. The nonlinear effects of the matching network will be evaluated in the entire circuit simulation in Chapter 4.

The simulated *IIP3* and NF of the designed CG LNA and the CCC-CG LNA which have an equivalent transconductance and load resistance are shown in Table 3.1. Although the *IIP3* of the CCC-CG LNA is degraded, it has a low NF which is considered necessary in the matching network design. Therefore, compared to the CG LNA, the CCC-CG LNA matching network is a better approach.

Table 3.1 Simulated characteristics of CG LNA and CCC-CG LNA

Parameters	IIP3 (dBm)	NF (dB)
CG LNA	-1.26	3.8
CCC-CG LNA	-6.01	3.0

3.5 Conclusion

A g_m -boosting CG topology of matching network is introduced in this chapter. The designed fully differential CCC-CG LNA exhibits a lower NF, consumes less power and degrades the linearities in contrast to the conventional CG LNA. The designed CCC-CG matching network obtains a simulated 16.4 dB gain, minimum 3.0 dB NF and consumes 1.9 mW with 1.3 V supply. The maximum NF of the entire predistortion circuit is 6.65 dB.

CHAPTER 4 DESIGN OF THE AMPLIFIER-BASED TUNEABLE RF PREDISTORTION

4.1 Introduction

In Chapter 2, we analyzed the principle of predistortion linearization and presented a triplet-core circuit to generate the desired distortion. Matching considerations of the triplet-core with the characteristic impedance of the RF system are presented. A matching network design and simulation results were presented in Chapter 3. This chapter discusses the design methods of the proposed amplifier-based RF predistortion circuit. The architecture of the predistortion circuit is described. A state-of-the-art design using both static and dynamic current mirrors is studied. The predistortion IC solution provides both modulation current and controllable bias current to drive the DFB-LD. Simulation results are presented showing the expected predistortion functions.

4.2 Design Guidelines of the Amplfier-Based Tuneable RF Predistortion Circuit

This section describes the outline of the analog predistortion IC based on system level specification. On-chip and off-chip components are selected in order to minimize chip area and reduce the cost. The system and chip architecture are presented. The circuit blocks include current mirror bias circuits, a current injection structure and a power supply output stage.

4.2.1 System Architecture Consideration



Figure 4.1 Block diagram of the system architecture.

Figure 4.1 shows the system architecture. It contains an off-chip 180^{0} hybrid coupler, two 20 *pF* off-chip capacitors C_{c1} and C_{c2} , and the predistortion IC consisting of the CCC-CG matching network and the proposed distortion generator. The off-chip 180^{0} hybrid coupler converts the single-ended signal to differential. C_{c1} and C_{c2} couple the differential signal into the predistortion IC. The CCC-CG matching network amplifies the signal supplied to the distortion generation block. The distortion generator can be tuned to produce the desired IMD3 to compensate the nonlinear distortion of the DFB-LD. The CCC-CG matching network is fully differential. The distortion generator converts the architecture makes it easier to integrate the system with other components. The detailed chip architecture is depicted in Figure 4.2.



Figure 4.2 Chip architecture.

In contrast with traditional matching approaches, CCC-CG allows broadband input matching without inductors which are usually used when designing LNAs. The only components which take a large area are the cross-coupling capacitors. They are selected

to be 1.07 pF and have a dimension of 26 μm *26 μm (available in mimcap_um, tsmcN90rf library). The CCC-CG supplies both carriers and the DC bias to the proposed triplet-core circuit. Compared with other existing RFICs, the signal path does not require any DC feed or AC coupling. The distortion generator includes the triplet-core circuit, which was described in Section 2.3.2, the current injection structure, the active current mirrors and the output power supply stage. The distortion signal generated by the triplet-

core circuit can be amplified up to $16 \ mA$ by the active current mirrors. A currentinjection technique is used to improve the efficiency of current mirrors. An additional transistor M_{13} provides a signal current of $9 \ mA$ maximum and a bias current of $30 \ mA$ maximum to the DFB-LD. The bias current of the DFB-LD can be controlled by I_{ref} .

More details about the output stage power supply are described in Section 4.2.4.

4.2.2 Current Mirror Design

Current mirrors are one of the most important building blocks of analog Very Large Scale Integration (VLSI) circuits. Various analog blocks use current mirrors designs. Analogto-digital converters (ADC), amplifiers, comparators are using them. Current mirrors are circuits designed to source and sink a constant current. They are extensively used to replicate accurately an input current. A well designed current mirror has high output impedance, a wide operating range and provides a constant current source. This section explains different types of current mirrors used in the proposed predistortion block. This included a basic current mirror, a cascode current mirror and an active current mirror.

4.2.2.1 Basic Current Mirror



Figure 4.3 A basic current mirror.

A basic current mirror [18] consisting of M_1 and M_2 is shown in Figure 4.3. The principle of the current mirror designs are explained with the square-law model of long channel MOSFET while ignoring short channel effect with little loss in accuracy. The diode connected transistor M_1 defines the gate-to-source voltage of M_2 , hence $V_{GS1}=V_{GS2}$. Normally, M_1 and M_2 are operating in saturation. If the two transistors are matched and operated in the saturation region, the current of I_{out} matches that of I_{ref} . Thus, we have

$$I_{ref} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_1 (V_{GS1} - V_{TH})^2 (1 + \lambda_{DS1})$$
(4.2.2.1.1)

$$I_{out} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_2 (V_{GS2} - V_{TH})^2 (1 + \lambda_{DS2})$$
(4.2.2.1.2)

Where μ_n is the carrier mobility in the conducting channel and C_{ox} is the oxide capacitance per unit area. W_1/L_1 and W_2/L_2 are the ratio of device dimensions of M_1 and M_2 , respectively. V_{TH} is the threshold voltage and λ_1 , λ_2 are the channel-length modulation factors of M_1 and M_2 , respectively.

Neglecting channel-length modulation, we have

$$I_{out} = \frac{(W/L)_2}{(W/L)_1} I_{ref}$$
(4.2.2.1.3)

In this case, M_1 and M_2 need not to be identical. M_1 and M_2 are chosen the same length in order to minimize errors due to the side diffusion of the source and drain area. The desired output current can be obtained by simply scaling the ratio of transistor width of M_1 and M_2 .

In this design work, the typical basic current mirrors are used to bias the current source transistors of the CCC-CG stage, the tail currents of the triplet-core circuit and the DC current of the DFB-LD (refer to Figure 4.2 for more details).

4.2.2.2 Cascode Current Mirror

Excellent current matching is desirable in current mirror designs. Accordingly, a well designed current mirror has high output resistance and excellent device matching. As we know, the basic current mirror is the simplest method to reproduce identical current in a different path. In spite of this, it has some disadvantages. The output current cannot accurately replicate the input due to a difference in effective length due to channel-length modulation. The basic current mirror has difficulty overcoming these drawbacks and thereby limits its application in IC design.

In contrast to a basic current mirror, cascode current mirrors are usually employed to minimize channel-length modulation effects. Cascode current mirrors are an attractive solution to achieving high output resistance, using low voltage and having high accuracy. They are used in many applications. In the CCC-CG matching design (half of the CCC-CG circuit is shown), transistors M_1 and M_2 are biased by current mirrors. The bias



network of the CCC-CG matching network is shown in Figure 4.4.

Figure 4.4 Current bias network the CCC-CG matching network.

The desired bias voltages V_{bias1} and V_{bias2} are 0.72 V and 0.55 V, respectively. V_{bias1} biases transistor M_1 of the CCC-CG and also processes the cross-coupled signal. To prevent the signal from entering M_{b6} , a transistor based resistor M_{bRa} is inserted between the bias network and transistor M_1 , adding about $1 k\Omega$ resistance. The bias voltages V_{bias2} is defined by

$$V_{bias2} = V_X = V_{GS,b1} \tag{4.2.2.2.1}$$

Transistor M_{b6} can be sized with a shorter width or longer channel length to give a higher overdrive voltage to bias M_2 .

$$V_{bias1} = V_{DS,b6} = V_{GS1} + V_{ov2} \tag{4.2.2.2.2}$$

In Figure 4.4, we have

$$V_{DS,b2} = V_{DD} - V_{GS,b4} \tag{4.2.2.2.3}$$

Where
$$V_{DS2} = V_{bias1} - V_{GS1} \tag{4.2.2.2.4}$$

This can lead to a difference between I_{out1} and I_{out} . The difference is dependent on V_{DD} and $|V_{TH,p}|$. Uncertaint in I_{out} can lead to uncertaint in the proximate of the triode or saturation boundary for M_1 and M_2 . The bias network in Figure 4.4 can be improved by putting a cascode transistor above M_{b2} as shown in Figure 4.5. In this circuit $V_{DS,b2} = V_{DS2}$, which gives a better match between I_{out1} and I_{out} , leading to a better prediction of the bias condition for M_1 and M_2 .



Figure 4.5 An improved bias network of the CCC-CG stage.

4.2.2.3 Active Current Mirror

As we know, current mirrors can be used to process signals. In this design, the active current mirror also converts the differential signal to a single ended output. Compared with a fully differential configuration, a single ended structure has a lower bandwidth because an internal high frequency pole is introduced by the diode-connected configuration and hence reduces the bandwidth. However, a single ended output is a superior option to enhancing the cascade capability of the predistortion system.

The triplet-core circuit uses a fully-differential configuration. It drives an active load formed by transistors M_5 and M_{10} . The circuit is shown in Figure 4.6. The currents flowing into transistors M_5 and M_{10} define the gate-to-source voltages of M_7 and M_{11} , respectively. The signal passes through M_7 , M_8 , and M_{12} . The differential currents are subtracted at node P. An extra signal path through M_{13} is introduced to produce more signal current and a portion of the common-mode current to the DFB-LD.



Figure 4.6 Proposed active current amplification stage.

For an active current mirror, if i_{in} increases by ΔI , then i_{out} increases by ΔI $(W/L)_i/(W/L)_i$ which indicates that the current mirror amplifies the small-signal current if $(W/L)_i/(W/L)_i > 1$. If the current mirror is designed with a ratio k, both bias current and signal current are amplified by a factor of k. The signal amplification is achieved by increasing system power dissipation. In this work, the current ratio of M_5 and M_7 , M_{10} and M_{11} , M_8 and M_{12} , M_8 and M_{13} are shown in Table 4.1. In this design, the current ratio k_1 , 56

and k_2 are selected based on the modulation requirement of the DFB-LD. If the signal current at each differential output of the triplet-core is Δi , the total signal current available to drive the DFB-LD is $(2k_1 + k_2)\Delta i$. Based on bandwidth optimization consideration, the mirror ratio of M_5 and M_7 is chosen to be $1/\sqrt{k_1 + k_2}$.

Table 4.1 Active current mirrors involved in Figure 4.6.

Current Mirror	M_{5}/M_{7}	M_{10}/M_{11}	M ₈ /M ₁₂	<i>M</i> ₈ / <i>M</i> ₁₃
Mirror ratio	$1/\sqrt{k_1 + k_2}$	$1 / k_1$	$\sqrt{k_1 + k_2} / k_1$	$\sqrt{k_1 + k_2} / k_2$

4.2.3 Current Injection Technique

The current injection technique, also known as current bleeding, is a very attractive approach for biasing circuit designs. A charge injection method used by Gilbert cells is presented in [32-33]. This type of biasing topology provides several advantages over the traditional biasing techniques. Firstly, this topology enables an easy way to adjust the bias current present in the Gilbert cell input transistors while keeping the bias current in other transistors steady. Secondly, the Gilbert cell benefits by improved gain and linearity by using current injection method (the linearity enhanced by increasing *IP3* which was discussed in Section 3.3). As explained in [32], increasing I_{ss} can improve the gain and *IP3* of Gilbert cells. Thirdly, this biasing method reduces the voltage headroom. Low voltage and low power are a trend in future integrated circuit designs.

The current injection circuit shown in Figure 4.6 is outlined in the blue dotted lines. The two PMOS transistors M_6 and M_9 supply some of the DC current to the triplet-core circuit. Transistors M_5 , M_6 , M_9 and M_{10} have the same W/L dimensions. Hence, the

current injection circuit establishes an identical drain current in M_5 , M_6 , M_9 and M_{10} . Transistor M_6 and M_9 are biased by a current mirror which can provide half of the tail current of the triplet-core circuit. Therefore, half of the tail current flows into the drains of active current mirror transistors M_5 and M_{10} . The input impedance at the drain of M_6 is high. Therefore, the RF signals only flow into the active current mirror. The current copier M_7 and M_{11} , with a factor of $\sqrt{k_1 + k_2}$ and k_1 , multiplies half the DC current while keeping the same signal current. With the current injection method, the transistor size of M_7 , M_8 , M_{11} , M_{12} and M_{13} can be reduced to half compared to the transistor sizes without using current injection. Therefore, the current injection approach reduces power dissipation of the proposed predistortion circuit by more than 100 mW.

4.2.4 Laser Bias Circuit and Output Stage Power Supply

The output stage power supply for the DFB-LD is shown in Figure 4.7. Transistor M_{12} processes the modulation current while M_{14} supplies additional bias current to drive the DFB-LD. Transistor M_{13} provides both modulation and bias current. The basic current mirror of M_{14} and M_{15} , with a W_{14}/W_{15} ratio of 8, supplies a tuneable bias current. By adjusting the current source I_{b4} from 0.625 mA to 10 mA, M_{14} could supply a current in the range of 50 ~ 80 mA to the DFB-LD. If the voltage at node P is V_p and the forward voltage of LD is V_{fd} , then the value of +V is $V_p + V_{fd}$. Typically, the offset voltage of node P is set to be 0.7 V. To improve the matching and avoid input signal degradation, the input termination of the DFB-LD has to be physically placed as close as possible to the predistortion IC using bonding wires.



Figure 4.7 Laser diode power supply.

4.3 Circuit Performance Evaluation

Harmonic balance (HB) [34] is a frequency-domain analysis technique to calculate the steady-state response of electrical circuits. It is a useful method to perform analysis of strongly or weakly nonlinear circuit. It is normally the preferred analysis method chosen by simulators when investigating analog RF systems.

The complete chip is designed using the Cadence design environment. To evaluate system performance, Spectre circuit simulator is used. Spectre is a state-of-theart tool used to simulate RFICs, such as power amplifiers, LNAs and mixers. HB simulation in Periodic Steady-State (PSS) analysis is used to compute the nonlinearity of the predistortion circuit.

4.3.1 Two-Tone Signal Simulation

Multiple frequencies or tones (typically two-tones) are usually used to evaluate IMD in analog RF or microwave circuits. In the simulator, the two-tone signal is generated using a power source *port* component, which is available in the Analog Library of Cadence. This source provides two sinusoidal signals with zero degree phase offset at a specified power level. In the simulation set up, the two fundamental frequencies are 1600 *MHz* and 1604 *MHz* with an input power of $-25 \, dBm$. The internal source resistance is set to 50 Ω . To convert the single input to differential, an S2P file based 180⁰ hybrid coupler is used. Current sources I_{b1} , I_{b2} , I_{b3} and I_{b4} are used to bias the predistortion circuit. I_{b1} supplies the bias current to the biasing network. I_{b2} and I_{b3} are tuneable sources that adjust the nonlinearity of the predistortion circuit. I_{b4} controls the DC supply of the DFB-LD. The DFB-LD is biased at 35 *mA* and modulated with a current of 16 *mA*. In order to reach the modulation strength needed by the DFB-LD, the total input power of the predistortion circuit is set to $-25 \, dBm$, corresponding to $25 \, mV$ peak-to-peak for each differential input branch. Therefore, the equivalent transconductance of the differential input predistortion circuit is 0.64 *S*. The simulation setup of the predistortion IC which includes the CCC-CG matching network and distortion generation block is illustrated in Figure 4.8.



Figure 4.8 Harmonic balance simulation setup of the DFB-LD with predistortion circuit.

To compare the linearity improvement, we set the output power level constant and compare the IMD3 to carrier ratios between the linearized and nonlinearzed DFB-LD. Figure 4.9 (a)-(b) shows the simulated RF spectra at the output of the DFB-LD without and with predistortion, respectively. It is shown that the predistortion circuit reduces IMD3 to less than 50 *dBc*. This gives an IMD3 suppression of 12 dB.



Figure 4.9 Simulated spectra at the output of the DFB-LD, (a) without and (b) with predistortion (matched) circuit.

Next, we vary the input power and measure the DFB-LD output RF power of the carrier and IMD3 with and without predistortion. The predistorted DFB-LD satisfies system requirement over a wide dynamic range of current input up to $20 \ mA$ (corresponding to $-30.6 \ dBm$ output RF power). The predistortion circuit is optimized at high power level to increase the dynamic range of the DFB-LD. Figure 4.10 shows that the third-order nonlinearity is fully suppressed for output power greater than $-32.6 \ dBm$. Even though the IMD3 is not fully suppressed at lower power, the predistortion circuit improves IMD3 suppression by more than $10 \ dB$ and the system still satisfies the required $45 \ dBc$ suppression of IMD3 below the carrier.



Figure 4.10 Simulated carrier and IMD3 of DFB-LD, with and without predistortion (matched)

circuit at 1600 MHz.

Furthermore, the performance of the predistortion circuit is simulated for broadband operation with a two-tone signal input. The frequency spacing between the two tones is kept at 4 MHz and the operation frequency of the first tone is swept from 0.7 to 2.5 GHz in steps of 100 MHz. The results of theoretical analysis using nonlinear transmission coefficients are plotted in Figure 4.11. Theoretically, the IMD3/C can be improved by 13.4 dB at 16 mA current input power level. With the predistortion circuit, the IMD3/C is improved by 15 dB at 700 MHz and 10 dB at 2500 MHz. This is because the theoretical analysis of the predistortion circuit transfer function is limited to the thirdorder nonlinearity with frequency independent coefficients. The simulated predistortion circuit cancels some IMD3 terms generated by higher order nonlinearity. The poor performance of the predistortion circuit at high frequency may be due to the high insertion loss at high frequency, the matching circuit and the presence of nonlinear parasitic capacitance that increases the phase shift between the carrier and IMD3 [34-35]. The parasitic capacitance of MOSFET is usually nonlinear. Nonlinear capacitors increase the phase shift between signal carrier and distortion terms with the increase of operation frequency.



Figure 4.11 Simulated IMD3/C of DFB-LD, theoretical analysis, with and without predistortion (matched) from 0.7 to 2.5 *GHz*.

We compared the distortion suppression with matched and unmatched predistortion circuit. The unmatched predistortion circuit only contains the distortion generation block. The CCC-CG matching network degrades IMD3 cancellation, as depicted in Figure 4.12. The effect of the nonlinear parasitic capacitance that increases the phase shift between carrier and IMD3 is evident in Figure 4.13 for the unmatched predistortion circuit. The matching network generates some distortion products and increases the phase mismatch between the carrier and IMD3 as shown in Figure 4.13. These distortion products are amplified by the distortion generation block along with the carriers and are sent to the DFB-LD. When these amplified distortion products are comparable with the ones generated by the distortion generation block only, they interact destructively and reduce the amount of IMD3 input to the DFB-LD to suppress its third-order nonlinearity. To reduce the nonlinearity effect caused by the CCC-CG matching network, the triplet-core circuit is tuned to generate more distortion signal.



Figure 4.12 Simulated IMD3/C with matched and unmatched predistortion circuit.



Figure 4.13 Simulated phase difference between signal carrier and IMD3 with matched and unmatched predistortion circuit.

4.3.2 Tuneability Evaluation

Another advantage of this predistortion circuit is that the generated IMD3 can be varied by up to 10 dB by tuning the bias current I_2 and I_3 . For effective third-order nonlinearity suppression of a DFB-LD, there is a required amount of IMD3 to be generated by the predistortion circuit at the input of DFB-LD. The nonlinearity of the triplet-core circuit was discussed in Section 2.3.3. As we shown, tuning the bias current of differential pairs would change the nonlinearity of the entire transconductance. Adjusting the bias current should keep the active current mirrors in saturation.

Figure 4.14 is plotted by feeding the output current of the predistortion circuit to a 50 Ω load. The bias current I_1 and I_3 , I_2 of the proposed triplet-core circuit can be tuned by adjusting the bias current of M_{16} and M_{17} (refer to Figure 4.2 for more information). Since I_1 and I_2 can be tuned from 2.6 ~ 3 mA and 0.8 ~ 2 mA while the current mirror ratio of M_{16}/M_{1C} and M_{16}/M_{2C} are 1/2 and 1, respectively. Correspondingly, the bias currents I_{b2} and I_{b3} of the predistortion circuit can be adjusted from 1.3 ~ 1.5 mA and 0.8 ~ 2 mA respectively. IMD3 can be increased by reducing I_{b2} or increasing I_{b3} . The highest dynamic range of IMD3 is obtained when I_{b2} is 1.3 mA and I_{b3} is 2 mA. The strong tuneability enables the predistortion circuit to correctly linearize some unknown LD sources.



Figure 4.14 Simulated output power of the predistortion circuit for different bias currents I_{b2} and I_{b3} .

4.4 Comparison of This Work with Previous Predistortion

Comparing the designed amplifier-based predistortion with the most recently published predistortion in circuit level [2, 7-10], this work has three advantages. First, the designed predistortion circuit achieves $6 \sim 15 \ dB$ IMD3 suppression over a broadband operation, from 700 *MHz* to 2500 *MHz*. The IMD3 suppression of this predistortion circuit is comparable with [8], which is designed for a single operation frequency. Second, the designed amplifier-based predistortion circuit uses a single path to predistort and amplify the signal. Contrasting to the multi-path configuration in [2, 7-10], this design has a simple structure. Third, as opposed to the voltage-mode currently reported CMOS

predistortion circuit [7, 10], the designed predistortion is a current-mode approach which supplies directly current source to the LD. Although the predistortion circuit in [8] is a current approach, our design can supply higher modulation current and operate in much broader bandwidth. Table 4.2 shows a comparison of this work and recently published predistortion circuit.

	Tech.	Operating Frequency (MHz)	IMD3 Suppression (dB)	Complexity
This work	90 nm CMOS	$700 \sim 2500$	6~15	Low
[10]	0.18 µm CMOS	1850 ~ 2150	5~10	High
[9]	Not reported	5800	16	High
[8]	0.35 µm CMOS	1350	12	High
[7]	0.18 µm CMOS	$50 \sim 500$	5~10	High
[2]	Not reported	$370 \sim 480$ $820 \sim 960$ $1710 \sim 1980$	6~10	High

Table 4.2 Comparison of previously published predistortion design

4.5 Conclusion

In this chapter, detailed information of the circuit design is introduced. The predistortion circuit consists of basic, cascode and active current mirror networks. The current injection technique significantly improves the efficiency of current amplification and reduces power dissipation. The predistortion IC supplies a modulation signal of up to $25 \ mA$ and bias current of $110 \ mA$ with $200 \ mW$ of power consumption. The equivalent transconductance of the predistortion IC is $0.64 \ S$. The predistortion circuit is simulated

using Cadence Virtuoso Spectre circuit simulator. The designed predistortion achieves more than 10 dB improvement from 0.7 to 2.5 *GHz*. By adjusting the bias currents, the IMD3 can be shifted 10 dB, which is suitable to linearize other LDs.

CHAPTER 5 CONCLUSION

5.1 Conclusion

In wireless access networks, RoF systems have the highest potential to satisfy large capacity, high speed and cost effective requirements. However, the nonlinearity introduced by optical modulators' response significantly distorts RoF transmission. Among currently available linearization techniques, predistortion is selected to linearize the DFB-LD.

In this thesis, an amplifier-based tuneable RF predistortion IC solution is investigated and designed using TSMC 90 nm technology. The complete circuit includes a triplet-core circuit, matching networks and current mirror designs. The IC supplies up to $25 \ mA$ modulation current and $110 \ mA$ bias while consuming $200 \ mW$. It is capable of suppressing IMD3 up to $15.4 \ dB$ compared to the free-running DFB-LD at $16 \ mA$ signal amplitude input. The frequency of operation ranges from 0.7 to 2.5 *GHz*.

The presented predistortion circuit is the first gain boosting IC solution which provides a cost effective approach. The designed predistortion circuit does not require external amplifiers or phase shifters because they would introduce undesired IMD3 and limit the operation bandwidth. Also, the gain boosting predistortion circuit makes it possible to remove the LNA which is the block just before the modulator. Thirdly, the IC is broadband matched without using inductors. Inductors take up a large amount of chip area. Therefore, the predistortion IC solution reduces system cost significantly.

5.2 Future Work

The future results of extensive research done on the predistortion IC are described:

The IC layout and fabrication are the first considerations. Since the input has a fully differential configuration, careful design is necessary to ensure symmetry of the CCC-CG stage and to the input path of the triplet-core circuit. Also, the symmetrical parts of LNA and active current mirrors have to be matched. Otherwise, the different signal delay will diminish the capability of IMD3 suppression.

The second consideration involves testing the chip. It is necessary to design a PCB which includes a broadband 180° hybrid coupler and two off-chip 20 *pF* capacitors. The 180° hybrid coupler converts the single ended input RF signal to differential inputs. The differential signals are coupled to the predistortion IC using two 20 *pF* capacitors. To reduce the interconnection loss between the predistortion IC and DFB-LD, the two blocks are placed physically close and a bonding wire is used to connect them together.

The third consideration involves the proposed approach to improving the system's stability. As we know, the laser's band gap changes with temperature and thermal expansion and hence, varies the nonlinearity of LDs. Therefore, an adaptive temperature control circuit would enhance its temperature tolerance. In the future, instead of using discrete devices, the predistortion IC and DFB-LD can be fabricated in one package. Therefore, the cascaded commercialized modulator can provide a much more linear transmission in RoF systems.

Last but not the least, more advanced TSMC technologies, like 65 nm, 40 nm or 28 nm can be used to design a high frequency, Ultra-Wideband and low power analog

predistortion IC. Additionally, an automatic gain control LNA can be designed to regulate the signal input to the distortion generation block. Also, the predistortion circuit can be modified to linearize power amplifiers (PAs) and other modulators as well.

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