

Urban Sprawl Metrics (USM) Toolset – User Manual for QGIS

First edition, 23 August 2023

Parnian Pourtaherian^a, Naghmeh Nazarnia^a, Christian Schwick^{b,c}, Yves Maurer^d, Joel Schwab^e, Jochen A.G. Jaeger^{a,*}

^a Concordia University Montreal, Department of Geography, Planning and Environment, 1455 De Maisonneuve Blvd. West, Suite H1255, Montreal, QC, H3G 1M8, Canada

^b Die Geographen schwick+spichtig, Turbinenstrasse 60, CH-8005 Zurich, Switzerland

^c Swiss Federal Research Institute WSL, Zürcherstrasse 111, CH-8903 Birmensdorf, Switzerland

^d Swiss Federal Office for Spatial Development (ARE), CH-3003 Bern, Switzerland

^e Institute for Software (IFS), Ostschweizer Fachhochschule OST, Oberseestrasse 10, CH-8640 Rapperswil, Switzerland

* Primary contact, jochen.jaeger@concordia.ca

The Urban Sprawl Metrics (USM) Toolset is a geographic information system (GIS) toolset and was developed using Python and C+ languages. This tool is freely available under the Creative Commons Licence¹ and can be downloaded from the Institute for Software (IFS), Geometa Lab² GitLab (www.gitlab.com/geometalab/usm_toolset/usm_calculator) as well as from Spectrum, Concordia University's open access research repository (spectrum.library.concordia.ca) or can be accessed directly on the QGIS Repository (https://plugins.qgis.org/plugins/usm_calculator-main/). Two versions are currently available, one for QGIS and one for ArcGIS version 10.1 (ESRI, 2010) or higher. This User Manual is for the QGIS version.



Fig. 1: Example of a landscape from Switzerland that includes built-up areas (close to Zurich). The USM Toolset can be used to measure the degree of urban sprawl of this landscape (photo: J. Jaeger, 2015).

¹ distributed under the terms of the Creative Commons Attribution-NonCommercial-NoDerivatives License (<http://creativecommons.org/licenses/by-nc-nd/4.0/>), which permits non-commercial re-use, distribution, and reproduction in any medium, provided the original work is properly cited, and is not altered, transformed, or built upon in any way. Permission is granted subject to the terms of the License under which the work was published. Please check the License conditions for the work which you wish to reuse.

² Part of Eastern Switzerland University of Applied Sciences (OST)

Table of contents

1. Introduction
 2. Important background information
 - 2.1 Definition of built-up areas
 - 2.2 Metrics of urban sprawl
 - 2.3 Choice of the Horizon of Perception
 - 2.4 Job data full-time equivalents
 - 2.5 City boundaries adjustment for comparison of cities of differing sizes (optional)
 3. Installation of the Urban Sprawl Metrics (USM) Toolset
 - 3.1 Urban Sprawl Metrics Toolset archive
 - 3.2 Step by step installation guide
 4. How to use the Urban Sprawl Metrics Toolset
 - 4.1 Calculate Weighted Urban Proliferation tool
 - 4.1.1 How to use the Calculate Weighted Urban Proliferation tool
 - 4.2 Recalculation (Explore Weighted Urban proliferation) tool
 - 4.2.1 How to use the Recalculation (Explore Weighted Urban proliferation) tool
 5. Examples of using the USM Toolset
 - 5.1 Six simple hypothetical model landscapes
 - 5.2 One example of an urban landscape from Canada
 - 5.3 Six European cities with and without greenbelts
- Acknowledgements
- Suggested References

1. Introduction

The USM Toolset was developed to facilitate the calculation of Weighted Urban Proliferation (*WUP*) and all components of urban sprawl for landscapes that include built-up areas (e.g., dispersion (*DIS*), land uptake per person (*LUP*); Fig. 1). The Toolset is straightforward to use. The language of the user interface is English. The Toolset requires three input data:

- (1) the binary map of built-up areas (settlements areas and/or solitary buildings), in raster format;
- (2) the geometry of reporting unit(s) (e.g., municipalities, districts, or a grid of a certain cell size) in vector format; and
- (3) the number of inhabitants and jobs for the reporting unit(s) (this information must be saved by the user in the attribute table of the reporting unit(s) shapefile); and
- (4) the share of settleable area for the reporting units to calculate WUP_b (optional).

2. Important background information

A variety of definitions have been proposed in the literature in the last hundred years (Fig. 2). However, no agreement about the main components has been achieved so far. Most importantly, the conceptual diversity is caused by some attempts to define urban sprawl using its causes and consequences and including them in the definition. However, it is advisable to differentiate the causes and consequences of urban sprawl from the main phenomenon (Schwick et al. 2012).

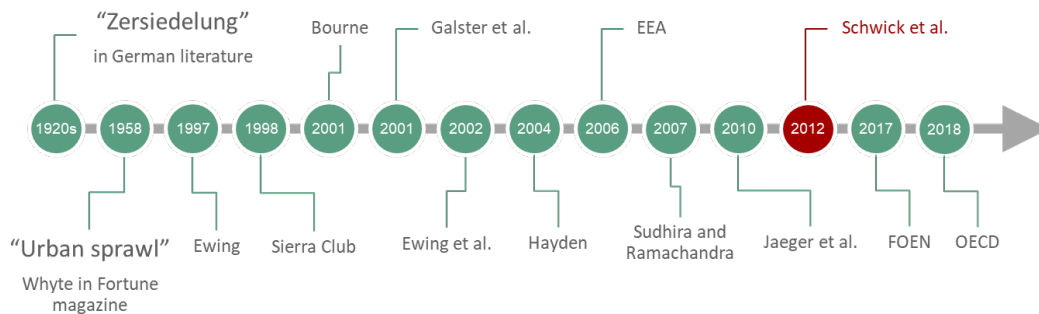


Fig. 2: Timeline of most common definitions of urban sprawl.

The metrics of Weighted Urban Proliferation (*WUP*) and Weighted Sprawl per Capita (*WSPC*) have three components: *PBA*, *DIS* and *LUP* (or *UD*) (Fig. 3).

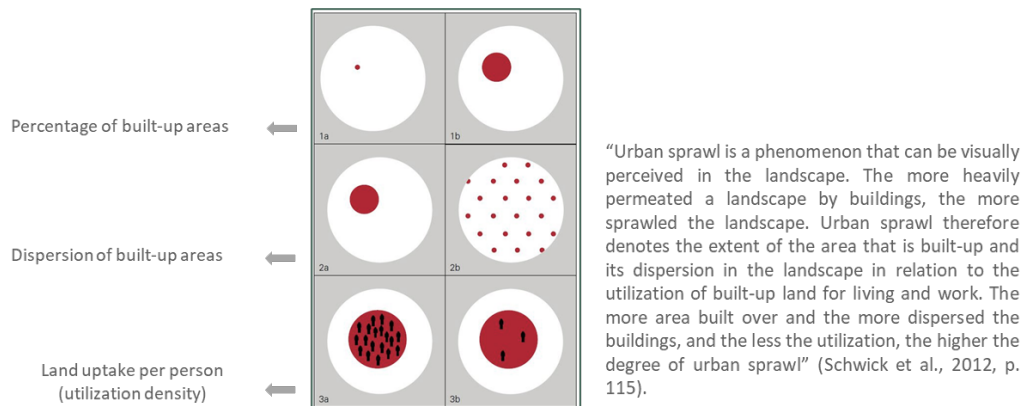


Fig. 3: The three components of urban sprawl *PBA*, *DIS*, and *LUP* (Schwick et al. 2012).

The relationships between the metrics of Weighted Urban Proliferation (*WUP*) and Weighted Sprawl per Capita (*WSPC*) and their three components: *PBA*, *DIS* and *LUP* (or *UD*) are illustrated in Fig. 4.

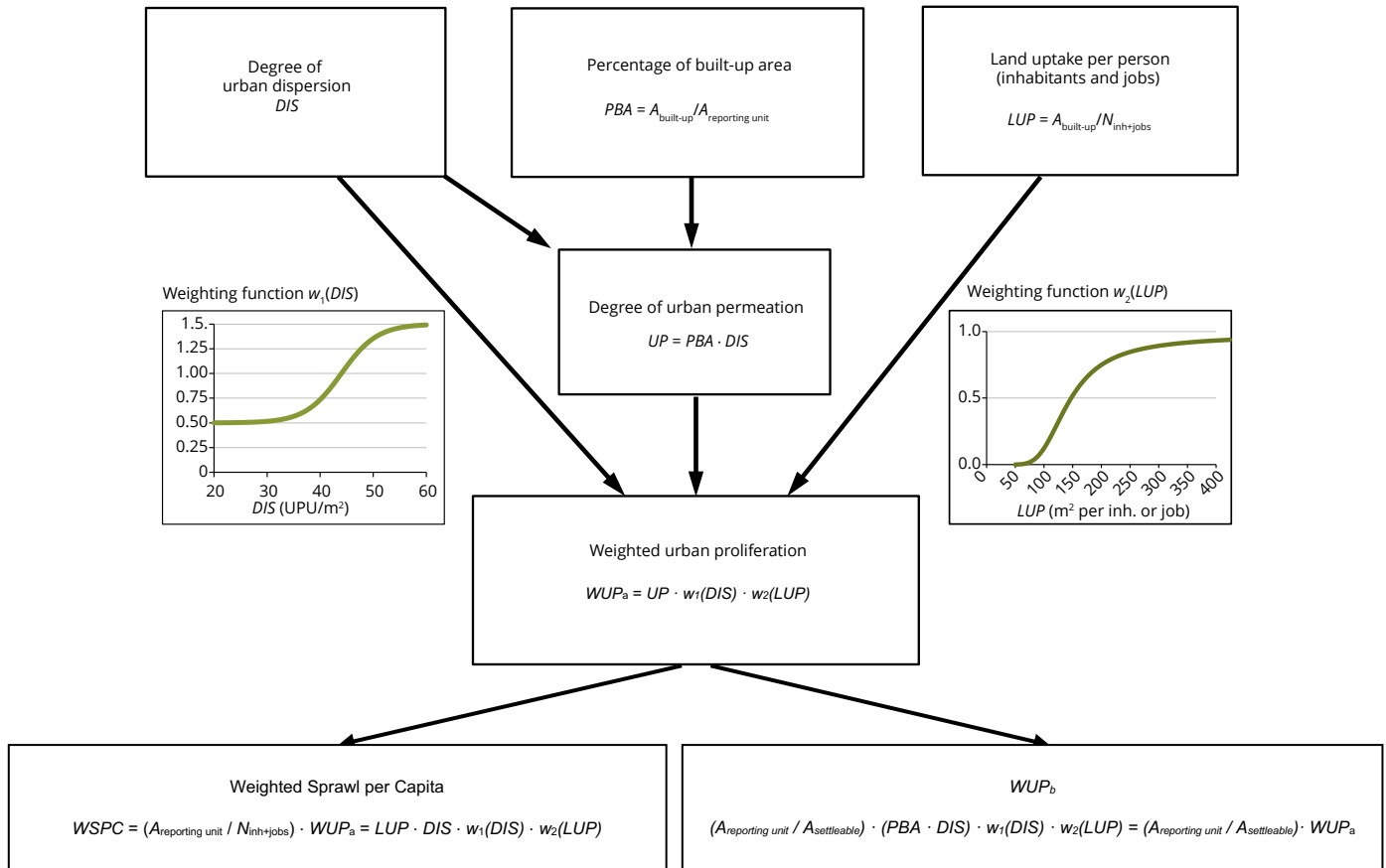


Fig. 4: The relationships between the *WUP* metric (*WUP_a* and *WUP_b*) and the *WSPC* metric and their components *DIS*, *PBA*, and *LUP* (EEA & FOEN 2016: 39). The *DIS*, *PBA* and *UD* (= 1/*LUP*) metrics are intensive metrics. $A_{reporting\ unit}$ = area of the reporting unit (the landscape studied); $A_{built-up}$ = size of built-up area in the reporting unit; $N_{inh+jobs}$ = number of inhabitants and jobs in the built-up area of the reporting unit. The shapes of the weighting functions are shown in the boxes as indicated.

Users who already have sufficient knowledge of the definition of built-up areas and the metrics of urban sprawl can continue reading in section 3 (installation of the USM Toolset). However, if the users do not yet have adequate background knowledge, we highly recommend that they read this section carefully or the paper by Jaeger and Schwick (2014) or the first part (sections 2.1 and 2.2) of Chapter 2 "Measurement of urban sprawl, base data, and hypotheses about potential drivers" in the report "Urban sprawl in Europe" (EEA & FOEN 2016) for more detailed information (Fig. 5), e.g., about the meaning of the values of *WUP* and *DIS*.

2.1 Definition of built-up areas

Built-up areas "may include various types of settlement and buildings, ranging from places with urban character to villages to separate single buildings in the open landscape. Generally, a built-up area is defined as a surface covered by man-made structures. Roads and railways outside towns and cities are not included in this definition, since they are not perceived to be part of urban sprawl (but rather contribute to landscape fragmentation)" (EEA and FOEN, 2016, p. 47).

For the purpose of comparisons between different regions (or for one region between different points in time), the definition of the built-up areas must be chosen in a precise and consistent way. For smaller regions, usually there are more detailed datasets on 'built-up areas' available (e.g., data on the elements of urban

surface such as building footprints). However, for large areas, data on built-up areas do not usually include such details of the urban surface. It should be noted that for a meaningful comparison between different points in time, it is necessary to use the same delineation criteria of built-up area. Examples are given in Nazarnia et al. (2016).

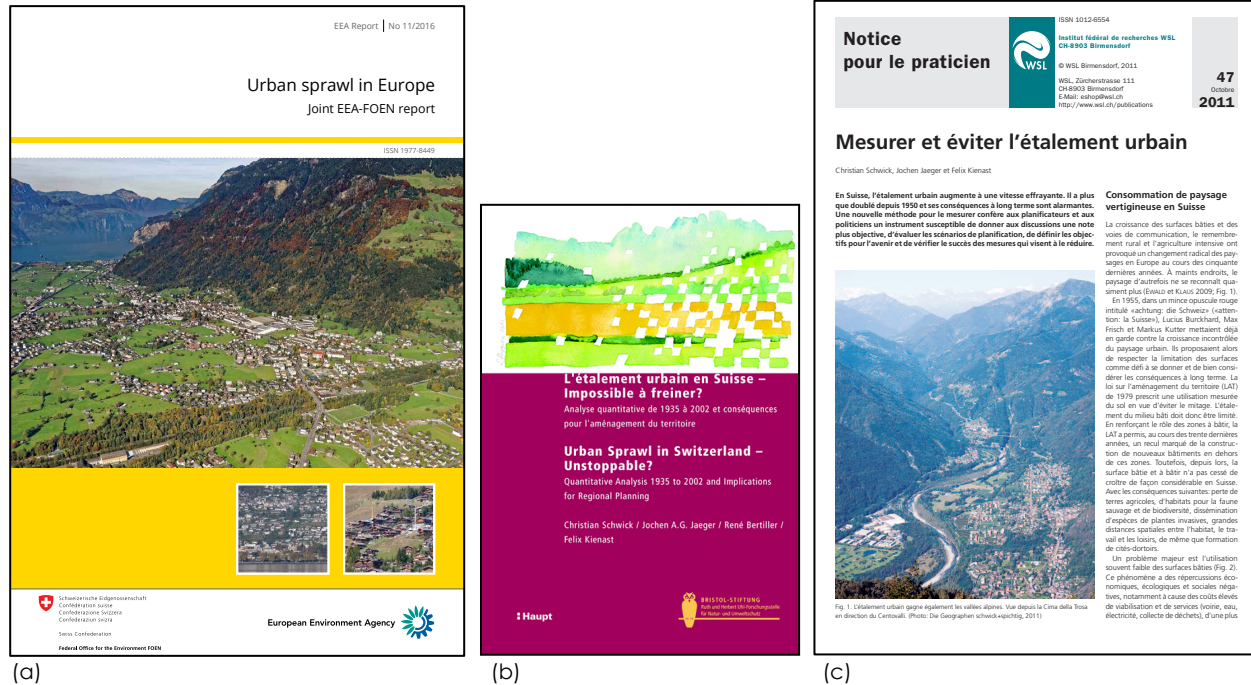


Fig. 5: Chapter 2 of the report "Urban sprawl in Europe" (EEA and FOEN 2016) is highly recommended reading before using the USM Toolset (a). A book about the WUP method and results for Switzerland is available in English and French (Schwick et al. 2012) and German (Schwick et al. 2010) (b). A Practitioner's Introduction to the WUP method is available in German (Schwick et al. 2011a) and French (Schwick et al. 2011b) as a PDF online at http://www.wsl.ch/info/fokus/zersiedelung/index_FR (c).

2.2 Metrics of urban sprawl

Weighted Urban Proliferation (*WUP*) has three components: *PBA*, *DIS* and *LUP* (or *UD*) (Fig. 2). In addition, the two metrics of *TS* and *UP* are defined here.

The proportion of built-up areas (*PBA*) is the proportion of the size of built-up areas to the size of the landscape (reporting unit): $PBA = \text{Area of built-up area} / \text{Area of reporting unit}$.

Degree of urban dispersion (*DIS*) measures the dispersion of built-up areas based on the distances between any two points within the built-up areas (Jaeger et al. 2010b). *DIS* is expressed in urban permeation units per square meter of built-up area (UPU/m²). The more dispersed the built-up areas, the larger the value of *DIS*. Therefore, more compact built-up areas have lower values of *DIS* than more dispersed built-up areas.

w₁(*DIS*) is a weighting function for *DIS* which assumes values between 0.5 and 1.5 to give higher weights to the more dispersed built-up areas and lower weights to less dispersed areas (Jaeger and Schwick 2014).

Total Sprawl (*TS*) is defined as the average sum of the weighted distances between all points in the urban area and randomly chosen second points where each second point is not farther away from the first point than the horizon of perception (*HP*). The value of *TS* is the product of *DIS* and the total amount of built-up area ($TS = DIS * \text{Area of built-up area}$). To learn more about *TS*, see Jaeger et al. (2010b).

Utilization Density (UD) measures the number of people living and working per km² of built-up area. The more people and jobs are located in a built-up area, the higher the land utilization as measured by utilization density (UD). This metric is expressed in inhabitants and jobs per square kilometer of built-up areas (inhabitants+jobs / km²).

w₂(UD) is a weighting function for UD which assumes values between 0 and 1 to give lower weights to more intensively utilized urban areas, i.e., those that have more inhabitants and jobs. The value of w₂(UD) is close to 1 when there are less than 40, and close to 0 when there are more than 100 inhabitants and jobs per hectare of built-up area (Jaeger and Schwick 2014).

Land Uptake per person (LUP) is the area of land that is used per inhabitant or job within the built-up areas and expressed in square meters per inhabitant or job (m²/(inh. or job)) ($LUP = \text{Area of built-up areas} / \text{Number of inhabitants and jobs}$). High LUP values indicate that more space is used per inhabitant or workplace compared to areas where LUP values are lower. LUP is in fact the reciprocal of UD: $LUP = 1/UD$.

Urban Permeation (UP) is a measure of the permeation of a landscape by built-up areas. It accounts for the DIS and PBA and is expressed in urban permeation units per m² of landscape (UPU/m^2): $UP = PBA \cdot DIS$.

Weighted Urban Proliferation (WUP) is the main metric used to quantify urban sprawl. It is the product of the Urban Permeation (UP), the weighting of DIS (w₁(DIS)) and the weighting of the UD (w₂(UD)). WUP is expressed in urban permeation units per square meter of landscape (UPU/m^2): $WUP = UP \cdot w_1(DIS) \cdot w_2(LUP)$. More detailed information about these metrics of urban sprawl can be found in Jaeger and Schwick (2014), and in Jaeger et al. (2010b, p. 431, Fig. 4) regarding the cross-boundary connections (CBC) procedure.

Weighted Urban Proliferation of the settleable part of the study area (WUP_b): Urban sprawl can be measured with and without the inclusion of those areas that are not suitable for the construction of buildings (called the "unsettleable" or "irreclaimable areas") of the study area. Examples of such types of areas considered as not feasible for the construction of buildings are glaciers and perpetual snow, watercourses, lakes and other water bodies, coastal lagoons, estuaries, inland marshes, and peat bogs. Areas in which the construction of buildings is not permitted, could also be excluded, e.g., protected areas in Switzerland. Excluding the areas not suitable for construction from the reporting units results in larger WUP values. WUP_b can be calculated as

$$WUP_b = (A_{\text{reporting unit}} / A_{\text{settleable}}) \cdot (PBA \cdot DIS) \cdot w_1(DIS) \cdot w_2(LUP) = (A_{\text{reporting unit}} / A_{\text{settleable}}) \cdot WUP.$$

WUP_b is expressed in urban permeation units per square meter of landscape (UPU/m^2). More detailed information can be found in Hennig et al. (2015: 492-494).

Weighted Sprawl per Capita (WSPC) measures the contribution of each inhabitant or job to urban sprawl in the reporting unit and is expressed in urban permeation units per inhabitant or job ($UPU / (\text{inh. or job})$): $WSPC = (\text{Area of reporting unit} / \text{Number of inhabitants and jobs}) \cdot WUP$ (Behnisch et al., 2022; Pourtaherian & Jaeger, 2022).

While Shannon's entropy has been widely used for measuring urban sprawl in earlier studies, Nazarnia et al. (2019) proved that it is not a suitable method for the assessment of urban sprawl since it does not comply with the 13 suitability criteria introduced by Jaeger et al. (2010b). The number of studies using the WUP method and the USM toolset for the measurement and analysis of urban sprawl has increased since. Pourtaherian and Jaeger (2022) used this method to analyze the degree to which greenbelts are effective at mitigating urban sprawl, and Behnisch et al. (2022) measured urban sprawl globally to reveal trends in urban sprawl since 1990.

Tab. 1: Metrics for the measurement of urban sprawl and their associated equations and units

Acronym	Name of the metric	Equation	Unit	Mathematical homogeneity
<i>WUP</i>	Weighted Urban Proliferation	$(PBA \cdot DIS) \cdot w_1(DIS) \cdot w_2(LUP)$	UPU per m ² of landscape	Intensive
<i>WUP_b</i>	Weighted Urban Proliferation for the settleable part of the study area	$(A_{\text{reporting unit}} / A_{\text{settleable}}) \cdot (PBA \cdot DIS) \cdot w_1(DIS) \cdot w_2(LUP) = (A_{\text{reporting unit}} / A_{\text{settleable}}) \cdot WUP$	UPU per m ² of landscape	Intensive
<i>PBA</i>	Percentage of Built-up Area	$A_{\text{built-up}} / A_{\text{reporting unit}}$	%	Intensive
<i>DIS</i>	Dispersion	–	UPU per m ² of built-up area	Intensive
<i>LUP</i>	Land Uptake per Person (per inhabitant or job)	$A_{\text{built-up}} / N_{\text{inh+job}}$	m ² per inhabitant or job	Intensive
<i>UD</i>	Utilization Density	$N_{\text{inh+job}} / A_{\text{built-up}}$	Inhabitants or jobs per km ² of built-up area	Intensive
<i>UP</i>	Urban Permeation	$PBA \cdot DIS$	UPU per m ² of landscape	Intensive
<i>TS</i>	Total Sprawl	$DIS \cdot A_{\text{built-up}}$	MUPU	Extensive
<i>WTS</i>	Weighted Total Sprawl	$w_1(DIS) \cdot w_2(LUP) \cdot TS$	MUPU	Extensive
<i>SPC</i>	Sprawl per Capita	$TS / N_{\text{inh+job}}$	UPU per inhabitant or job	Intensive
<i>WSPC</i>	Weighted Sprawl per Capita	$w_1(DIS) \cdot w_2(LUP) \cdot SPC = (A_{\text{reporting unit}} / N_{\text{inh+job}}) \cdot WUP = WTS / N_{\text{inh+job}}$	UPU per inhabitant or job	Intensive

2.3 Choice of the Horizon of Perception

Calculation of the dispersion of built-up areas (*DIS*) and Weighted Urban proliferation (*WUP*) requires a defined scale of analysis, which is specified by the Horizon of Perception (*HP*). The user can choose the size of the *HP* between 0.2 and 10 km. However, the default value of *HP* in the USM Toolset is 2 km, and the weighting function for the computation of weighted Dispersion ($w_1(DIS)$) operates properly only when 2 km is selected. The reason is that the weighting of *DIS* as a component of *WUP* was chosen for this scale of analysis of urban sprawl based on expert opinion (see Jaeger and Schwick 2014 for details). If users are interested in using a different value of *HP* they may need to consider modifying the weighting function equation accordingly in the *sivalues.exe* tool (see section 3.1). However, working on the logic of suitable weighting functions for *HPs* other than 2 km should be done in a cautious way and this remains future work.

2.4 Job data full-time equivalents

When it is possible to distinguish between part-time and full-time jobs, converting part-time jobs into full-time equivalents would lead to more accurate urban sprawl metrics results. This can be done using the average number of weekly hours worked for each type of employment in a given country. By calculating a conversion factor based on this data, part-time jobs can be converted into full-time equivalents, which can then be added to the number of full-time jobs to obtain the total number. In cases where part-time and full-time jobs are not provided separately, it may still be possible to estimate them using the percentage of part-time employment as a percentage of total employment, as seen in App. D in Pourtaherian and Jaeger (2022) (Fig. 6).

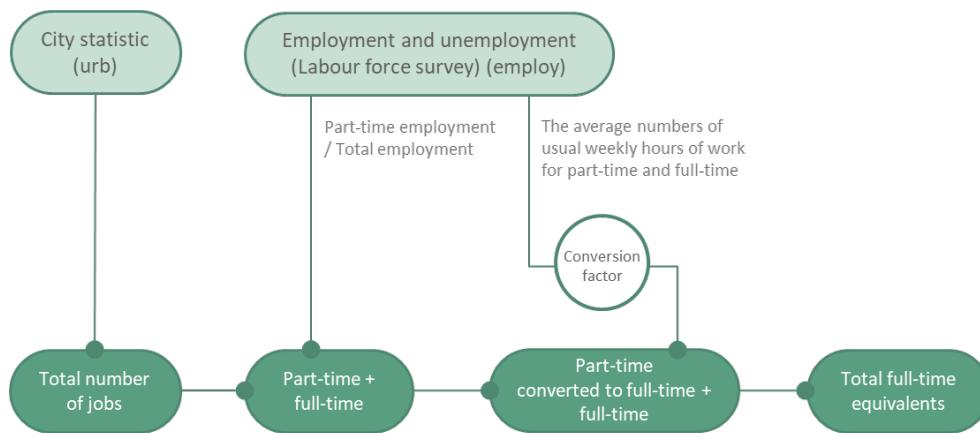


Fig. 6: Job data preparation in the case that part-time and full-time jobs can be distinguished: An example of a data source (urb and employ are European databases European Commission, Eurostat open source datasets).

2.5 City boundaries adjustment for comparison of cities of differing sizes (optional)

Because *WUP* is an intensive metric, it can be applied to, and compared between, landscapes irrespective of their sizes. However, in some cases (e.g., Uppsala), the boundary of the city is located far from the built-up areas, whereas in other cases (e.g., Glasgow), the boundary runs closely along the built-up areas. Such differences convolute a fair comparison of the cities, because even when the population sizes and the amounts and spatial arrangements of the built-up areas of two cities are the same, the *PBA* of the two cities differs. In such a situation in which the sizes and patterns of built-up areas are similar in two cities, but their boundaries and area sizes differ, the value of *WUP* will be lower for the landscape of the city whose

boundary is located farther away as a result of its lower *PBA*. Therefore, the boundaries can be rescaled to make the cities comparable on an equal footing. In contrast, *WSPC* relates to the number of inhabitants and jobs rather than the landscape and is not affected by changes in the boundaries.

For this purpose, Pourtaherian and Jaeger (2022) used the relationship between population size and the city size (log-transformed) by applying a linear regression to determine average city size as a function of population size, which they called “adjusted city size” (Fig. 7). In the cases in which the adjusted city size was greater than the original area, this step corresponds to adding some empty space with no built-up areas and no population in it. Hence, the only component adjusted is *PBA*, while *DIS* and *LUP* remain the same. The adjusted city size was larger than the size of the built-up areas in all 60 European cities they studied. Consequently, none of the cities for which the area shrank due to the adjustment lost any built-up areas, i.e., its boundaries were simply drawn somewhat closer around the built-up areas, and population stayed the same as well. The corresponding values of the metrics are referred to as adjusted *PBA* and adjusted *WUP*. This adjustment is an interesting option for the comparison of cities.

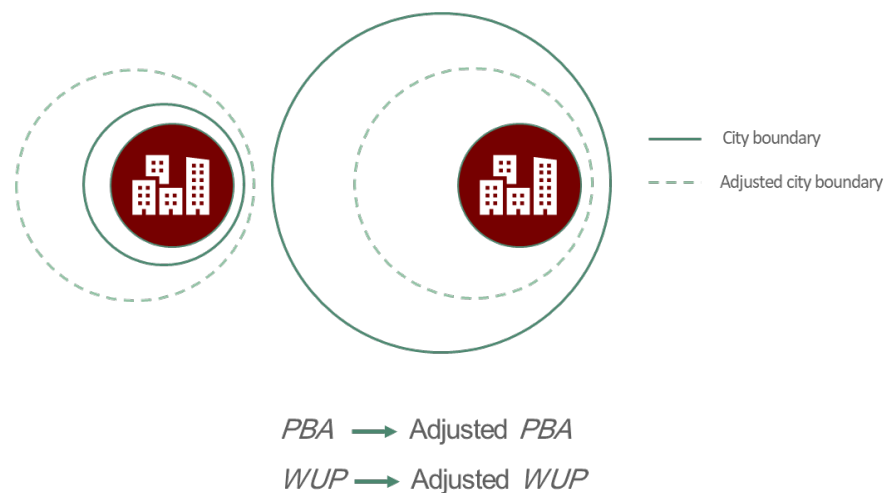


Fig. 7: Illustration of city size adjustment. In case that the population size of the two cities is the same, their adjusted city size will be the same.

3. Installation of the Urban Sprawl Metrics (USM) Toolset

The Urban Sprawl Metrics Toolset works with QGIS. No license is required for the installation of this Toolset. Minimum requirements for the system (PC/laptop) on which the Toolset will be installed are:

- (1) 4 GB or more Random Access Memory (RAM),
- (2) 10 GB or more free space on the disc where the data files are stored,
- (3) 10 GB or more free space on the disc where working directories (see section 4 for explanation on working directories) will be stored.

3.1 Urban Sprawl Metrics Toolset archive

The USM Toolset is distributed as a “zip” archive called “usm_calculator-main.zip”. The toolset can be downloaded from https://gitlab.com/geometalab/usm_toolset/usm_calculator/-/archive/main/usm_calculator-main.zip or Concordia Spectrum.

3.2 Step by step installation guide

The installation of the USM Toolset can be done with the plugin manager.

Step 1: Download the “usm_calculator-main.zip” archive from https://gitlab.com/geometalab/usm_toolset/usm_calculator/-/archive/main/usm_calculator-main.zip.

Step 2: Open the QGIS window.

Step 3: Click on the “Plugins” option in the Toolbar and from there open “Manage and install plugins...” (Fig. 8).

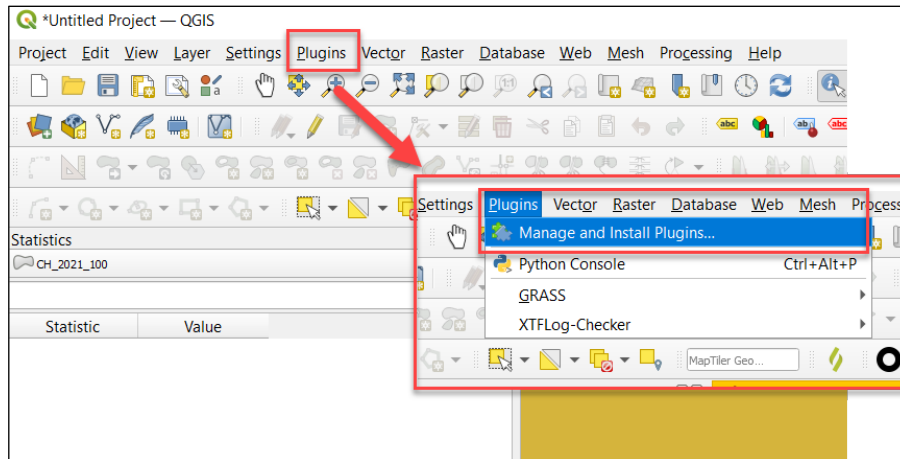


Fig. 8: Manage and install plugins in QGIS.

Step 4: Use the option “Install from ZIP” and use the previously downloaded zip File (Fig. 9).

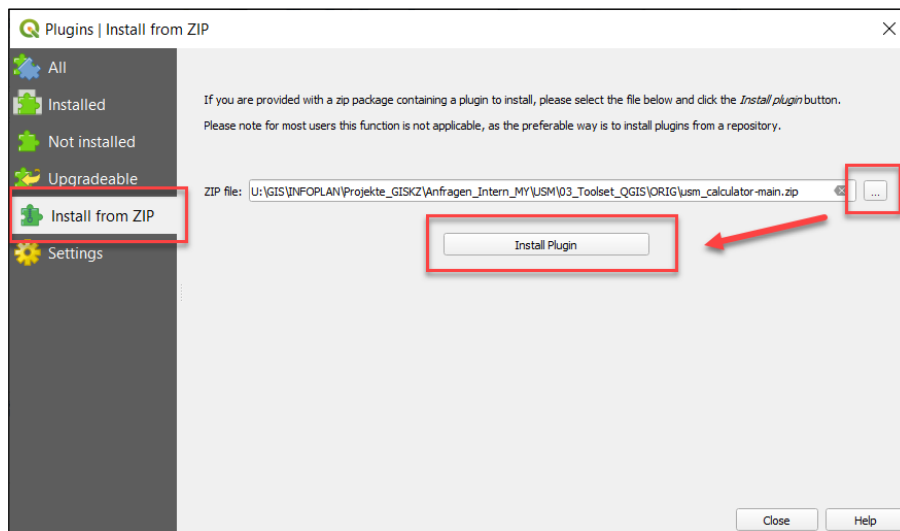


Fig. 9: Plugins-Install plugin from ZIP.

Step 5: The set of processing algorithms should now appear in the processing toolbox (Fig. 10).

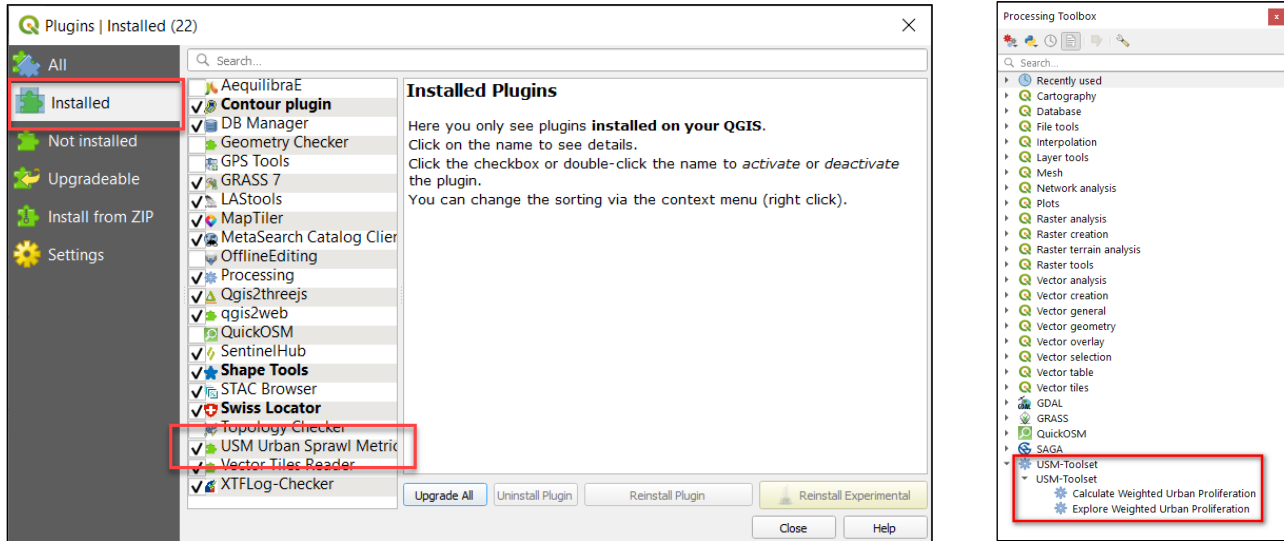


Fig. 10: (a) Installed plugins, (b) Processing toolbox.

For more information regarding the operating instructions, please refer to the [README file on GitLab](#).

4. How to use the Urban Sprawl Metrics Toolset

In the following sections, a step-by-step guide to use the USM Toolset is described. Users should consider preparing their input data and working directories before using the USM Toolset. Users need to have two working folders: (1) a 'Directory' folder and (2) an 'Output' folder. In the directory folder users should store their input data. The two components of the directory folder should be (1) the binary map of built-up areas³, and (2) feature class or Shapefile of the reporting unit(s)/area of study. Users should keep the Output folder empty because the outputs of the calculations will be sorted in this folder automatically. The default *HP* of the USM Toolset is 2 km and the calculation of metrics of urban sprawl is based on weighting functions that are appropriate for a horizon of perception of 2 km.

4.1. Calculate Weighted Urban Proliferation tool

The purpose of this tool is to calculate the suite of metrics of urban sprawl (e.g., *DIS*, *UP*, *UD*, *WUP*). The input data for the Metrics calculation tool are:

- (1) the binary map of built-up areas in raster format (0 values for non-built-up areas and 1 value for built-up areas), and
- (2) the feature class or the shapefile of the reporting unit(s) which includes two fields in its attribute table: reporting unit(s) identifier and number of inhabitants and jobs.

The output of the tool is a feature class within a GeoPackage (similar to the shapefile of the reporting unit(s)) that includes all the values of the urban sprawl metrics in its attribute table (see examples in section 5). The file of the reporting unit and the SI-raster will be stored in the output directory as well.

³ If the data about built-up areas is in vector format, in order to convert the data to raster binary format, users should first convert the feature class or Shapefile to a raster. The second step is to reclassify the output raster file to a binary file.

4.1.1 How to use the Calculate Weighted Urban Proliferation tool

1. From Processing Toolbox, select USM Toolset and click on the first tool (Calculate Weighted Urban Proliferation) (Fig. 11).
2. From the 'Built-up area (Raster)' bar skip to the directory folder, select the binary map of built-up areas, and click on the 'Open' button.
3. From the 'Reporting unit (Vector)' bar, skip to the directory folder, select the shapefile of reporting unit, and click on the 'Open' button.
4. From the 'Identifier' drop down menu, select the field in which the ids of the reporting unit(s) is/are stored (identifier can be numeric or string).
5. From the 'Inhabitants' drop-down menu, select the field in which the number(s) of inhabitants is/are stored for the reporting unit(s).
6. Similarly, from the 'Employees' drop-down menu, select the field in which the number(s) of employees is/are stored for the reporting unit(s) if the data is available.
Note: When the data of inhabitants and jobs are combined in a single field (as in the examples in section 5), user should include this field in the 'Inhabitants' bar.
7. If applicable, choose the settleable portion of the study area from the 'Share of settleable area' option.
8. To tailor to specific requirements, choose either the 'Directory' or 'Temporary Directory' option from the 'Output folder' bar.

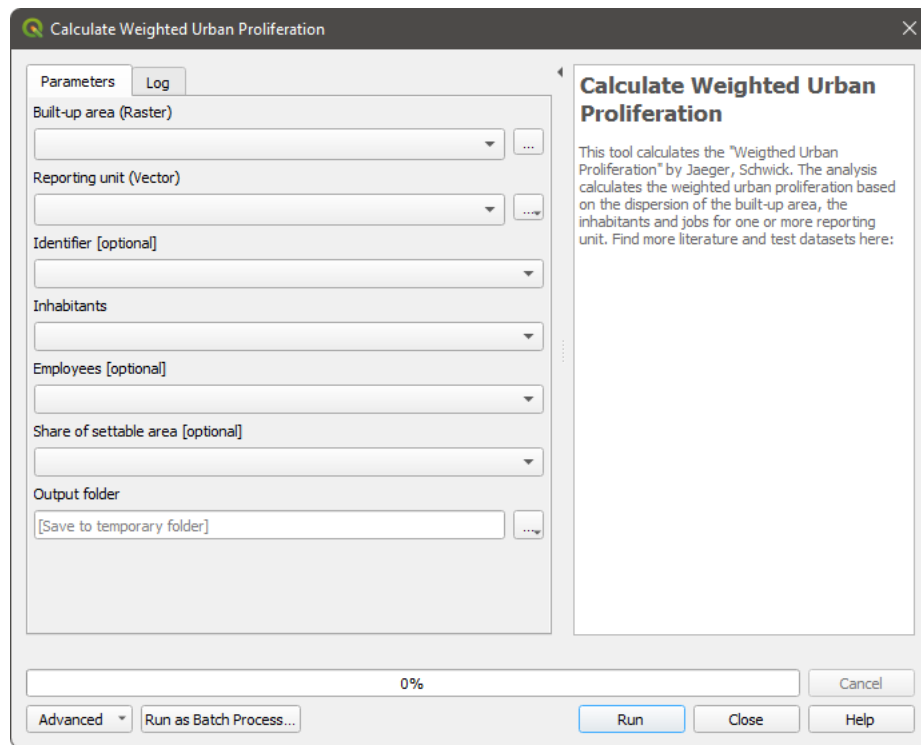


Fig. 11: Calculate Weighted Urban Proliferation tool.

4.2 Recalculation (Explore Weighted urban Proliferation) tool

The Explore Weighted Urban Proliferation Tool allows users to recalculate *WUP* in different scenarios. After initially calculating *WUP* using the first tool, users can swiftly modify attribute table values and recalculate *WUP*. This allows for rapid generation of new datasets, as *DIS* is read directly from the attribute table without requiring recalculation (within 2 km).

4.2.1 How to use the Recalculation (Explore Weighted Urban Proliferation) tool

"Explore WUP" allows users to recalculate, and to some degree "explore", WUP in a fast way for situations in which DIS is not changing, i.e., the built-up area is not changed. It can be applied to explore the effects of densification or reductions in density: What happens if the number of inhabitants and jobs increases or decreases in an area, in which the built-up area is not changing. (If the built-up area changes, DIS will need to be recalculated, which will take more time.)

1. Modify the attribute table of the output obtained from the initial tool.
2. Access the Processing Toolbox and choose the USM Toolset. Locate and select the second tool (Explore Weighted Urban Proliferation) (Fig. 12).
3. In the 'Inputlayer (Vector or Table)' section, navigate to the folder where you have saved the modified shapefile or table. Select the file and click the 'Open' button.
4. In the 'Urban dispersion (DIS)' section, retrieve the dispersion value.
5. In the 'Settlement area' drop-down menu, choose the 'settlement_area' field that contains the recorded area of built-up areas.
6. Recalculate WUP by following steps 5 to 8 from the previous section.

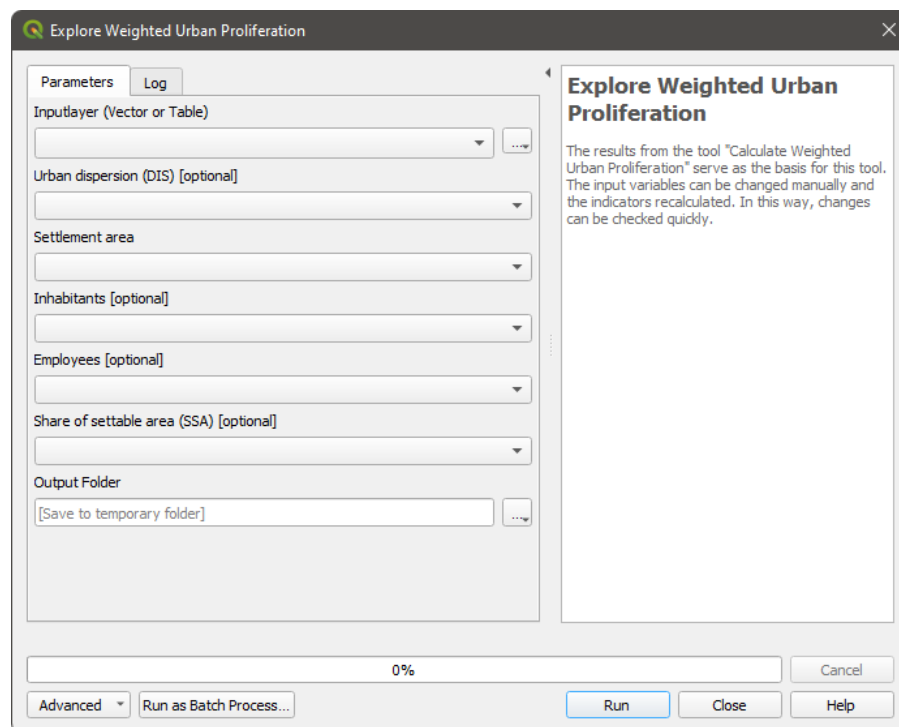


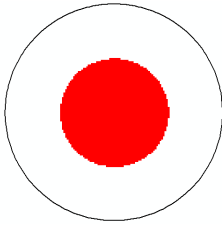
Fig. 12: Explore Weighted Urban Proliferation Tool

5. Examples of using the USM Toolset

In this section, you find six simple model and seven real landscapes and the results of applying the USM Toolset to these landscapes. The files of all examples are available with this tool (on Concordia University's Spectrum website) for users to practice. For each example, users should create two folders: (1) a directory folder (e.g., Directory_ex1) and (2) an Output folder (e.g., Output_ex1). Copy and paste the relevant raster file and shapefile of each example (e.g., example 1) into the directory folder. Then follow the steps described in section 4.

5.1 Six simple hypothetical model landscapes

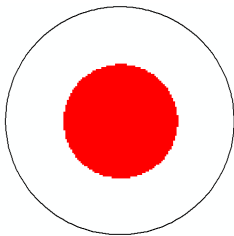
Example 1: Area of built-up areas = 785,000 m² (circle with a radius of 500 m), Area of the reporting unit = 3.14 km², Number of inhabitants and jobs = 2,600 people and jobs.



Field	Value
Id	0
inhbjob	2600
RU_id	1
DIS	28.130739449231818
settlement_area	785700
WDIS	0.5092631011135808
LUP	302.1923076923077
PBA	0.25012917131577045
UP	7.036318546936207
UD	3309.1510754741
WUD	0.8937922939415252
TS	22102321.98526144
WUP_a	3.202759357962054
WUP_b	NULL
WSPC	3869.3977046917307

The value of Weighted Urban Proliferation for a landscape of size 3.14 km² and with 785,000 m² of built-up areas and 2,600 inhabitants and jobs is 3.2 UPU/m². The value of WSPC is 3869.4 UPU/(inhb. or job). Increasing the number of inhabitants and jobs for the same theoretic landscape will decrease the WUP value. See the next example for details.

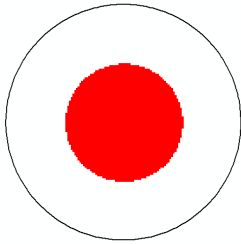
Example 2: Area of the built-up areas = 785,000 m² (circle with a radius of 500 m), Area of the reporting unit = 3.14 km², Number of inhabitants and jobs = 12,000 people and jobs.



Field	Value
Id	0
inhbjob	12000
RU_id	1
DIS	28.130739449231818
settlement_area	785700
WDIS	0.5092631011135808
LUP	65.475
PBA	0.25012917131577045
UP	7.036318546936207
UD	15273.004963726615
WUD	0.00545766747253473
TS	22102321.98526144
WUP_a	0.019556663990939818
WUP_b	NULL
WSPC	5.119245260642863

The only difference between the theoretic landscape shown in this example and example 1 is the number of inhabitants and jobs (12,000 versus 2,600 people and jobs). In this example, the higher number of inhabitants and jobs resulted in a higher value of Utilization Density, and therefore, in a lower value of WUP (0.02 UPU/m²). The value of WSPC is 5.12 UPU/(inhb. or job).

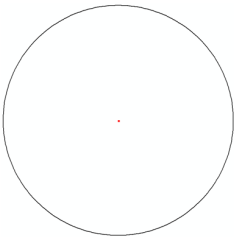
Example 3: Area of built-up areas = 785,000 m² (circle with a radius of 500 m), Area of the reporting unit = 3.14 km², Number of inhabitants and jobs = 0 people and jobs.



Field Name	Value
Id	0
inhbjob	0
RU_id	1
DIS	28.130739449231818
settlement_area	785700
WDIS	0.5092631011135808
LUP	-1
PBA	0.25012917131577045
UP	7.036318546936207
UD	0
WUD	0.9846171555600075
TS	22102321.98526144
WUP_a	3.528215481779602
WUP_b	NULL
WSPC	NULL

In this example, the number of inhabitants and jobs is zero and therefore the value of *UD* is zero indicating that the built-up area is not utilized at all. The value of -1 for *LUP* indicates an undefined value, because *LUP* is the result of a division of the area of built-up areas by the number of inhabitants, which is infinity when there are no inhabitants and no jobs. The value of *WSPC* also is infinity.

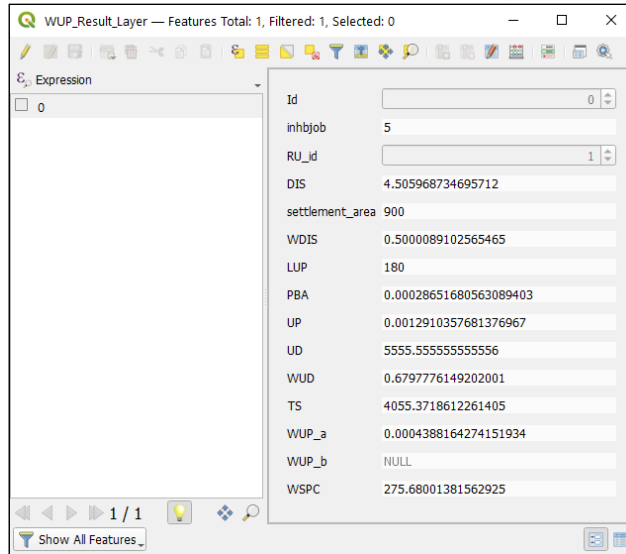
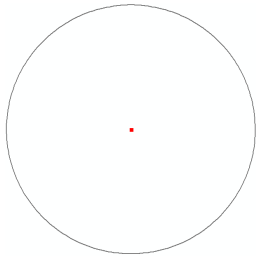
Example 4: Area of built-up areas = 225 m² (1 pixel size of 15 m x 15 m), Area of reporting unit = 3.14 km², Number of inhabitants and jobs = 2 people and jobs.



Field Name	Value
Id	0
inhbjob	2
RU_id	1
DIS	2.961048057335979
settlement_area	225
WDIS	0.5000056538244261
LUP	112.5
PBA	7.162920140772351e-05
UP	0.00021209750767686727
UD	8888.888888888889
WUD	0.21568359854292682
TS	666.2358129005953
WUP_a	2.28732354884568e-05
WUP_b	NULL
WSPC	35.92444061750949

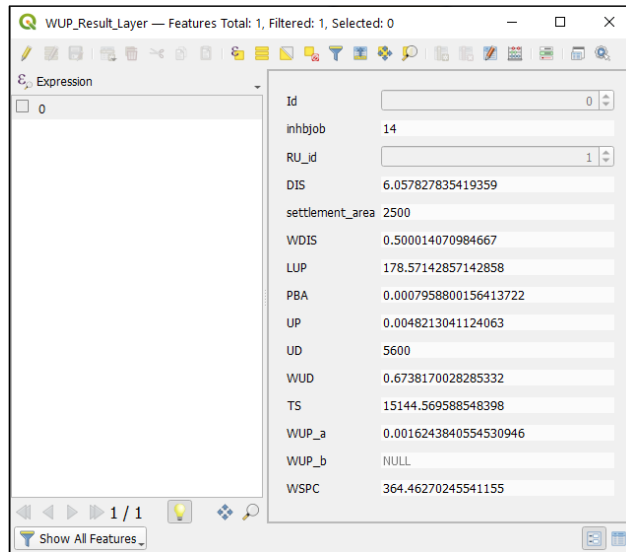
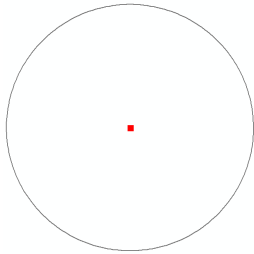
The smallest possible built-up area at any given resolution is one pixel. This will result in very low values of *DIS* and *WUP*. The example shown here is for a pixel size of 15 m x 15 m. The value of *WSPC* is 35.92 UPU/(inhb. or job).

Example 5: Area of built-up areas = 900 m² (1 pixel size of 30 m x 30 m), Area of reporting unit = 3.14 km², Number of inhabitants and jobs = 5 people and jobs.



Increasing the size of the built-up area results in a higher value of *UP* and *DIS* and accordingly, in a higher value of sprawl (0.00044 UPU/m² in this example compared to 0.00002 UPU/m² in example 4). The value of *WSPC* is 275.68 UPU/(inhb. or job).

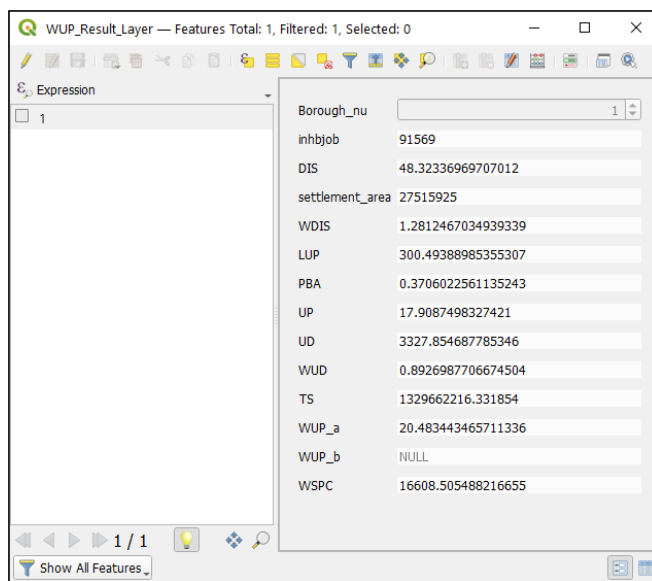
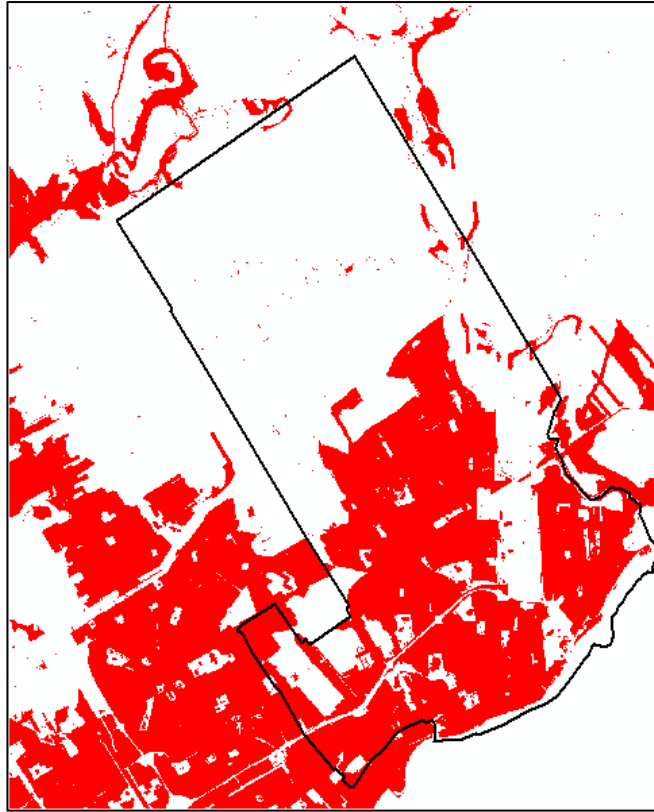
Example 6: Area of built-up areas = 2,500 m² (1 pixel size of 50 m x 50 m), Area of reporting unit = 3.14 km², Number of inhabitants and jobs = 14 people and jobs.



Similar to example 5, this example shows that a higher amount of built-up areas results in higher degree of urban sprawl. In this example, the number of inhabitants and jobs was selected proportional to the size of the built-up area to be comparable to example 5 (*LUP* values in the two examples are very close). The value of *WSPC* is 364.46 UPU/(inhb. or job).

5.2 One example of an urban landscape from Canada

Example 7: Area of built-up areas = 27,506,925 m² (in 2011), Area of reporting unit = 74 km² (borough of Beauport in Quebec City, Quebec, Canada, 2011), Number of inhabitants and jobs = 91,569 people and jobs; pixel size is 15 m x 15 m (see detailed information in Nazarnia et al. 2016).



Beauport is a northeastern suburb of Quebec City and is one of the oldest European-founded communities in Canada. Between highly sprawled boroughs of Quebec City, the borough of Beauport is the third-least sprawled area with *WUP* value of 20.48 UPU/m² and *WSPC* value of 16,608.5 UPU/(inhb. or job).

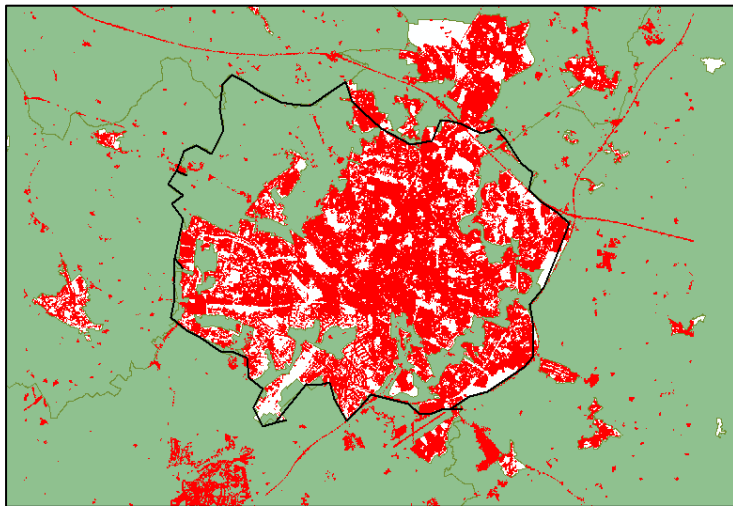
5.3 Six European cities with and without greenbelts

The examples presented below are taken from the research conducted by Pourtaherian and Jaeger (2022). These examples show the impact of greenbelts on urban sprawl, as measured by the USM toolset. The study evaluates 60 European cities with and without greenbelts to understand the extent of urban sprawl and the effectiveness of greenbelts at mitigating it. For more detailed information on the study and its findings, readers are encouraged to refer to Pourtaherian and Jaeger's research paper and appendices.

Please note the following important points regarding the examples in this section:

1. The tool currently does not support ArcGIS native raster formats like OVR. However, you can use all raster formats with the appropriate coordinate system and export them as GeoTIFF to perform calculations seamlessly.
2. In some cases, the USM toolset may fail to execute due to inconsistencies in the geometry of reporting unit shapefiles, such as overlapping lines. To resolve this, you can utilize the "fix geometry" tool in QGIS.
3. The examples provided in this section have already been modified and are compatible with the toolset. However, if you are using the examples that accompany the USM toolset for ArcMap (Nazarnia et al. 2023), please be aware that those raster files are in OVR format, and the reporting units are the original shapefiles downloaded from Eurostat without any geometry modifications. When using those examples, you would first need to make the required corrections yourself.

Example 8, Coventry: Area of built-up areas = 48 km² (in 2015), Area of reporting unit = 99 km² (City of Coventry), Number of inhabitants and jobs = 475,614 people and jobs; pixel size is 20 m x 20 m.

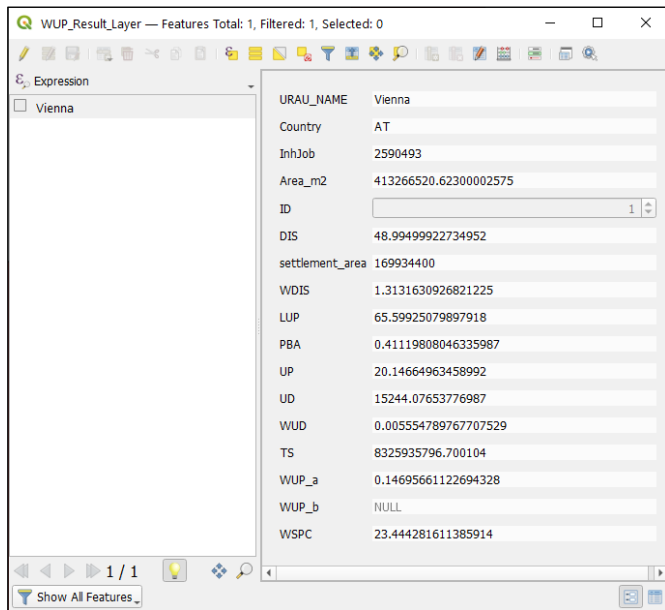
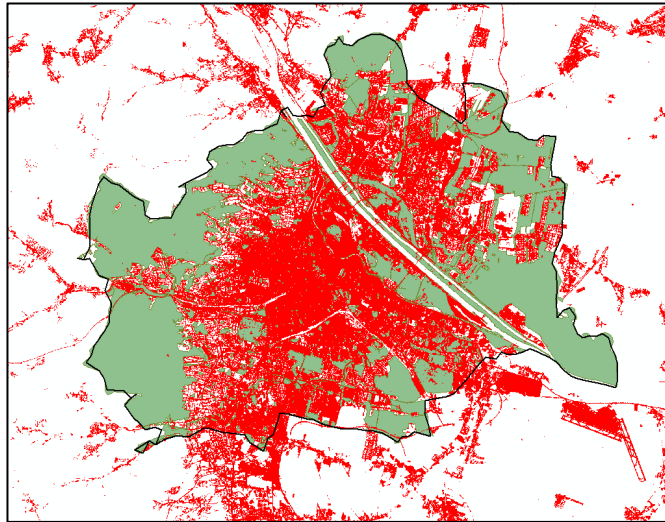


Attribute	Value
URAU_NAME	Coventry
Country	UK
InhJob	475614
Area_m2	98740617.45520001650
ID	1
DIS	48.78017105497863
settlement_area	48382800
WDIS	1.3033623755181396
LUP	101.72703074341798
PBA	0.4899989613892255
UP	23.90223315332829
UD	9830.22892432848
WUD	0.13375487266460462
TS	2360121260.11882
WUP_a	4.1669018469070505
WUP_b	NULL
WSPC	865.0764301282037

The greenbelt of Coventry is part of the West Midlands greenbelt and has been in place since 1982. In 2001, three small areas were detached from the greenbelt to accommodate population growth, but the overall extent of the greenbelt has remained untouched since then and accommodating housing needs while keeping the greenbelt area intact has been effective in controlling urban sprawl.

$WUP = 4.17 \text{ UPU/m}^2$; $WSPC = 865.08 \text{ UPU}/(\text{inhb. or job})$

Example 9, Vienna: Area of built-up areas = 170 km² (in 2015), Area of reporting unit = 413 km² (City of Vienna), Number of inhabitants and jobs = 2,590,493 people and jobs; pixel size is 20 m x 20 m.



In 1995, the Vienna Greenbelt Masterplan was officially adopted, marking a pivotal moment in the city's efforts to expand green space. The city took decisive steps towards achieving this goal, and today, over 50% of the city's area is covered by greenery. As a result of this initiative, Vienna has a very low *WUP* value, making it a model of sustainable urban development.

$WUP = 0.15 \text{ UPU/m}^2$; $WSPC = 23.44 \text{ UPU}/(\text{inhb. or job})$

Example 10, Munster: Area of built-up areas = 58 km² (in 2015), Area of reporting unit = 304 km² (City of Munster), Number of inhabitants and jobs = 430,844 people and jobs; pixel size is 20 m x 20 m.

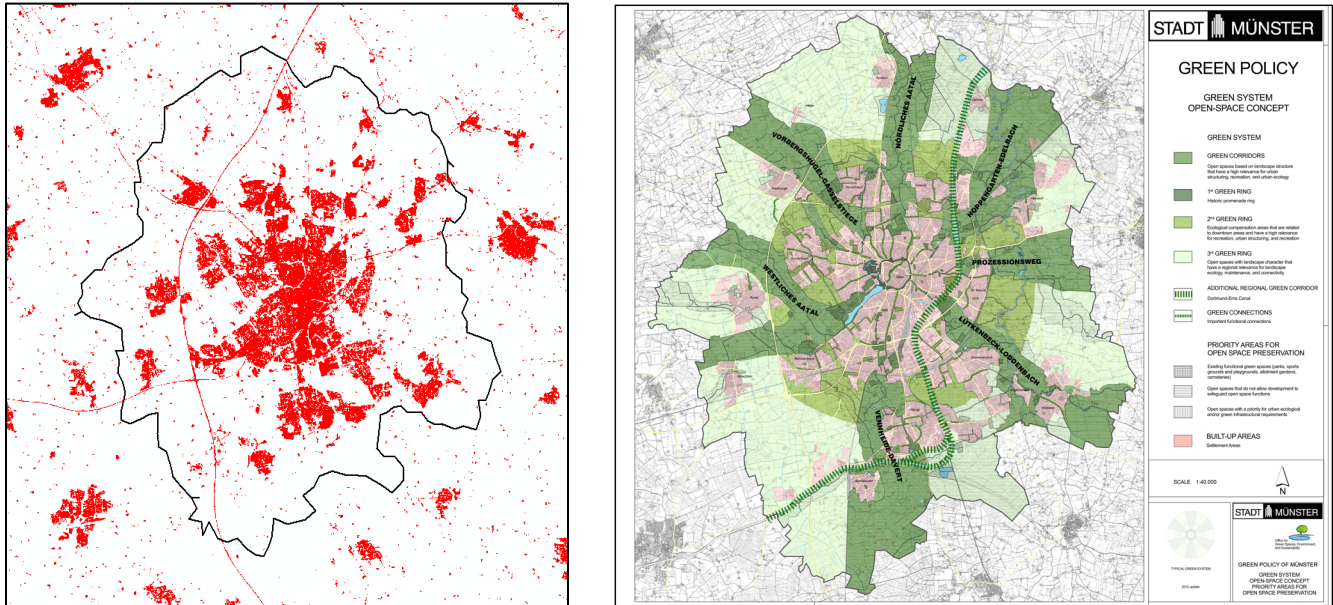


Fig. 13: Map of the “Green Policy Munster” (“Grünordnung Münster”). Source: Stadt Münster, n.d.; translated from German by Pourtaherian and Jaeger (2022).

WUP_Result_Layer — Features Total: 1, Filtered: 1, Selected: 0

Expression

Munster

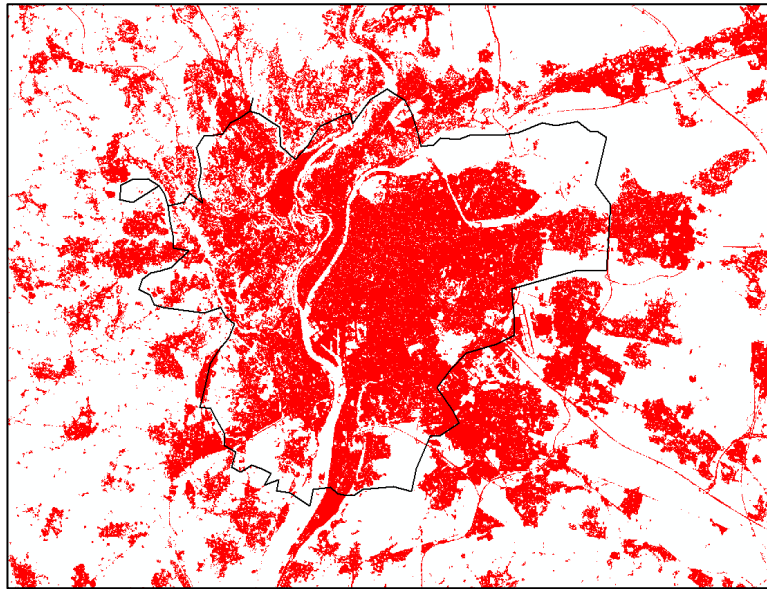
URAU_NAME	Munster
Country	DE
InhJob	430844
Area_m2	303678353.61799997091
ID	1
DIS	47.21787964002896
settlement_area	57992400
WDIS	1.2206030173432114
LUP	134.60185125010446
PBA	0.19096652530276595
UP	9.017034407020548
UD	7429.318324470102
WUD	0.40224952458640095
TS	2738278163.2364154
WUP_a	4.427246523032923
WUP_b	NULL
WSPC	3120.523751458698

Show All Features

Munster has a Green Policy consisting of three green rings and seven green corridors that act as a greenbelt for the city (Fig. 13). The Green Policy protects open spaces, leading to more compact forms of urban development and limiting urban sprawl.

$$WUP = 4.43 \text{ UPU/m}^2; WSPC = 3,120.52 \text{ UPU}/(\text{inhb. or job})$$

Example 11, Lyon: Area of built-up areas = 134 km² (in 2015), Area of reporting unit = 220 km² (City of Lyon), Number of inhabitants and jobs = 1,546,701 people and jobs; pixel size is 20 m x 20 m. Lyon does not have a greenbelt.



WUP_Result_Layer — Features Total: 1, Filtered: 1, Selected: 0

Expression

☐ Lyon

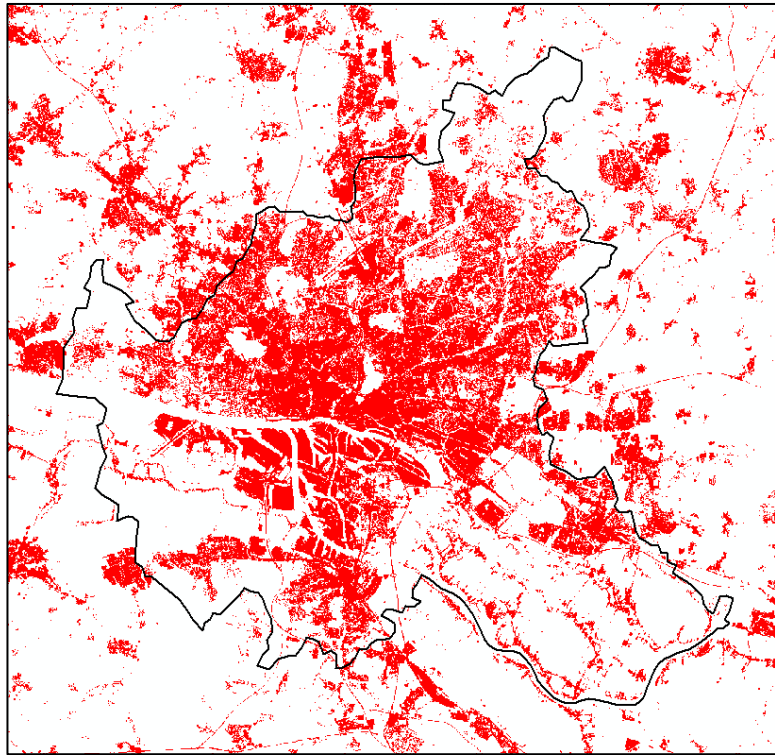
URAU_NAME	Lyon
Country	FR
InhJob	1546701
Area_m2	219778031.95100000501
ID	1
DIS	49.16128639379297
settlement_area	133645600
WDIS	1.3204878009209167
LUP	86.40687501980021
PBA	0.6080935333415155
UP	29.894660346815737
UD	11573.153175263533
WUD	0.05036460160374694
TS	6570189616.870297
WUP_a	1.9881695581470047
WUP_b	NULL
WSPC	282.5083792372754

1 / 1

Show All Features

$WUP = 1.99 \text{ UPU/m}^2$; $WSPC = 282.51 \text{ UPU/(inhb. or job)}$

Example 12, Hamburg: Area of built-up areas = 283 km² (in 2015), Area of reporting unit = 747 km² (City of Hamburg), Number of inhabitants and jobs = 2,561,708 people and jobs; pixel size is 20 m x 20 m. Hamburg does not have a greenbelt.



WUP_Result_Layer — Features Total: 1, Filtered: 1, Selected: 0

Expression

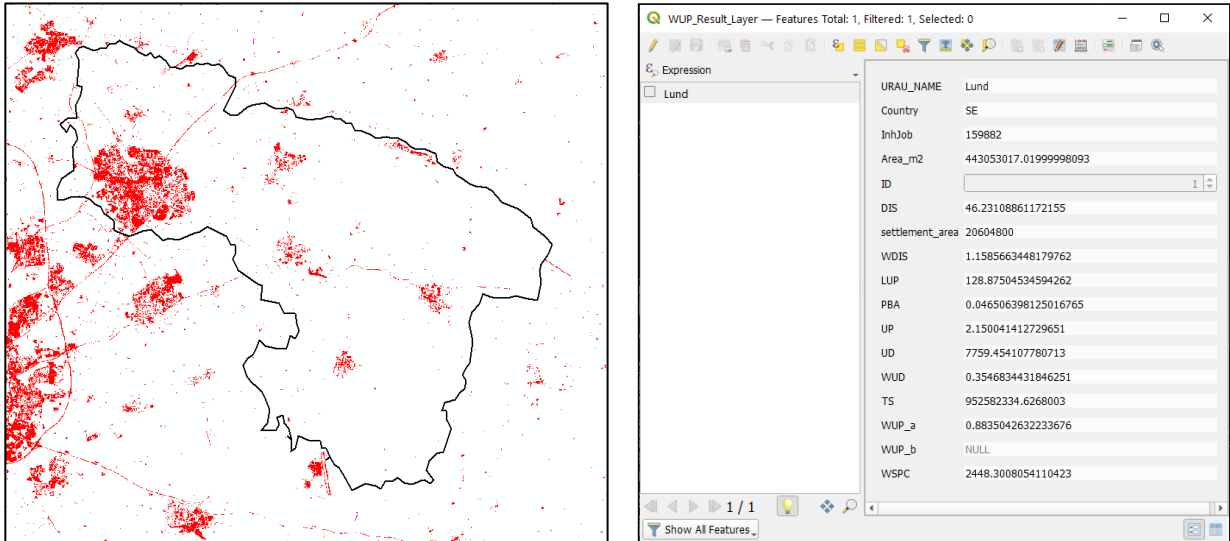
Hamburg

URAU_NAME	Hamburg
Country	DE
InhJob	2561708
Area_m2	747130046.35099983215
ID	1
DIS	48.71605310820936
settlement_area	283387200
WDIS	1.3003630465671354
LUP	110.6243178379425
PBA	0.37930103518661906
UP	18.47804937415012
UD	9039.60376474308
WUD	0.2004623686361603
TS	13805505885.386747
WUP_a	4.816744389142238
WUP_b	NULL
WSPC	1404.8183706813013

Show All Features

$WUP = 4.82 \text{ UPU/m}^2$; $WSPC = 1,404.82 \text{ UPU}/(\text{inhb. or job})$

Example 13, Lund: Area of built-up areas = 21 km² (in 2015), Area of reporting unit = 443 km² (City of Lund), Number of inhabitants and jobs = 159,882 people and jobs; pixel size is 20 m x 20 m. Lund does not have a greenbelt.



$WUP = 0.88 \text{ UPU/m}^2$; $WSPC = 2,448.3 \text{ UPU}/(\text{inhb. or job})$

Comparing a sample of 30 cities with greenbelt with 30 cities without greenbelt, Poutaherian and Jaeger (2022) revealed that greenbelts were highly effective in mitigating urban sprawl. The proportion of cities in which sprawl decreased was significantly higher in the group of cities with greenbelts, with 90% of these cities experiencing a decrease, more than twice the proportion of cities without greenbelts. While some cities without greenbelts also saw a decrease in urban sprawl, the average relative decrease was much stronger in cities with greenbelts.

It is worth noting that the examples included in this User Manual do not capture the aforementioned difference between cities with and without greenbelts, since (a) a single point in time is presented here, and (b) only a few examples are provided that are not representative of cities with and without greenbelts more broadly.

We wish you good success with your own urban sprawl analysis!

Acknowledgements

We thank Michael Wenzlaff and Beat Trachsler for their generous programming support. Michael Wenzlaff programmed the original URSMEC tool (that was used and explained in Jaeger et al. 2008). We also cordially thank Dr. Zachary Patterson for his help with job data and Dr. Pierre Gauthier for his great help in the selection of the examples of densification in Canada. We thank the Swiss Federal Office for the Environment (FOEN, contract no. 06.0111.PZ/M132-2143) and the European Environment Agency (EEA) for their financial support for our project "Urban sprawl in Europe" (Hennig et al. 2015; EEA & FOEN 2016). The development of the QGIS Toolset was fully funded by the Swiss Federal Office for Spatial Development ARE. In addition, some earlier parts of the work leading to the development of the USM Toolset were funded by the following institutions and foundations: the Swiss National Research Programme NRP 68 "Soil as a Resource", Swiss Federal Institute for Forest, Snow and Landscape Research WSL (Birmensdorf, Switzerland), Paul Schiller Foundation (Lachen, Switzerland), Sophie and Carl Binding Foundation (Basel, Switzerland) and the Bristol Foundation - Ruth und Herbert Uhl- Forschungsstelle für Natur- und Umweltschutz (Schaan, Principality of Liechtenstein).

Suggested References

- Behnisch, M., Krüger, T., Jaeger, J.A.G. (2022): Rapid rise in urban sprawl: Global hotspots and trends since 1990. *PLOS Sustainability and Transformation* 1(11): 0000034. <https://doi.org/10.1371/journal.pstr.0000034>
- Concepción, E.D., Obrist, M.K. Moretti, M., Altermatt, F., Baur, B., Nobis, M.P. (2016). Impacts of urban sprawl on species richness of plants, butterflies, gastropods and birds: not only built-up area matters. *Urban Ecosystems* 19(1), 225–242.
- El Dabee, N., Hudson, B., Zou, Y. Y., Prudencio Macaraeg, A. (2015). Brossard City center report. Advanced urban design laboratory, Concordia University.
- European Environment Agency (EEA) and Swiss Federal Office for the Environment (FOEN). (2016). Urban Sprawl in Europe. Joint EEA-FOEN report. EEA Report No 11/2016. Authors: Hennig, E.I., Soukup, T., Orlitova, E., Schwick, C., Kienast, F., Jaeger, J.A.G. ISSN 1777-8449, ISBN 978-92-9213-738-0, doi: 10.2800/143470. Luxembourg, Publications Office of the European Union. 135 pp. (+ Annexes 1-5: Urban sprawl in Europe. Joint EEA-FOEN report. 141 pp.). Available online at: <http://www.eea.europa.eu/publications/urban-sprawl-in-europe>.
- European Environment Agency (EEA) and Swiss Federal Office for the Environment (FOEN). (2011). Landscape fragmentation in Europe. Joint EEA-FOEN report. EEA Report No 2/2011, Authors: Jaeger, J.A.G., Soukup, T., Madiřňán, L.F., Schwick, C., Kienast, F. Luxembourg, Publications Office of the European Union. 87 pp. Available online: <http://www.eea.europa.eu/publications/landscape-fragmentation-in-europe/>.
- Gagné, S. A. and Fahrig, L. (2010). 'The trade-off between housing density and sprawl area: Minimising impacts to forest breeding birds', *Basic and Applied Ecology* 11(8), 723–733 (DOI: <http://dx.doi.org/10.1016/j.baae.2010.09.001>).
- Hennig, E.I., Schwick, C., Soukup, T., Orlitová, E., Kienast, F., Jaeger, J.A.G. (2015). Multi-scale analysis of urban sprawl in Europe: Towards a European de-sprawling strategy. *Land Use Policy* 49: 483-498.
- Jaeger, J., Schwick, C., Bertiller, R., Kienast, F. (2008). Urban sprawl in Switzerland: Quantitative analysis 1935 to 2002 and implications for regional planning (in German). Scientific final report. Swiss National Science Foundation. National Research Programme NRP 54 „Sustainable Development of the Built Environment“. Zurich, 344 pp.
- Jaeger, J.A.G., Bertiller, R., Schwick, C., Kienast, F. (2010a). Suitability criteria for measures of urban sprawl. *Ecol. Indic.* 10 (2), 397–406.
- Jaeger, J.A.G., Bertiller, R., Schwick, C., Cavens, D., Kienast, F. (2010b). Urban permeation of landscapes and sprawl per capita: new measures of urban sprawl. *Ecol. Indic.* 10 (2), 427–441.
- Jaeger, J.A.G., Schwick, C. (2014). Improving the measurement of urban sprawl: Weighted Urban Proliferation (WUP) and its application to Switzerland. *Ecol. Indic.* 38, 294–308.
- Jaeger, J.A.G., Soukup, T., Schwick, C., Hennig, E.I., Orlitova, E., Kienast, F. (2015). Zersiedelung in Europa: Ländervergleich und treibende Kräfte. (in German; Urban sprawl in Europe: Comparison of countries and driving forces.) In: Meinel, G., Schumacher, U., Behnisch, M., Krüger, T. (Hrsg.): *Flächennutzungsmonitoring VII: Boden – Flächenmanagement – Analysen und Szenarien*. IÖR-Schriften Band 67. Rhombos-Verlag, Berlin. ISBN 978-3-944101-67-5, pp. 267-277. PDF online: <https://www.ioer.de/publikationen-produkte/ioer-schriften/ioer-schriften-67/>.
- Jaeger, J.A.G., Schwick, C., Nazarnia, N., Pourtaherian, P., Mosharafian, S., Behnisch, M., Krüger, T., Maurer, Y. (2024, in prep.). Measuring and monitoring urban sprawl: Necessary steps toward more effective anti-sprawl policies. In: *A World Scientific Encyclopedia of Next Generation Cities*. Ed.-in-Chief: U. Eicker. Volume 2: Built and Natural Environments. Volume eds.: P. Gauthier, E. Yonder, C. Ziter, H. Ge. World Scientific Publishing.

- Nazarnia, N., Schwick, C., Jaeger, J.A.G. (2016). Accelerated urban sprawl in Montreal, Quebec City, and Zurich: Investigating the differences using time series 1951-2011. *Ecol. Indic.* 60: 1229-1251.
- Nazarnia, N., Schwick, C., Pourtaherian, P., Kopecky, M., Soukup, T., Orlitova, E., Kienast, F., Jaeger, J.A.G. (2023): Urban Sprawl Metrics (USM) Toolset – User Manual for ArcMap – Second Edition. Concordia University Montreal, Spectrum Research Repository. Link: <https://spectrum.library.concordia.ca/id/eprint/992200/>
- Pourtaherian, P., Jaeger, J.A.G. (2022). How effective are greenbelts at mitigating urban sprawl? A comparative study of 60 European cities. *Landscape and Urban Planning* 227: 104532 (17 pages). doi:10.1016/j.landurbplan.2022.104532
- Pourali, M., Townsend, C., Kross, A., Guindon, A., Jaeger, J.A.G. (2022): Urban sprawl in Canada: Values in all 33 Census Metropolitan Areas and corresponding 469 Census Subdivisions between 1991 and 2011. *Data in Brief* 41: 107941 (12 pages). <https://doi.org/10.1016/j.dib.2022.107941>
- Schwarzak, M., Behnisch, M., Meinel G. (2014). Zersiedelung in Deutschland - erste Ergebnisse nach Schweizer Messkonzept. (in German; Urban sprawl in Germany - first results according to Swiss measurement method.) In: Meinel, G.; Schumacher, U.; Behnisch, M. (Hrsg.): *Flächennutzungsmonitoring V: Methodik – Analyseergebnisse - Flächenmanagement*. IÖR-Schriften Band 61. Rhombos-Verlag, Berlin. ISBN 978-3-944101-18-7, S. 63-70.
- Schwick, C., Jaeger, J.A.G. (2010). Urban sprawl and its appearances in Switzerland in a spatial planning perspective: Quantitative Analysis 1935-2002. Expert report. (in German; Zersiedelung und ihre Ausprägungen in der Schweiz aus raumplanerischer Sicht: Quantitative Analyse 1935-2002.) ARE-Expertenbericht für das Schweizerische Bundesamt für Raumentwicklung, Bern. 38 pp. Available online at: <http://www.aren.admin.ch/themen/raumplanung/00246/00452/00453/index.html>.
- Schwick, C., Jaeger, J., Bertiller, R., Kienast, F. (2010). Zersiedelung der Schweiz – unaufhaltsam? Quantitative Analyse 1935 bis 2002 und Folgerungen für die Raumplanung. Bristol-Schriftenreihe. ISBN 978-3-258-07630-0. Haupt-Verlag, Bern / Stuttgart / Wien. 114 pp. and 4 maps.
- Schwick C., Jaeger J.A.G., Bertiller R., Kienast, F. (2012). L'étalement urbain en Suisse – Impossible à freiner? Analyse quantitative de 1935 à 2002 et conséquences pour l'aménagement du territoire. / Urban sprawl in Switzerland – unstoppable? Quantitative Analysis 1935 – 2002 and implications for regional planning. Zurich, Fondation Bristol; ISBN 978-3-258-07721-5. Berne, Stuttgart, Vienne, Haupt-Verlag. 216 pp. and 4 maps. (bilingual: French and English).
- Schwick, C., Jaeger, J., Hersperger, A., Kienast, F. (2013). Strongly accelerated increase in urban sprawl in Switzerland (in German; Stark beschleunigte Zunahme der Zersiedelung in der Schweiz). *Geomatik Schweiz* 111(2): 48-53.
- Schwick, C., Kienast, F., Jaeger, J. (2013). Zerschneidung und Zersiedelung im Rahmen der Landschaftsbeobachtung Schweiz. (in German; Landscape dissection and urban sprawl in the Swiss landscape monitoring program.) In: Meinel, G., Schumacher, U., Behnisch, M. (Hrsg.): *Flächennutzungsmonitoring V: Methodik – Analyseergebnisse - Flächenmanagement*. IÖR-Schriften Band 61. Rhombos-Verlag, Berlin. ISBN 978-3-944101-18-7, pp. 63-70.
- Soukup, T., Orlitova, E., Kopecky, M., Jaeger, J., Schwick, C., Hennig, E.I., Kienast, F. (2015). Application of a new GIS tool for urban sprawl in Europe. *Forum für Wissen, WSL Berichte Heft 33*, ISSN 2296-3448, Birmensdorf, Switzerland, pp. 57-64. PDF online: <http://www.wsl.ch/dienstleistungen/publikationen/pdf/15127.pdf>.
- Schwick, C., Jaeger, J.A.G., Kienast, F. (2011a). Zersiedelung messen und vermeiden. (in German; Measuring and avoiding urban sprawl.) – Merkblatt für die Praxis 47. Eidgenöss. Forschungsanstalt WSL, Birmensdorf, Switzerland. 12 pp. Available online at: http://www.wsl.ch/info/fokus/zersiedelung/index_DE.

- Schwick, C., Jaeger, J.A.G., Kienast, F. (2011b). Mesurer et éviter l'étalement urbain. - Notice pour le praticien 47. Institut fédéral de recherches WSL, Birmensdorf, Suisse. 12 pp. Available online at: http://www.wsl.ch/info/fokus/zersiedelung/index_FR.
- Sprague, S., Chinerman, S., Aouad, P. (2016). Cartierville urban vision report. Advanced urban design laboratory. Department of Geography, Planning & Environment, Concordia University.
- Statistics Canada. (2011). Spatial data files, built-up area data for 2011, Montreal census metropolitan area. Available online at: http://www.statcan.gc.ca/pub/16-201-x/2016000/list_m-c-eng.htm, last accessed: 23 December 2016.
- Torres, A., Jaeger, J.A.G., Alonso, J.C. (2016). Multi-scale mismatches between urban sprawl and landscape fragmentation create windows of opportunity for conservation development. *Landscape Ecology*. doi: 10.1007/s10980-016-0400-z.
- Ville de Montréal. (2016). Arrondissement de Verdun, Domaine Saint-Paul, Boisé de l'Île-des-Sœurs. Available online at: http://ville.montreal.qc.ca/portal/page?_pageid=8637,95933821&_dad=portal&_schema=PORTAL (last accessed: 14 December 2016).
- Wissen Hayek, U., Jaeger, J.A.G., Schwick, C., Jarne, A., Schuler, M. (2011). Measuring and assessing urban sprawl: What are the remaining options for future settlement development in Switzerland for 2030? – *Applied Spatial Analysis and Policy* 4(4): 249-279, DOI 10.1007/s12061-010-9055-3.