Discrete Event Control Kit

DECK 1.2013.11 User Manual

Shahin Hashtrudi Zad Department of Electrical and Computer Engineering Concordia University

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Abstract

Discrete Event Control Kit (DECK) is a toolbox (a set of functions) written in the programming language of MATLAB [2] for the analysis and design of supervisory control systems based on discrete—event models. This software has been developed by Shahin Hashtrudi Zad and two of his graduate students, Shauheen Zahirazami and Farzam Boroomand. It has been developed and tested on MATLAB release R2012b. DECK is provided under the terms of the GNU General Public License, version 2, as published by the Free Software Foundation. The text of the license appears in Appendix C.

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1 Introduction

Discrete Event Control Kit (DECK) is a toolbox (set of M-file functions) written in the programming language of MATLAB [2] for the analysis and design of supervisory control systems based on the Ramadge-Wonham (RW) theory of supervisory control of discrete-event systems (DES) [3]. The current version of DECK supports the case of supervision under full event observation. Future versions will extend the support to other cases. For information about supervisory control, the reader is referred to [5, 1].

DECK has been developed in the familiar environment of MATLAB as an educational tool for a graduate course at Concordia University on the supervisory control of discrete–event systems. Furthermore, DECK offers a set of functions that, along with the matrix and set operations of MATLAB, provide a convenient setup for implementing new algorithms and applying them to useful and interesting test cases.

The rest of this user manual is organized as follows. Section 2 explains how discrete—event models are built in DECK and provides an overview of the analysis and design functions that are available in DECK. The application of these functions to two examples is covered in Section 3. The second example is a well–known benchmark problem for which performance results (specifically, execution times) are provided. Section 4 contains the description of the functions. Appendix A contains a note on installation and Appendix B provides the release notes. Appendix C contains the text of the GNU General Public License, version 2.

2 Building Models and Solving Problems

In the RW supervisory control theory [3], it is assumed that the plant and the design specifications can be modeled as finite–state automata. A finite–state automaton is a five–tuple

$$G = (X, \Sigma, \eta, x_0, X_m)$$

where X is the finite state set, Σ the event set, x_0 the initial state, $X_m \subseteq X$ the set of marked states and $\eta: X \times \Sigma \to X$ is the transition (partial) function. An example is given in Fig. 1 with $X = \{1, 2, 3\}, \Sigma = \{11, 12\}, x_0 = 1$ and $X_m = \{2, 3\}$. The marked states are

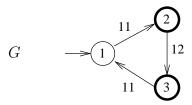


Figure 1: Automaton G.

shown with thick circles.

In DECK, an automaton is characterized by

- 1. N, the number of states,
- 2. TL, the list of transitions, and
- 3. Xm, the set of marked states.

N is a nonnegative $(N \ge 0)$ integer. For an automaton with $N \ge 1$, the state set is $\{1, \ldots, N\}$, with 1 used for the initial state. For an empty automaton, N = 0.

The event labels are nonnegative integers ¹. Zero (0) is reserved for clock tick. In supervisory control, the event set is partitioned into controllable and uncontrollable event sets. The controllability status of an event depends on the extent and scope of a supervisor's control over the plant and hence on both the plant and the supervisor. This issue becomes important, for instance, in decentralized supervisory control. Therefore, in DECK when an automaton is defined, the controllable/uncontrollable status of events are not specified. This status is declared only when a function related to supervisory control (i.e., supcon and controllable) is used.

TL (transition list) is a matrix with three columns. Each row represents a transition in the form [x1 e x2], where x1, e and x2 are the source state, event and target state. The event set Σ is implicitly taken to be the event labels that appear in the second column of the transition list, TL.

¹The default type for numerical variables in MATLAB is double precision floating point. To prevent roundoff errors in storing integer labels, the event labels should be no larger than 9×10^{15} .

Xm is a row vector containing the marked states.

The function automaton builds automaton objects. For example, the following statements build an automaton object G corresponding to the automaton G in Fig. 1.

```
N=3;
TL=[1 11 2; 2 12 3; 3 11 1];
Xm=[2 3];
G=automaton(N,TL,Xm);
```

Alternatively, the following compact form may be used.

```
G=automaton(3, [1 11 2; 2 12 3; 3 11 1], [2 3]);
```

The vector Xm (marked states) is optional and if omitted in the automaton statement, the default value of empty (Xm=[]) will be taken. Once the automaton object G is created, typing G returns a list of its properties, namely, the number of states, transition list and marked states (An automaton object does not have any methods).

G

G =

automaton

Properties:

N: 3

TL: [3x3 double]

Xm: [2 3]

Methods

Note that thoroughout this manual, MATLAB/DECK responses are shown in italics.

The number of states, transition list and marked states of an automaton object G can be accessed through G.N, G.TL and G.Xm. For example:

G.TL

ans =

1 11 2 2 12 3 3 11 1 The function automatonchk can be used to verify that an automaton object conforms to the conventions of DECK for naming states and event labels. This function is useful for checking DECK models that are created for the first time or imported from an input file. It can also help with debugging new functions developed in the DECK environment.

After the desired automata are built, they can be analyzed and manipulated using the available functions in DECK. The reach function can be used to perform reachability analysis on the transition graphs of automata. The function reachable and trim return the reachable and trim subautomata while complement finds the complement of an automaton. The project function returns a deterministic automaton that represents the natural projection of the marked and closed behaviors of its input automaton, and selfloop adjoins selfloops to each state of its input automaton (i.e., performs inverse projection).

The function is nondet determines if an automaton is nondeterministic and deterministic converts nondeterministic automata to deterministic automata.

The functions product and sync perform the parallel product (also known as "meet") and the synchronous product of an arbitrary number of automata G1, ..., Gn. The product and sync functions can also find the parallel and synchronous products of an array of automata. Furthermore, for every state of the resulting automaton, these functions return the information about the state of each of the constituent automata G1, ..., Gn.

Finally, the function **supcon** can be used to find the supremal controllable sublanguage and design minimally restrictive supervisor. The function **controllable** can be used to see if a language is controllable and in cases where controllability test fails, to obtain information about the circumstances under which the property has failed.

More details about each function is provided in Sec. 4 (Toolbox Functions). In the following section, two illustrative examples will be discussed.

3 Examples

3.1 Small Factory

This example has two parts. First it illustrates supervisor design using the Small Factory problem (Example 3.4.4, [5]). Next, it explains how it can be verified whether the plant (small factory) under the supervision of a given supervisor meets the design specifications.

The Small Factory (Fig. 2) consists of two machines, MACH1 and MACH2, and a buffer



Figure 2: Small Factory.

with a capacity of one. The automaton model of MACHi is depicted in Fig. 3. Starting

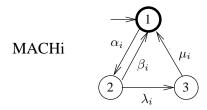


Figure 3: MACHi (i=1,2).

from the initial state I (idle), MACH1 takes a piece (α_1) from an (infinite) input bin and enters state W (work). Once the work of MACH1 is done, it deposits the workpiece in the buffer (β_1). If MACH1 breaks down (λ_1) and enters state D (down), the workpiece will be discarded but the machine can be repaired (μ_1). MACH2 takes workpieces from the buffer and puts the finished workpieces in an output bin.

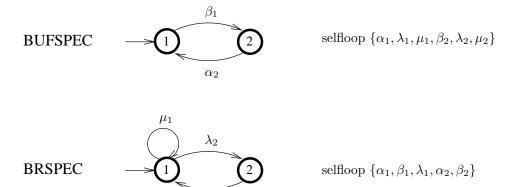
The objective is to design a supervisor to have a nonblocking system (i.e. plant under supervision) that meets the following design specifications.

- (S1) The buffer must not overflow or underflow.
- (S2) In case both machines fail, MACH2 must be repaired first.

The above two specifications can be captured using the following automata [5]. For the purpose of control, the events α_1 , α_2 , μ_1 and μ_2 are controllable and the rest of events are uncontrollable.

To design supervisor using DECK, we use the following codes for events (which are the same as those in [5]).

 $\begin{array}{llll} \alpha_1:11 & \beta_1:10 & \lambda_1:12 & \mu_1:13 \\ \alpha_2:21 & \beta_2:20 & \lambda_2:22 & \mu_2:23 \end{array}$



 μ_2

Figure 4: Small Factory: design specifications.

States I, W and D are named 1, 2 and 3. The following script design a minimally restrictive supervisor.

```
N1=3;
TL1=[1 11 2; 2 10 1; 2 12 3; 3 13 1];
Xm1=1;
MACH1=automaton(N1,TL1,Xm1);
N2=3;
TL2=[1 21 2; 2 20 1; 2 22 3; 3 23 1];
Xm2=1;
MACH2=automaton(N2,TL2,Xm2);
FACT=sync(MACH1,MACH2);
BUFSPEC=automaton(2, [1 10 2; 2 21 1], [1 2]);
BUFSPEC=selfloop(BUFSPEC, [11, 13, 14, 20, 22, 23]);
BRSPEC=automaton(2, [1 13 1; 1 22 2; 2 23 1], [1 2]);
BRSPEC=selfloop(BRSPEC, [10,11,13,20,21]);
SPEC=product(BUFSPEC, BRSPEC);
Euc=[10 12 20 22];
FACTSUP=supcon(SPEC,FACT,Euc);
```

First two automata objects MACH1 and MACH2 are created. Next the plant model FACT is obtained using the sync procedure. After automata objects for BUFSPEC and BRSPEC

are built, the automaton object SPEC is found using the product command. Finally the set of uncontrollable events are defined and the supervisor (in the form of an automaton FACTSUP) is obtained using supcon. FACTSUP has 12 states and 24 transitions.

FACTSUP

FACTSUP =

automaton

Properties:

N: 12

TL: [24x3 double]

Xm: [1 3]

Methods

The transition list and marked states can be examined as follows.

FACTSUP.TL

ans =

1	11	2
2	10	3
2	12	4
3	21	5
4	13	1
5	11	6
5	20	1
5	22	7
6	10	9
6	12	8
6	20	2
6	22	10
7	11	10
7	23	1
8	13	5
8	20	4
8	22	11
9	20	3
9	22	12
10	10	12
10	12	11

Figure 5: Small Factory: proposed supervisor BUFSUP.

10	23	2
11	23	4
12	23	3

FACTSUP.Xm

ans =

1 3

In the second part of this problem, let us consider Small Factory again with the objective of finding a nonblcking supervisor enforcing design specification S1 (regarding buffer overflow and underflow). First suppose the automaton in Fig. 5 has been proposed for supervisor. Note that this automaton is the same as the spec automaton BUFSPEC. The following script first builds the plant model which contains 9 states. This time, in addition to FACT, we have decided to get the information of the states of the components (MACH1 and MACH2) in the 9×2 matrix FACT_States. Next the proposed suprevisor BUFSUP is built and the controllable procedure is used to determine if BUFSUP is admissible (i.e., the closed behavior L(BUFSUP) is controllable).

```
MACH1=automaton(3, [1 11 2; 2 10 1; 2 12 3; 3 13 1], 1);
MACH2=automaton(3, [1 21 2; 2 20 1; 2 22 3; 3 23 1], 1);
[FACT,FACT_States]=sync(MACH1,MACH2);

BUFSPEC=automaton(2, [1 10 2; 2 21 1], [1 2]);
BUFSPEC=selfloop(BUFSPEC,[11 12 13 20 22 23]);

BUFSUP=automaton(2, [1 10 2; 2 21 1],[1 2]);
BUFSUP=selfloop(BUFSUP,[11 12 13 20 22 23]);

Euc=[10 12 20 22];
[ic,S,E]=controllable(BUFSUP,FACT,Euc)
```

The results are returned in ic, S, E.

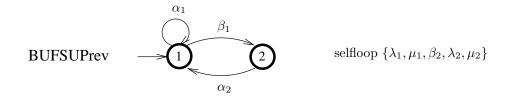


Figure 6: Small Factory: revised supervisor.

$$E = [10] [10] [10]$$

It is observed that BUFSUP is not admissible. Uncontrollable event disablement would occur when the plant and supervisor are in states given by the rows of S. The corresponding disabled uncontrollable events are provided in E. For instance, one such disablement occurs when FACT and BUFSPEC are in states 2 and 2. To determine the states of MACH1 and MACH2 when FACT is in state 2, we use

Thus MACH1 is in state 2 and MACH2 in state 1. In other words, when the buffer is full, MACH1 is in state 2 (W) and potentially ready to deposit another workpiece in the buffer, BUPSUP attempts to disable the uncontrollable event β_1 (event 10). In order to correct this issue, we remove the α_1 selfloop in state 2 of BUFSUP after the occurrence of β_1 (workpiece deposit in buffer) and effectively disable controllable event α_1 when the buffer is full. The resulting supervisor BUFSUPrev is shown in Fig. 6. We can see that this supervisor is addmissible.

```
[icrev,Srev,Erev]=controllable(BUFSUPrev,FACT,Euc)
icrev =
      1
Srev =
      []
Erev =
     {}
To verify that the plant under supervision is nonblocking and satisfies the design spec, first
it must be built.
FACTuSUP=product(FACT,BUFSUPrev)
FACTuSUP =
  automaton
  Properties:
     N: 12
    TL: [25x3 double]
    Xm: [1 3]
  Methods
Next the automaton FSco is constructed which marks L_m(FACT) \cap [L_m(SPEC)]^{co}.
SPECco=complement(BUFSPEC);
FSco=product(FACTuSUP,SPECco)
We note that the marked state set of FSco is empty and hence, L_m(FACT) \subseteq L_m(SPEC).
FSco.Xm
ans =
   Empty matrix: 1-by-0
```

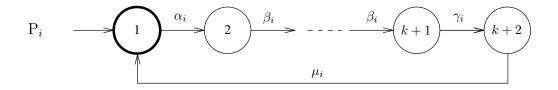


Figure 7: Dining Philosophers: Philosopher P_i .

Finally, to see if the (reachable) automaton FACTuSUP is nonblocking, the trim procedure is used.

FACTuSUPt=trim(FACTuSUP)
FACTuSUPt =
 automaton

Properties:

N: 12

TL: [25x3 double]

Xm: [1 3]

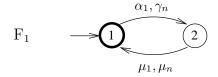
Methods

FACTUSUP has the same number of states as FACTUSUPt and hence it is nonblocking.

3.2 Dining Philosophers

In this example, an extension of the problem of Dining Philosophers (which was proposed in WODES 2008 as a benchmark problem for supervisory control software tools) is examined. In this problem, n philosophers P_1, \ldots, P_n ($n \geq 2$) are seated around a table and n forks F_1, \ldots, F_n placed on the table in the following order: $F_1, P_1, F_2, P_2, \ldots, F_n, P_n$. The automaton modeling philosopher P_i is shown in Fig. 7. Philosopher P_i takes the fork on his left F_i (event α_i) and executes k-1 ($k \geq 1$) intermediate events β_i till it reaches state k+1. Then it takes the fork on his right (that is F_{i+1} when $1 \leq i \leq n-1$, and F_1 when i=n.) and enters eating state k+2 (event γ_i). Finally, P_i returns the forks (event μ_i) and goes to its initial (idle) state. The automata for forks are shown in Fig. 8. The events "philosopher takes the left fork" (α_i) are assumed uncontrollable when i is even. The rest of events are controllable. The objective is to design a maximally permissive nonblocking supervisor.

The script for solving the problem is provided at the end of this section. Note that the automata for philosophers and forks are put together to form an array of automata Gs. The commands tic and toc measure the execution time of supcon. The execution times, along



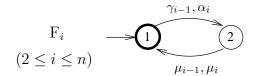


Figure 8: Dining Philosophers: Fork F_i .

with the number of states of the supervisor, are provided for various values of n and k in Table 1.

Remark: Note that the philosopher and fork automata are placed in array Gs in the order $F_1, P_1, \ldots, F_n, P_n$. The order affects the execution time (and space requirement) of the sync operation (despite the fact that the order of arguments in sync function does not change the final result – except perhaps for the name of the states). For instance, for n = 10 and k = 1, $sync(P1, \ldots, Pn, F1, \ldots, Fn)$ takes 24 times longer to run compared with $sync(F1, P1, \ldots, Fn, Pn)$. For an explanation, refer to the description of the sync function in Sec. 4.

$k \setminus n$	2	3	4	5	6	7	8	9	10	11	12	
1	< 0.1	< 0.1	< 0.1	< 0.1	0.2	0.5	1.7	5.8	28.1	185	1476	T (sec)
	3	12	30	78	190	470	1138	2770	6694	16206	39138	N
2	< 0.1	< 0.1	< 0.1	0.3	1.4	7.9	89.8	1240				T (sec)
	4	24	83	321	1082	3855	12863	44172				N
4	< 0.1	< 0.1	0.4	3.5	69	2795						T (sec)
	6	60	327	2175	11602	69785						N
8	< 0.1	0.3	4.8	325								T (sec)
	10	180	1703	21267								N
16	< 0.1	2	313									T (sec)
	18	612	10695									N

Table 1: Dining Philosophers: Execution time of supcon, T (sec), and the number of states of the resulting automaton, N, for various values of philosopher number, n, and intermediate states, k. Execution times are measured on a PC with Intel Core i5-2500, 3.10 GHz, 8GB RAM, running 64-bit Windows 7 and MATLAB R2011b (64-bit). Execution times longer than one hour have not been measured.

Script for solving the problem of Dining Philosophers

```
% Solves the "Dining Philosophers" benchmark problem of WODES 2008
%
display('Dining Philosophers')
% Number of philosophers (and forks) (n>=2)
n=9;
fprintf('Number of philosophers (n): %d\n', n)
% Number of intermediate states
k=1;
fprintf('Number of intermediate states (k): %d\n', k)
%
% Plant model (G)
display('Building Plant model (G)')
% Event coding
%
  For philosopher Pi:
     alpha(i)=10*i+1
                       beta(i)=10*i+2 gamma(i)=10*i+3 mu(i)=10*i+4
alpha=10*(1:n)+1;
beta=10*(1:n)+2;
gamma=10*(1:n)+3;
mu=10*(1:n)+4;
%
% Gs is an array of the automata of Philosophers and Forks
% in the order F1, P1, F2, P2, ..., Fn, Pn.
for i=1:2*n
  Gs{i}=automaton(0,[],[]);
end
%
% Philosophers
for i=1:n
```

```
TLi=[1 alpha(i) 2];
  for j=2:k
    TLi=[TLi; j beta(i) j+1];
  TLi=[TLi; k+1 gamma(i) k+2; k+2 mu(i) 1];
  Gs{2*i}=automaton(k+2, TLi, 1);
end
%
% Forks
% The first fork
Gs{1}=automaton(2, [1 alpha(1) 2; 1 gamma(n) 2; 2 mu(1) 1; 2 mu(n) 1], 1);
% The other forks
for i=2:n
  Gs{2*i-1}=automaton(2, [1 gamma(i-1) 2; 1 alpha(i) 2;
                        2 mu(i-1) 1; 2 mu(i) 1], 1);
end
G=sync(Gs);
% Spec (H)
display('Building Spec model (H)')
% Event set
if k==1
  E=[alpha gamma mu];
else
  E=[alpha beta gamma mu];
H=selfloop(automaton(1,[],1),E);
% Uncontrollable events
Euc=alpha(2:2:n);
display('Supcon')
```

```
tic
K=supcon(H,G,Euc);
toc
%
%
%
End of code
```

4 Toolbox Functions

4.1 Automaton

Create an automaton model ('automaton' object) for use by Discrete Event Control Kit (DECK).

Syntax

G=automaton(N,TL)
G=automaton(N,TL,Xm)

Inputs

N Number of states

TL Transition list

Xm Marked states (row vector)

Outputs

G Output automaton

Description

The class 'automaton' has the following properties:

N Number of states.

The states must be named using the following convention: the state set must be $\{1, ..., N\}$, with 1 used for the initial state.

TL Transition list.

TL is an m-by-3 matrix where m is the number of transitions. Each row of TL represents a transition in the form [x1, sigma, x2], with x1 and x2 being the source and destination states, and sigma, the corresponding event.

Xm Marked states (row vector).

G=automaton(N,TL,Xm) returns an automaton model (object) G with state set $\{1, ..., N\}$, transition list TL and set of marked states Xm.

G=automaton(N,TL) returns an automaton G with Xm=[].

4.2 Automatonchk

Verify the validity of an automaton object.

Syntax

```
flag1=automatonchk(G)
[flag1,flag2]=automatonchk(G)
```

Inputs

G Input automaton

Outputs

```
flag1 Automaton validity flag (part 1)
flag2 Automaton validity flag (part 2)
```

Description

[flag1,flag2]=automatonchk(G) verifies the validity of the automaton object G and returns the result in flag1. In cases where the automaton is not valid, the invalid property is identified in flag2. The various cases are explained in the following table.

flag1	flag2	Description
-3	1	G.N has wrong size (is not a scalar)
-3	2	G.TL has wrong size
-3	3	G.Xm has wrong size
-2	1	G.N is not an integer
-2	2	G.TL contains entry that is not an integer
-2	3	${\tt G.Xm}$ contains entry that is not an integer
-1	1	G.N is negative
-1	2	G.TL has out-of-range entry
-1	3	G.Xm has out-of-range entry
		(The valid range for states is 1,,G.N,
		and for events, nonnegative integers.)
	9	a mr. l
0	2	G.TL has repeated rows
0	3	G.Xm has repeated entries
1	0	Automaton is valid

Automatonchk examines the above list of cases from the top. Once a case is identified, the function returns with the corresponding flags.

4.3 Complement

Complement of a deterministic automaton.

Syntax

Gco=complement(G)
Gco=complement(G,Ea)

Inputs

G Input deterministic automaton

Ea List of events (vector)

Outputs

Gco Output deterministic automaton

Description

Let E denote the event set of the input automaton G.

Gco=complement(G) returns an automaton Gco with

$$L_m(G_{co}) = E^* - L_m(G), \quad L(G_{co}) = E^*$$

where $L_m()$ and L() denote marked behavior (marked language) and closed behavior (generated language), and E^* is the Kleene closure of E.

Gco=complement(G,Ea) returns an automaton Gco with

$$L_m(G_{co}) = E_e^* - L_m(G), \quad L(G_{co}) = E_e^*$$

where $E_e = E \cup E_a$. The event set of the input automaton, E, and E_a must be disjoint.

4.4 Controllable

Determine if a language is controllable.

Syntax

```
isctrb=controllable(K,G,Euc)
[isctrb,States]=controllable(K,G,Euc)
[isctrb,States,Events]=controllable(K,G,Euc)
```

Inputs

K Automaton representing the test language

G Plant Automaton

Euc Uncontrollable events (vector)

Outputs

isctrb Test result

States List of states where disablement of uncontrollable events occurs

Events List of disabled uncontrollable events (cell array)

Description

Let $L_m()$ and L() denote marked behavior (marked language) and closed behavior (generated language). isctrb=controllable(K,G,Euc) returns isctrb=1 if and only if L(K) is controllable with respect to L(G) and E_{uc} . Otherwise, it returns isctrb=0. When K is trim, controllable(K,G,Euc) returns 1 if and only if $L_m(K)$ is controllable with respect to L(G) and E_{uc} .

[isctrb,States]=controllable(K,G,Euc) returns a two-column matrix States. Each row of States, [xK,xG], is a state of product(K,G) where disablement of uncontrollable events (if any) occurs, i.e., the test fails. If L(K) is controllable (isctrb=1), then States=[].

[isctrb, States, Events] = controllable (K,G,Euc) returns the list of disabled uncontrollable events (if any) in the cell array Events. The i-th cell of Events, Events[i], is a row vector containing the uncontrollable events disabled in [xKi,xGi] (the i-th row of States).

Tip

The controllable function can be used to generate the list of all event disablements in a DES plant G, by a supervisor K, if the input argument Euc (the set of uncontrollable events) is replaced with the entire event set, E; that is, using [isctrb,States,Events]=controllable(K,G,E).

4.5 Deterministic

Convert nondeterministic automaton to deterministic automaton.

Syntax

Gdet=deterministic(G)
[Gdet,States]=deterministic(G)

Inputs

G Input automaton (deterministic or nondeterministic)

Outputs

Gdet Output automaton (deterministic)

States State set of output automaton (cell array)

Description

Gdet=deterministic(G) returns a deterministic automaton Gdet that has the same marked and closed behavior as G:

$$L_m(G_{\text{det}}) = L_m(G), \quad L(G_{\text{det}}) = L(G).$$

Here $L_m()$ and L() denote marked behavior (marked language) and closed behavior (generated language). If G is deterministic, then Gdet=G.

Deterministic uses the subset construction to build Gdet. [Gdet,States]=deterministic(G) returns a cell array States containing information about the states of Gdet. The i-the cell of Gdet, is a row vector containing the subset of states of the input automaton G associated with state i of Gdet.

4.6 Isnondet

Determine whether automaton is nondeterministic.

Syntax

flag=isnondet(G)

Inputs

G Input automaton

Outputs

flag logical 1 (true) or 0 (false)

Description

Returns logical 1 (true) if the input automaton G is nondeteterminstic. Otherwise it returns logical 0 (false).

4.7 Product

Product of automata.

Syntax

G=product(G1,...,Gn)
[G,States]=product(G1,...,Gn)

G=product(Ga)
[G,States]=product(Ga)

Inputs

Gi Input automaton i (i=1, ..., n)

Ga Cell array containing input automata

Outputs

G Output automaton

States State set of output automaton

Description

G=product(G1,...,Gn) returns the product of G1, ..., Gn $(n \ge 2)$. If $L_m()$ and L() denote marked behavior (marked language) and closed behavior (generated language), then

$$L_m(G) = Lm(G_1) \cap \ldots \cap L_m(G_n)$$

 $L(G) = L(G_1) \cap \ldots \cap L(G_n).$

[G,States]=product(G1,...,Gn) returns an $N \times n$ matrix States where N is the number of states of G. Let [xi1 ... xin] be the i-th row of States. Then xi1, ..., xin are the states of G1, ..., Gn when G is in state i.

Product can be used with arrays of automata. Let Ga denote a cell array containing automata Ga1, ..., Gan (n >= 2). product (Ga) returns the product of Ga1, ..., Gan.

4.8 Project

Find a deterministic automaton to represent the projection of a language.

Syntax

```
Go=project(G,Euo)
[Go,States]=project(G,Euo)
```

Inputs

```
G Input automaton (deterministic or nondeterministic)
Euo Events to be erased (vector)
```

Outputs

```
Go Output automaton (deterministic)
States State set of output automaton (cell array)
```

Description

Let E be the event set of the input automaton G, E_{uo} the events to be erased (unobservable events) and $P: E \to (E - E_{uo})$ the natural projection onto $E - E_{uo}$. Furthermore, let $L_m()$ and L() denote marked behavior (marked language) and closed behavior (generated language).

Go=project(G, Euo) returns a deterministic automaton Go which marks $P(L_m(G))$ and generates P(L(G)): $L_m(G_o) = P(L_m(G))$ and $L(G_o) = P(L(G))$. Go may be regarded as an observer automaton.

[Go,States]=project(G,Euo) returns a cell array States containing information about the states of Go. The i-the cell of States, States $\{i\}$, is a row vector containing the state estimate for the input automaton G when the observer Go is in state i.

4.9 Reach

Find the reachable states of transition graph.

Syntax

Xr=reach(TL,S)

Inputs

TL Transition list

S Source states (vector)

Outputs

Xr States reachable from S (row vector)

Description

Xr=reach(TL,S) returns the states of the (automaton) transition graph that are reachable from the set of source states S using the breadth-first-search algorithm. The reachable states appear in Xr in the order they are discovered in the breadth-first search.

4.10 Reachable

Find reachable subautomaton.

Syntax

Gr=reachable(G)
[Gr,Xr]=reachable(G)

Inputs

G Input automaton

Outputs

Gr Reachable subautomaton

Xr Reachable states of G (row vector)

Description

Gr=reachable(G) returns the subautomaton of G that is reachable (from the initial state of G). The states of Gr are renamed in the order they are discovered in a breadth-first search. [Gr,Xr]=reachable(G) returns the reachable states of G in Xr.

4.11 Selfloop

Add selfloops to automaton.

\mathbf{Syntax}

Gs=selfloop(G,Es)

Inputs

G Input automaton

Es List of events (vector)

Outputs

Gs Output automaton

Description

Adds selfloop transitions [x, e, x] to the transition list of the input automaton G, for all states x of G and all events e in the event list Es. The event set of G and Es must be disjoint.

4.12 Supcon

Supremal Controllable Sublanguage.

Syntax

K=supcon(H,G,Euc)

Inputs

H Specification (deterministic) automaton

G Plant (deterministic) automaton

Euc Uncontrollable events (vector)

Outputs

K Trim (deterministic) automaton marking supremal controllable sublangage

Description

Let $L_m()$ and L() denote marked behavior (marked language) and closed behavior (generated language). Supcon calculates the supremal sublanguage of $L_m(H) \cap L_m(G)$ that is controllable with respect to L(G) and E_{uc} . The result is returned in the trim automaton K which marks the supremal controllable sublanguage. The calculations are based on the algorithm introduced in

W.M. Wonham and P.J. Ramadge, "On the supremal controllable sublanguage of a given language," *SIAM J. Control and Optimization*, Vol. 25, No. 3, May 1987.

4.13 Sync

Synchronous product of automata.

Syntax

G=sync(G1,...,Gn)

[G,States]=sync(G1,...,Gn)

[G,States,Blocked_events] = sync(G1,...,Gn)

G=sync(Ga)

[G,States] = sync(Ga)

[G,States,Blocked_events] = sync(Ga)

Inputs

Gi Input automaton i (i=1, ..., n)

Ga Cell array containing input automata

Outputs

G Output automaton

States State set of output automaton

Blocked_events Events blocked (absent) in output automaton (row vector)

Description

G=sync(G1,G2) returns the synchronous product of G1 and G2. Let E_1 and E_2 be the event sets of G_1 and G_2 . If $L_m()$ and L() denote marked behavior (marked language) and closed behavior (generated language), then

$$L_m(G) = L_m(G_1) || L_m(G_2)$$

 $L(G) = L(G_1) || L(G_2)$

Here $L_1||L_2|$ is the synchronous product of languages L_1 and L_2 defined according to

$$L_1||L_2 = P_1^{-1}(L_1) \cap P_2^{-1}(L_2)$$

where P_1 (resp. P_2) is the natural project of $(E_1 \cup E_2)^*$ onto E_1^* (resp. E_2^*).

G=sync(G1,...,Gn) returns the synchronous product of G1,...,Gn (n>=2).

[G,States]=sync(G1,...,Gn) returns the $N \times n$ matrix States where N is the number of states of G. Let [xi1 ... xin] be the i-th row of States. Then xi1, ..., xin are the states of G1, ..., Gn when G is in state i.

[G,States,Blocked_events]=sync(G1,...,Gn) returns the row vector Blocked_events containing the events that are in the transition list of at least one of the input automata (Gi) and absent in the transition list of the output automaton (G).

Sync can be used with arrays of automata. Let Ga denote a cell array containing automata $Ga1, ..., Gan (n \ge 2)$. sync(Ga) returns the synchronous product of Ga1, ..., Gan.

Remark: The execution time (and space requirement) of the sync operation depends on the order of the input arguments G1, ..., Gn. This can be explained as follows. In DECK, G=sync(G1,G2,G3,G4), for instance, is evaluated in the following steps. First sync(G1,G2) is calculated. Let us call the result G12. Next G123=sync(G12,G3) and finally G=sync(G123,G4) are found. If automata that have common events are listed next to eachother, then the intermediate automata resulting from successive application of sync (in our example, G12, G123) are likely to have fewer states because of the interactions among the neighboring automata on the list of input arguments. Therefore, this results in smaller intermediate automata (hence, less space requirement) and faster execution time. Coversely, if automata with no common events appear first on the list of sync, the intermediate automata in sync computations could become very large, resulting in prolonged execution times.

4.14 Trim

Find the reachable and coreachable subautomaton.

Syntax

```
Gt=trim(G)
[Gt,Xrc]=trim(G)
```

Inputs

G Input automaton

Outputs

Gt Trim subautomaton

Xrc States of G that are reachable and coreachable (row vector)

Description

Gt=trim(G) returns the trim subautomaton of G (containing only those states of G that are both reachable and coreachable). The states of Gt are renamed in the order they are discovered in a breadth—first search.

[Gt, Xrc]=trim(G) returns the states of G that are reachable and coreachable in Xrc.

A Installation

Simply unzip the downloaded file. If you wish to keep your data files and scripts in a separate directory (folder) and run DECK from that directory, then on the HOME tab (of MATLAB Desktop), in the ENVIRONMENT section, click on "Set path" to add the directory of DECK files to MATLAB's search path. Alternatively, this can be done using the command "path".

B Release Notes

DECK 1.2013.11

- New functions: deterministic, isnondet and project.
- Bug fixes:
 - The functions reachable, supcon and trim in the previous version of DECK resulted in MATLAB error message for some single—state automata that had two or more transitions. The problem is fixed in this version.

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