

1 **Modeling and Analysis of Renewable Heat Integration into**  
2 **Non-Domestic Buildings - The Case of Biomass Boilers: A**  
3 **Whole Life Asset-Supply Chain Management Approach**

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13  
14 **Abstract** – This study proposes a whole life asset-supply chain optimization model for  
15 integration of biomass boilers into non-domestic (non-residential) buildings, under a  
16 renewable heat incentive scheme in the UK. The proposed model aims at identifying the  
17 optimal energy generation capacities and schedules for biomass and backup boilers, along  
18 with the optimal levels of biomass ordering and storage. The sensitivity of these decisions  
19 are then analyzed subject to changes in source, types and pricing of biomass materials as  
20 well as the choice of technologies and their cost and operational performance criteria.  
21 The proposed model is validated by applying it to a case study scenario in the UK. The

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22 results indicate that a Renewable Heat Incentive scheme could incentivize the adoption of  
23 biomass boilers, with a 3 to 1 ratio for biomass and backup boilers' utilization. As such,  
24 the findings from this study will be useful for industry managers, tasked with the decision  
25 of which biomass boiler system to utilize, considering the support from RHI. On the other  
26 hand, it is shown that RHI does not provide an encouragement for efficiency when it  
27 comes to the choice of biomass technologies and fuels. This presents itself as a major  
28 implication for the success and sustainability of the UK government's renewable heat  
29 incentive scheme.

30

31 **Keywords:** Renewable Heat Incentive; Biomass Boilers; Non-domestic Buildings;  
32 System Dynamics; Supply Chain Management; Asset Management

33

## 34 **1. Introduction**

35 Energy from renewable sources not only plays a critical role in cutting carbon emissions,  
36 but also reduces dependency on fossil fuels, promoting energy security. Increasing the  
37 share of renewable energy is a major component of many national and regional energy  
38 directives across the globe, such as feed-in-tariff and renewable portfolio standard  
39 policies, which are mostly directed towards creating a surge in renewable electricity  
40 generation capacities [1]. Globally, however, heating is associated with about half of the  
41 final energy use, compared to about 30% and 20% shares for electricity and transport [2,  
42 3]. This clearly highlights the importance and impact of increasing the share of renewable  
43 energy sources for heat generation. Further, it should be mentioned that space heating and

44 hot water in domestic (residential) and non-domestic (non-residential) buildings account  
45 for over half of the global energy needs for heating purposes [2, 3].

46 This study is based in the UK and it develops and presents a model that is applicable  
47 to making optimized decisions regarding the choice of ‘building-integrated’ biomass  
48 boilers under the renewable heat incentive scheme of the UK government. In the UK,  
49 when it comes to use of renewable sources, electricity generation accounts for 75% of all  
50 installed renewable energy capacities, followed by heat and transport with a share of 15%  
51 and 10% [4]. This lack of investment in use of renewable energy for heat generation runs  
52 contrary to the fact that heating accounts for over 40% of energy consumption in the UK  
53 [5]. In the particular case of non-domestic buildings, about half of the energy  
54 consumption is attributable to heating [6]. Based on this realization, integration of  
55 renewable heat technologies into non-domestic buildings has become an integral part of  
56 the UK Government’s agenda for the building sector through the introduction of  
57 Renewable Heat Incentive (RHI) program in 2011 [7]. It is the world’s first support  
58 program that directly pays and incentivizes the non-domestic building participants  
59 generating and using renewable energy (from certain eligible technologies) to heat their  
60 buildings [8].

61 For managers who wish to participate in this scheme and take advantage of the  
62 incentives from the government, there are several important decisions to be made  
63 regarding, for example, the capacity of the biomass boiler and the type of biomass boiler.  
64 It is important that the right combination of decisions is made in order to maximize the  
65 incentives received to avoid a loss-making investment. It is also important for the success  
66 and sustainability of the UK government’s policy that a win-win scenario is generated

67 such that the buildings that invest in biomass boilers are not financially disadvantaged.  
68 Being a pioneering scheme, there is currently no model that can be applied to support and  
69 direct the integration of biomass boilers in buildings under RHI.

70 Recognizing such a gap, in the following sections, we first present a literature review,  
71 then turn to a methodology section exploring the rationale behind developing our  
72 proposed model, its elements including the objective function, decision variables, and  
73 constraints. We further elaborate on the adopted optimization framework, followed by a  
74 case study and results analysis to implement the model, interpret the findings and report  
75 on sensitivity of a number of targeted parameters. The paper concludes with a research  
76 summary as well as recommendations for future research.

77

## 78 **2. Literature Review**

79 RHI is designed to bridge the gap between the cost of fossil fuel heat and that of  
80 renewable heat technologies, thus, encouraging private investments in decentralized  
81 heating [9]. In addition to carbon saving benefits, decentralized heat generation in cities  
82 from renewable sources (instead of heating from centrally supplied electricity or natural  
83 gas) helps reduce the pressure on urban energy supply infrastructure [10], increasing their  
84 resilience, longevity and reliability. Under the RHI scheme, the eligible technologies are  
85 solar thermal collectors, biomass boilers, ground-source and air-to-water heat pumps, and  
86 biogas waste digesters [7]. The amount of the incentive is calculated based on three  
87 criteria of “type of technology”, “generation capacity”, and “actual renewable energy  
88 use”. Table 1 presents the renewable heat incentive structure for non-domestic  
89 applications. The leading technologies are solar thermal and biomass boilers that could

90 receive an incentive up to 9.2 and 8.6 pence per each KWh of renewable heat energy  
91 generated, respectively [7, 11]. The incentive payments are spread over 20 years and paid  
92 on a quarterly basis.

93 Biomass is the most utilized type of renewable energy in the UK that comprises a  
94 70.7% share of renewable energy uses for electricity and heat generation (followed by  
95 wind at 20.8% and solar at 5.4%) [4]. It has a 2.3% share in electricity generation and 1%  
96 in heat generation [5]. The UK Bioenergy Strategy for 2020 targets an increase of  
97 biomass share to 5–11% in power generation and 6% in heating [12]. As a result, some  
98 researchers have investigated the factors that could influence the growth of biomass  
99 energy sector for heating and power in the UK [13, 14]. Biomass, in this context, refers to  
100 solid biomaterials (in form of woodchips, pellets, etc.) produced from agricultural  
101 residues, waste wood, and municipal solid waste.

102 With support from the scheme RHI, the installation and use of biomass boilers is  
103 becoming a leading choice (for renewable heating) in non-domestic buildings in the UK  
104 [15]. There are many reasons to back such a transition. First, RHI provides a high level of  
105 support for small scale (less than 200KW) biomass boilers, second only to solar energy  
106 [7]. Also, the levelized capital cost (cost per KWh) of biomass boilers is considerably  
107 lower than solar thermal collectors [8]. Moreover, the energy conversion performance of  
108 biomass boilers (KWh output per unit cost) is higher than alternative renewable heating  
109 technologies [15]. In addition, there exists a higher level of standardization in  
110 manufacturing of biomass boilers, while the alternative technologies are project-based  
111 with high dependency on characteristics of each specific site. This also creates the  
112 advantage of flexibility in terms of generation capacity when it comes to biomass boilers.

113 Last but not the least is the fact that biomass is a fuel-based source of energy with  
114 benefits for various stakeholders across its supply chain, contributing to its promotion  
115 [16]. The promise of biomass applies to society at large by reducing dependence on fossil  
116 fuels and transferring some of the weight to more sustainable and environmentally  
117 friendly biomass fuels. There are also implications for the reduction of fossil fuel  
118 distribution through expensive centralized piping systems. These are in addition to the  
119 commercial advantages to the supply chain partners including biomass fuel suppliers,  
120 boiler manufacturers and transportation companies.

121 Investigating and understanding the potentials and challenges of mass utilization of  
122 building-integrated small size biomass boilers for space heating and hot water is an  
123 emerging area. Kranzl et al. [19] have developed a simulation model to forecast the 2030  
124 fuel-mix for space heating purposes in the EU countries, taking into account future  
125 scenarios of demand for space heating, potentials for renewable support policies and  
126 incentives, and expected energy (and fuels) prices. They have identified the integration of  
127 “small-scale biomass boilers” as one of the core drivers for future growth in renewable  
128 heating. Saidur et al. [20] provided a review of biomass boilers including common  
129 technologies, suitable fuels, and their advantages and disadvantages with respect to cost,  
130 requirements, operational performance and environmental impacts. As a result of the  
131 potential advantages of economies of scale [21], supplying renewable heat to buildings  
132 through utilization of biomass boilers for district heating is also receiving growing  
133 attention [22, 23]. McManus [24] has provided an environmental assessment framework  
134 to quantify the emission levels from a number of case study small size biomass boilers in  
135 the UK. Numerical models and computer simulations were also suggested to monitor and

136 control the operation of small size biomass boilers with the aim of increasing the energy  
137 efficiency and/or reducing NO<sub>x</sub> and CO emissions [25, 26]. Further, operational  
138 performance optimization frameworks were proposed to identify the optimal of mix of  
139 biomass fuels [27] and the optimal size of thermal storage for biomass boilers [28].

140 As the promotion of renewable heat technologies under the RHI scheme is a recent  
141 phenomenon, there has been very little research reported on the supply chain and asset  
142 management performance of the building-integrated biomass boilers (from cost,  
143 reliability, and environmental perspectives) with the existence of such an incentive [15,  
144 29].

145 Despite the recognized advantages of installing localized biomass boilers, there are  
146 also inherent risk factors. If not properly installed, the indoor air quality may deteriorate  
147 due to NO<sub>x</sub>, CO and other air pollutants from biomass burning [30, 31]. Biomass boilers  
148 operate with a lower energy conversion performance compared to natural gas boilers,  
149 requiring a considerable space for biomass storage. More importantly, as biomass is a  
150 seasonal (and mostly foreign) source of fuel, it requires a back-up natural gas boiler,  
151 presenting some challenges with respect to the need to a dual capacity planning (for two  
152 boilers) and availability of space (for both boilers and storage). The relaxation of energy  
153 consumption targets is another cause for concern. The concern is that by installing  
154 biomass boilers, building/facility managers can achieve the carbon target without making  
155 any extra efforts on energy conservation [5]. Thus there is a concern that behavioral  
156 patterns that develop may not be fully aligned with what was desired.

157 There are also variations in type, quality and supply chain characteristics of biomass  
158 materials with direct impact on their logistics and storage [32, 34], as well as indirect

159 influence on cost, energy efficiency, carbon performance, and operational requirements  
160 of boilers [17, 18]. This is an important factor when considering the success of the RHI  
161 scheme as it should be able to promote the use of more efficient and sustainable biomass  
162 materials [5, 13].

163

### 164 **3. Problem Statement**

165 This study is a first attempt to propose a whole life asset and supply chain simulation and  
166 optimization model to capture the integration of biomass boilers into non-domestic  
167 buildings with incorporation of back-up natural gas boilers. Figure 1 captures the  
168 elements of such a model with choices (decision variables) on suppliers, biomass  
169 purchase, boilers' capacities and their utilization subject to changes in biomass inventory  
170 levels and energy demand over time. Subject to various operational constraints including  
171 those on air pollution criteria, the model aims at identifying the optimal values of the  
172 above mentioned decision variables while minimizing the whole life cost of the system.  
173 A “whole life” perspective, as advocated in the asset management literature, is a costing  
174 scope that accounts for the ownership costs associated with physical assets during their  
175 service and residual life [35]. Through a case study, the sensitivity of the outcomes are  
176 then analyzed subject to changes in source, types and pricing of biomass materials as well  
177 as the choice of technologies and their cost and environmental performance profiles.

178

### 179 **4. Methodology**

180 Energy production from solid biomass comes with a number of peculiar supply chain  
181 management issues. Those are the seasonality of biomass (and its supply), variations in



182 types and quality of biomass materials, multiplicity of suppliers with varied  
183 characteristics, and environmental impacts of biomass transport [18, 33]. These issues  
184 can create complexities and uncertainties with respect to the use of biomass boilers.  
185 Consequently, there are important decisions to be made with respect to the installation  
186 and running of biomass boilers. In case of small biomass boilers (for domestic and non-  
187 domestic applications), there are further asset management challenges including the  
188 availability of various boiler technologies with varied capital intensity and operational  
189 performance, space requirements for the boiler, its backup, and biomass storage, and  
190 consideration of indoor air quality criteria [20].

191 In this sense, integration of biomass boilers into non-domestic buildings in the UK (as  
192 encouraged by RHI), needs to be carefully crafted using a combined supply chain/asset  
193 management model that addresses the above-mentioned issues. In such a model, we need  
194 to deal with decisions such as the selection of biomass sources, quantity and timing of  
195 orders, storage capacities, boilers' capacities, and energy production schedules. These  
196 decisions are made such that the system yields a minimum total cost that includes its  
197 supply chain expenditures as well as the capital and operational costs of its physical  
198 assets while meeting energy demand and certain technical and environmental constraints.

199 Several surveys of supply chain models with source selection, order allocation, and  
200 storage and production planning components have been reported in the literature [36, 37].  
201 In case of bioenergy, Mafakheri and Nasiri [18] have reviewed decision support and  
202 optimization models that have been developed in line with various operations along the  
203 bioenergy supply chains including harvesting, storage, transport, and energy conversion.  
204 Considering the literature on biomass supply chain modeling, there is a clear gap in the

205 models that can address the peculiar supply chain and operational attributes of “building-  
 206 integrated” biomass boilers. Consequently, given the encouragement from non-domestic  
 207 renewable heat incentive policy, and with respect to the supply chain and asset  
 208 management peculiarities of biomass boilers, we propose a combined life supply chain-  
 209 asset management model for integration of biomass boilers into non-domestic buildings  
 210 in the UK. The proposed model identifies an optimal integration and operation plan,  
 211 optimizing the total cost of biomass boiler’s ownership over its service life, with  
 212 decisions on biomass purchase, main and backup boilers’ capacities, and their energy  
 213 production levels that evolves over time. The model, with its objective function and the  
 214 associated technical, operational, and environmental constraints, is presented through the  
 215 following equations (descriptions of the symbols used in the model are provided in the  
 216 nomenclature section at the end):

217

218 The objective is to minimize the whole life (including asset management and supply  
 219 chain) cost of biomass and backup boilers over a targeted service life of  $T$ :

220

221 Minimize

222

$$\begin{aligned}
 \pi = & \underbrace{\sum_{t=1}^T \sum_{i=1}^n p_i^{(t)} \cdot s_i^{(t)}}_{\text{Biomass Purchase}} + \underbrace{\sum_{i=1}^n [c_i \cdot \sum_{t=1}^T s_i^{(t)}]}_{\text{Biomass Transport}} + \underbrace{h \cdot \sum_{t=1}^T I^{(t)}}_{\text{Biomass Storage}} + \underbrace{\sum_{t=1}^T p_g^{(t)} \cdot y^{(t)}}_{\text{Natural Gas Cost}} - \underbrace{\sum_{t=1}^T \beta^{(t)} \cdot x^{(t)}}_{\text{RHI Benefit}} \\
 & + \underbrace{c_b \cdot \sum_{t=1}^T x^{(t)}}_{\text{Biomass Boiler Utilization}} + \underbrace{(v + c_g) \cdot \sum_{t=1}^T y^{(t)}}_{\text{Backup Boiler Utilization}}
 \end{aligned} \tag{1}$$

223

224

225

226 Subject to the following constraints, and conditions:

227

$$228 \quad I^{(t)} = (1 - \alpha)I^{(t-1)} - \frac{1 + \varepsilon}{r_b} x^{(t)} + \sum_{i=1}^n s_i^{(t-t_i)}; \quad (2)$$

229 Eq.2 captures the biomass inventory at the end of any period of time, which is equal to  
230 the amount of in-hand inventory,  $I^{(t-1)}$ , that deteriorates with a spoilage rate of  $\alpha$ , minus  
231 biomass used in that period calculated based on converting biomass energy generation  
232 using biomass materials energy content (which is varying for different biomass materials)  
233 and boiler's efficiency rate (which is varying for different boiler technologies), and  
234 finally adding the biomass purchases that arrive for storage in the given period.

235 The above inventory level has a non-negative value (at least no inventory is in  
236 place) and is constrained by a maximum storage capacity due to space limitations:

$$237 \quad 0 \leq I^{(t)} \leq \bar{I}; \quad (3)$$

238

239 Also, the purchase from each supplier is a time dependent variable and could fluctuate  
240 over time due to changing needs of the client as well as the seasonality of biomass that  
241 impacts the capacity of suppliers:

$$242 \quad s_i^{(t)} \leq S_i; \quad (4)$$

243

244 There shall be a balance equation between heating energy generation and consumption  
245 from boilers:

$$246 \quad x^{(t)} + y^{(t)} = D^{(t)}; \quad (5)$$

247

248 We assume a preferential pricing from the suppliers (i.e. higher purchase from a  
249 particular supplier leads to a discount):

$$250 \quad p_i^{(t)} = P_i \left(1 - k_i \frac{s_i^{(t)}}{S_i}\right); \quad (6)$$

251

252 And more important, as per Table 1, the RHI mechanism links the amount of incentive to  
253 the hours of operation for the biomass boiler. In this sense, the RHI incentive rate is  
254 calculated based on the ratio of biomass energy generation to biomass boiler's capacity.  
255 This is where the non-linearity is introduced to our model:

$$256 \quad \beta^{(t)} = \begin{cases} \beta_1 & \frac{1}{X} \cdot \sum_{r=t-12}^t x^{(r)} \leq H \\ \beta_2 & otherwise \end{cases}; \quad (7)$$

257

258 The generation of energy from biomass and natural gas is not only bounded by the  
259 boilers' capacities but also is subject to boilers' availability at any particular point of time  
260 (i.e. accounting for the times that the boilers are unavailable for periodical service and  
261 maintenance):

$$262 \quad x^{(t)} \leq w_b^{(t)} X; \quad (8)$$

$$263 \quad y^{(t)} \leq w_g^{(t)} Y; \quad (9)$$

264

265 The decisions on boilers' capacities are subject to the availability of space. The size of  
266 boilers dictates the dimensions of the boiler room as it should host the boilers, their

267 associated hot water tank(s), panels, pipes, as well as the adjacent storage space for  
268 biomass following certain benchmarks [15]:

$$269 \quad l(X, Y) \leq L; \quad (10)$$

270

271 There are standards for air pollution criteria as well as targets for carbon emissions that  
272 could influence the energy generation mix from biomass and backup boilers:

$$273 \quad \sum_{t=1}^T e_j(x^{(t)}, y^{(t)}) \leq E_j \quad (j=1, 2, \dots, m); \quad (11)$$

$$274 \quad \sum_{t=1}^T e(x^{(t)}, y^{(t)}) \geq E_0 \quad (12)$$

275

276 And finally, the non-negativity conditions on supply and generation decision variables as  
277 well as the biomass and backup capacity requirements:

$$278 \quad s_i^{(t)}, x^{(t)}, y^{(t)} \geq 0 \quad \text{and} \quad X, Y > 0 \quad (13)$$

279

280 The schedule of the above decision variables is identified by simulating and optimizing  
281 the above multi-period non-linear model over the targeted service life of the system. We  
282 adopt the use of a system dynamics (SD) approach. Research in the use of system  
283 dynamics modeling in supply chain management is established in academic literature  
284 [38], mostly in close loop supply chains [39, 40] and reverse logistics [41]. System  
285 dynamics (SD) is a modeling framework developed in the 1960s [42] for analyzing the  
286 behavior of complex systems that evolve over time. The SD approach is a well-suited  
287 framework for our proposed model as; (1) the objective function (total cost of boilers'

288 ownership incorporated with the benefits from RHI), constraints (such as energy demand  
289 and biomass supply) and external drivers (such as energy prices and incentives) are  
290 varying over time, (2) there are a schedule of decisions made over time (capacities,  
291 production levels, and biomass purchase), (3) decisions made in one stage impact the  
292 ones in the subsequent stages, and (4) there are feed-back loops (circular causal  
293 relationships) in the model governing the interactions among various components of the  
294 model (as presented in Figure 2).

295 Figure 2 indicates that although heat energy generation from biomass boilers in non-  
296 domestic buildings is encouraged by the renewable heat incentive scheme, it is  
297 constrained by space requirements (eq. 10) as well as decisions on capacities (eqs. 8 and  
298 9) and inventories (eqs. 2 and 3). Eq. 2 captures the balancing relationship between  
299 biomass energy generation,  $x^{(t)}$ , and inventory of biomass,  $I^{(t)}$ , in which an increase in  
300 the former leads to a decrease in the latter. Replacing  $I^{(t)}$  with its equivalent from eq. 2  
301 in the left side of eq. 3 (i.e.  $I^{(t)} \geq 0$ ), we can depict the reinforcing relationship between  
302 biomass inventory,  $I^{(t-1)}$ , and biomass use for energy generation,  $x^{(t)}$  (i.e. energy  
303 generation from biomass is bounded by the inventory already in place). These causal  
304 relationships form a balancing “asset management loop”. On the other hand, the  
305 availability of biomass materials imposes a balancing “supply chain loop”. First, eq. 2  
306 shows the reinforcing (linear) relationship between the sum of biomass orders  
307 (purchases) from suppliers to arrive at time  $t$  and the expected level of biomass inventory,  
308  $I^{(t)}$  (i.e. for any given level of biomass energy generation, the more the purchase the  
309 higher the inventory). In addition, replacing  $I^{(t)}$  with its equivalent from eq. 2 in the

310 right side of eq. 3 (i.e.  $I^{(t)} \leq \bar{I}$ ), for any given level of biomass energy generation,  $x^{(t)}$ , a  
311 higher level of expected in-hand biomass inventory,  $I^{(t-1)}$ , reduces the need to biomass  
312 ordering from suppliers for arrival at time  $t$ .

313 As per Figure 2, these asset management and supply chain balancing loops, constrains  
314 the continuity of biomass boilers' operation, resulting in higher cost and lower  
315 operational performance for such boilers. This phenomenon necessitates the existence of  
316 the renewable heat incentive as a driving force to compensate on the price of biomass,  
317 which incentivizes the purchase of biomass, resulting in higher biomass inventories, and  
318 thus an increased level of biomass energy production. It should be mentioned that each  
319 arrow in Figure 2 captures the relationship between its tail and head variables. A “+” sign  
320 indicates that an increase in the arrow tail variable could lead to an increase in the arrow  
321 head variable. A “-“ sign means that an increase in the arrow tail variable could lead to a  
322 decrease in the arrow head variable.

323 With respect to the above balancing loops, the proposed model (eqs 1-12) is  
324 implemented in a SD simulation-optimization platform using Vensim modeling  
325 (professional edition 5.9e) software [43]. This model, as presented in Figure 3, is  
326 comprised of stock (boxes) and flow (double line arrows) elements, representing state  
327 and rate variables of the system, respectively. Consequently, biomass fuel inventories, the  
328 boiler's total cost of ownership, and total carbon savings are presented as stock, with their  
329 inflows and outflows as flow variables. The model is optimized with respect to the total  
330 cost of ownership, which is the cumulative sum of asset management and supply chain  
331 costs. When implemented in Vensim, we calculate the net present value of this cost to  
332 incorporate the impact of interest rate. The aim is to identify the optimal (i.e. least cost)

333 levels of biomass purchase, utilization, and (biomass and backup) boilers' capacities (as  
334 presented in red color in Figure 3), with respect to scenario parameters as relate to source  
335 of biomass, pricing and type of biomass boiler (as presented in green color in Figure 3),  
336 in addition to other influencing parameters (a full description of the model's equations as  
337 implemented in Vensim platform is provided in the appendix). In the following section,  
338 we will simulate and optimize the model using Vensim's optimization toolbox [43] based  
339 on data from a case study. In doing so, we analyze the impact of a renewable heat  
340 incentive (for non-domestic renewable heat generation) on transition from a natural gas-  
341 only heating system to a biomass one (with a backup natural gas boiler) and the arising  
342 sensitivities subject to changes in source, types and pricing of biomass materials as well  
343 as the choice of technologies and their cost and operational performance.

344

## 345 **5. Case study**

346 Transition from a natural gas-only heating to a biomass one is sought for a local authority  
347 building in south London, UK. The aim is to benefit from the recently introduced  
348 Renewable Heat Incentive for non-domestic buildings while supporting local biomass  
349 suppliers as well as contributing to the local government's carbon mitigation agenda.

350 The building, comprised of a floor area of 20,000 m<sup>2</sup>, is currently served by a  
351 500KW natural gas boiler. Due to seasonal variations, the energy demand for heating in  
352 this building fluctuates from approximately 5MWh in July to just over 20MWh in  
353 January. The size of the floor area and the amount of heating energy demand makes this  
354 building a representative case study for RHI implementation, benefiting from the  
355 economy of scale when integrating renewable energy technologies such as biomass



356 boilers. The location of the building in London is also positioning it with easier access to  
357 local suppliers of biomass across the UK and in Europe.

358 It is envisioned that the current boiler is replaced with a biomass boiler in the capacity  
359 range of [300, 400] KW to be accompanied by a back-up (natural gas) boiler in range of  
360 [100, 200] KW. We did not consider any such boundaries on capacities in the proposed  
361 model. But in the case study, from a practical point of view, the client opted for these  
362 boundaries for several reasons. First, they wanted to make sure that the biomass boiler is  
363 the main boiler and the natural gas boiler will only be a backup one. Second, the  
364 company providing the biomass boiler is one of the very few that manufacture larger  
365 biomass boilers but is not manufacturing biomass boilers above 400KW due to lack of  
366 many customers for that range of capacity. Third, biomass boilers need more space  
367 compare to the natural gas one, for the boiler and biomass storage. Space limitation is a  
368 barrier for installation of larger biomass boilers in the case study building. The total  
369 available space for the boilers and storage would be 70m<sup>3</sup> (considering a plant room  
370 height of 3.5m). Based on a recent study in London, there are two types of biomass fuels,  
371 , wood chips and wood pellets, which are competitive in terms of availability, price,  
372 physical density and energy content as presented in Table 2 [15].

373 Minimizing the total cost of the proposed system, which includes asset management  
374 and supply chain costs, according to eq. 1 and subject to eqs. 2-12, will result in making  
375 decisions on boilers' capacities, their operational plans, and biomass ordering quantities  
376 and timing. Figures 4-6 show the outcomes of the optimization process using a Vensim  
377 optimization platform [43] which utilizes a Powell hill climbing algorithm [44] to search  
378 for the optimal plan over a targeted service life of 25 years.

379 As energy demand in the building is varying on a monthly basis, for the sake of the  
380 clarity and simplicity of presentations, the results for the first 48 months are shown in  
381 Figures 4-6. Switching to a medium size biomass boiler in the capacity range of [300,  
382 400] KW, according to Table 1, could yield an incentive of 0.05 GBP/KWh, if operated  
383 less than 1,314 annually, otherwise it is associated with an incentive of 0.021 GBP/KWh.  
384 Optimizing the model. On that basis, the installation of a 400KW biomass boiler,  
385 accompanied by a 100KW backup one, is recommended.

386 In this sense, we have the following outcomes as the long-run service life operational  
387 plans of the boilers: The cumulative annual utilization of biomass boiler is identified as  
388 reaching 306 hours annually (Figure 4a), which is associated with the higher bound of the  
389 incentive. Keeping the operational hours to such a level is made possible as a result of the  
390 use of an 8 m<sup>3</sup> buffer (hot water) tank (included in the biomass boiler's cost and space  
391 estimations). The backup boiler's operation, as shown by Figure 4a, is mainly happening  
392 during the peak demand period in winter. Once the system establishes a reliable level of  
393 biomass storage, the share of backup boiler further shrinks and we reach approximately a  
394 3 to 1 ratio for (biomass and backup) boilers' utilization. The monthly utilization  
395 numbers ranges seasonally from 3,888 to 15,261 KWh for biomass boiler and from 912  
396 to 4,464 KWh for the natural gas boiler. As depicted by Figure 5, until the system reaches  
397 a reliable system of inventory, there would be two peak orderings for biomass in each of  
398 the first two years, which will reduces to one occasion thereafter. In the long run, the  
399 orders will establish a seasonal range from 1.20 to 6.30 tons of biomass. The system will  
400 also maintain a safety inventory of 4.50 tons of biomass materials throughout its service  
401 life.

402 According to Figure 6, the renewable heat incentive will cover approximately a  
403 quarter of the costs associated with biomass boiler's utilization, enough to establish it as  
404 the main heat producing boiler in our least total cost solution. In the light of the above  
405 results, we now develop a sensitivity analysis to investigate the impact of source, types  
406 and pricing of biomass materials as well as the choice of technologies (efficiency versus  
407 cost) on the outcomes of the optimization, and in particular, the optimal production plan  
408 and total cost.

409

## 410 **6. Results Analysis**

411 When it comes to biomass boiler's technologies, their difference is in the types of  
412 biomass materials they can handle with respect to the moisture content and particle size.  
413 The potential for such variations was captured in the proposed model by introducing a  
414 "Boiler's Efficiency Coefficient", ranging from 0 to 1, where a higher value represent a  
415 more tolerant boiler. It is also the case that the boilers with higher tolerance would have a  
416 higher price tag. Figure 7 presents the range of values which correspond with various  
417 boilers' technologies and that match the required capacity [15], with differences that  
418 originate from their feeding mechanism, grating system, and combustion technology. On  
419 the other hand, the choice of biomass materials could also vary greatly. Again, Table 2  
420 captures the range of values associated with such a choice. The pricey wood pellets have  
421 higher energy content and physical density, which means a better combustion and storage  
422 efficiency, compared to the cheaper woodchips. Figure 8 presents these variations based  
423 on the values shown in Table 2.

424 This study presents a sensitivity analysis using Vensim sensitivity analysis platform  
425 [43] to investigate the impact of variations in (1) the efficiency and price of biomass  
426 boiler's technology (Figure 7) and (2) the choice of biomass materials (Figure 8), on the  
427 main service life characteristics of the system, namely the extent of energy generation  
428 from biomass and the associated total cost. This analysis is subject to the key assumption  
429 that all other parameters of the model are fixed while varying the two indicated  
430 parameters.

431 Assuming that the above choices for technologies and materials are available for our  
432 case study, we consider that the variations follow a uniform distribution, giving each  
433 value the same likelihood. Figure 7 shows that when installing a more expensive biomass  
434 boiler (with a higher reliability and a better rate of biomass-to-heat conversion), the  
435 potential to use biomass in heat supply could be negatively impacted. This is due to the  
436 fact that the increase in capital costs (associated with the more efficient boiler  
437 technologies) will not fully be offset with the operational gains and support from  
438 Renewable Heat Incentive. Thus, for building managers, it will be more financially  
439 logical to favour higher dependence on the cheaper natural gas (back-up) boiler. On the  
440 contrary, switching to a more efficient fuel option (with a higher energy content and  
441 density) will not contribute to a considerable change in the share of biomass-based heat  
442 as the operational gains due to a better storage and conversion performance are offset by  
443 the higher biomass prices that contribute to an increase in the overall cost of the system.  
444 Thus while this option is somewhat more financially viable than the former option, it is  
445 not without its drawbacks.

446        These are important findings that show that even with the availability of support from  
447 a renewable heat incentive (RHI) scheme, there would be no motivation to go for a better  
448 performing biomass boiler technology or a more efficient biomass fuel option. This is  
449 mainly due to the fact the RHI scheme does not provide a prioritization based on the type  
450 of technologies or fuel options, it is only concerned about the size and extent of the  
451 utilization of the technology. The findings reconfirm the lack of encouragement for  
452 efficiency as a major issue when it comes to supporting mechanisms for renewable  
453 energy generation. This has major implications for the government’s RHI scheme as it  
454 suggests that the scheme itself may not be surgical enough as it does not take into  
455 account, the specific impacts of technology type or biomass fuel characteristics.

456

## 457 **7. Conclusion and Policy Implications**

458 This study proposed a simulation-optimization model to capture the whole life asset and  
459 supply chain management elements of building-integrated biomass boilers. It paid  
460 particular attention to incorporate the recently proposed UK government’s renewable heat  
461 incentive scheme for non-domestic buildings. The study validated the model by applying  
462 it to a real-world case study and analyzed the results of its applicability.

463        By considering a whole life costing approach, we created a model that  
464 incorporated the costs associated with supply, storage, and use of biomass as well as the  
465 capital and operational costs of biomass and natural gas boilers throughout their service  
466 life. In this sense, we were able to investigate the impact of RHI on the asset management  
467 and supply chain characteristics of building-integrated biomass boilers. From an asset  
468 management perspective, it identified the optimal energy (heat) generation capacities and

469 schedules for biomass (and backup) boilers, linking them to supply chain-related  
470 decisions on levels of biomass source, ordering and storage. The sensitivity of those  
471 decisions, subject to variations in biomass boiler's technologies (considering their capital  
472 costs and operational performance) and biomass materials (considering source, types and  
473 pricing) were further analyzed.

474         The results indicated that, the availability of a Renewable Heat Incentive policy  
475 scheme was effective in incentivizing the switch to a biomass boiler but it did not  
476 encourage shifting to more efficient boiler technologies or biomass fuels. This is a  
477 common problem with the renewable energy support mechanisms that provide direct  
478 incentives (such as feed-in-tariff policy), as they encourage the uptake of more expensive  
479 renewable means of energy generation through a direct incentive without creating a  
480 motivation for more (cost and energy) efficient practices. In this sense, the adoption of  
481 (or mixing RHI with) a renewable portfolio standard (RPS) policy can be envisioned as a  
482 way to address the efficiency when encouraging building-integrated renewable heat  
483 technologies. An RPS sets targets for renewables but leaves the choice of technology and  
484 fuels to the developers, leading to adoption of more cost-efficient options in long term  
485 [1]. In contrary, RHI creates a quick surge towards the renewable technologies. The ideal  
486 picture would be a combination of such policies to create a compromise between  
487 effectiveness of RHI and efficiency of RPS policies.

488         This study could be extended in different ways. First, the model could be adopted  
489 for larger scale district heating systems with multiple users. It is possible that the  
490 economies of scale could result in different outcomes compared to the ones found in this  
491 study. In addition, future studies may consider a scenario where the value of the

492 renewable heat incentive is determined endogenously. Such a study could indicate if  
493 there is an optimal level of support for our specific case study and if it is beneficial to  
494 provide RHI support on the basis of the characteristics of individual projects.

495

#### 496 **Acknowledgment**

497 The authors are very much thankful to the reviewers of this paper for their review, helpful  
498 comments and suggestions.

499

#### 500 **Nomenclature**

501  $\pi$  : Whole life (ownership) cost for the main and backup boilers (GBP)

502  $t$  : Time step (Month)

503  $T$  : Targeted service life (Month)

504  $n$  : Number of potential suppliers

505  $p_i^{(t)}$  : Supplier ‘ $i$ ’ price for biomass at period ‘ $t$ ’ (GBP/kg)

506  $s_i^{(t)}$  : Biomass supply from supplier ‘ $i$ ’ at period ‘ $t$ ’ (kg/Month) – Decision variable

507  $c_i$  : Cost of biomass supply (including ordering and transport) from supplier ‘ $i$ ’

508 (GBP/Month)

509  $h$  : Holding cost of biomass (GBP/kg)

510  $I^{(t)}$  : Biomass storage (buffer) at period ‘ $t$ ’ (kg)

511  $p_g^{(t)}$  : Natural gas price at period ‘ $t$ ’ (GBP/KWh)

512  $y^{(t)}$  : Heating energy (production) from natural gas (backup) boiler at period ‘ $t$ ’

513 (KWh/Month) – Decision variable

514  $\beta^{(t)}$ : Rate of renewable heat incentive (RHI) at period ‘ $t$ ’ (GBP/KWh)

515  $x^{(t)}$ : Heating energy (production) from biomass boiler at period ‘ $t$ ’ (KWh/Month) –

516 Decision variable

517  $c_b$ : Levelized (capital and operational) cost of biomass boiler (aggregated over its service

518 life) (GBP/KWh)

519  $\nu$ : Climate change levy (for energy from fossil fuels) (GBP/KWh)

520  $c_g$ : Levelized (capital and operational) cost of natural gas (backup) boiler (aggregated

521 over its service life) (GBP/KWh)

522  $\alpha$ : Biomass materials deterioration (spoilage) rate (1/Month)

523  $\varepsilon$ : Biomass boiler’s efficiency ratio (dimensionless)

524  $r_b$ : Biomass materials’ energy content rate (KWh/kg)

525  $t_i$ : Supplier ‘ $i$ ’ order (delivery) time (Month)

526  $\bar{I}$ : Available storage capacity (Cubic Meter)

527  $S_i$ : Supplier ‘ $i$ ’ order capacity (kg/Month)

528  $D^{(t)}$ : Building energy demand at period ‘ $t$ ’ (KWh/Month)

529  $P_i$ : Supplier ‘ $i$ ’ base price for biomass (GBP/kg)

530  $k_i$ : Supplier ‘ $i$ ’ discount ratio (dimensionless)

531  $H$ : RHI’s preferred target for biomass boilers’ cumulative hours of operation (on a

532 yearly basis) (Hour)

533  $\beta_1$ : Rate of renewable heat incentive (RHI) for boilers operating within the preferred

534 target (on a yearly basis) (GBP/KWh)



535  $\beta_2$  : Rate of renewable heat incentive (RHI) for boilers operating beyond the preferred  
536 target (on a yearly basis) (GBP/KWh)

537  $X$  : Biomass boiler's capacity (KW) – Decision variable

538  $Y$  : Backup boiler's capacity (KW) – Decision variable

539  $w_b^{(t)}$  : Availability of biomass boiler at period 't' (Hour)

540  $w_b^{(t)}$  : Availability of backup boiler at period 't' (Hour)

541  $l(X, Y)$  : Space requirement for biomass and backup boilers (including storage and buffer  
542 tank) (Square Meter)

543  $L$  : Available space for biomass and backup boilers (including storage and buffer tank)  
544 (Square Meter)

545  $m$  : Number of air pollution criteria

546  $e_j(x^{(t)}, y^{(t)})$  : Aggregated air pollutant 'j' emission from biomass and backup boilers at  
547 period 't' (kg/Month)  
548

549  $E_j$  : Allowance (standard) for air pollutant 'j' emission (kg)

550  $e(x^{(t)}, y^{(t)})$  : Carbon savings achieved at period 't' (kg/Month)

551  $E_0$  : Carbon saving target (kg)

552

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- 663

664 **Figures**

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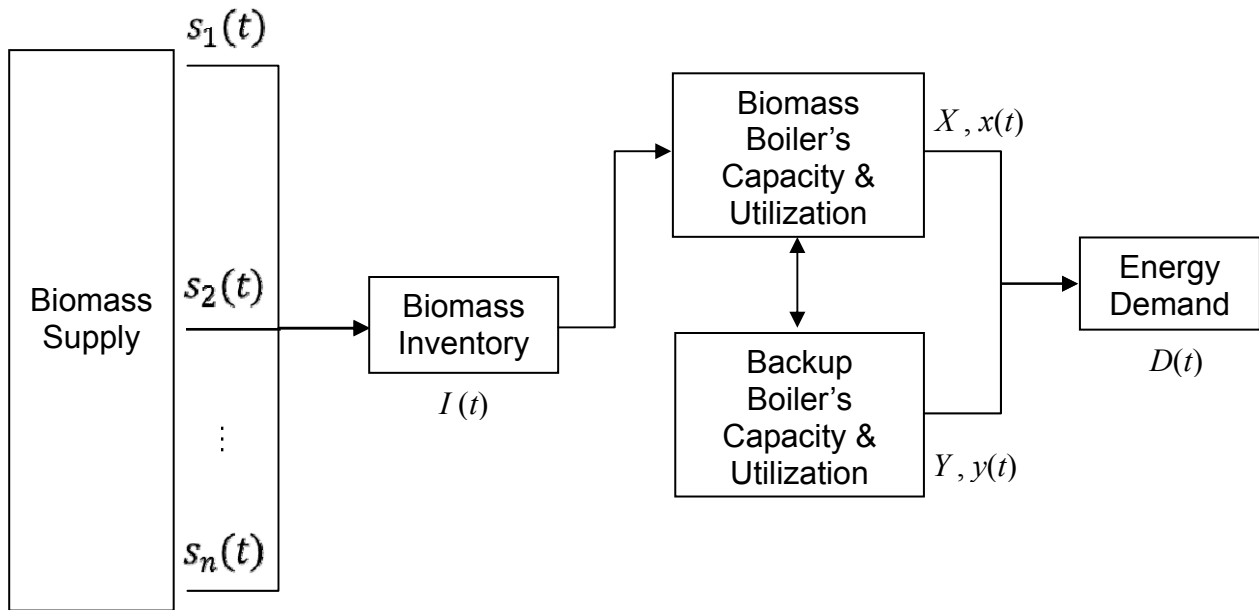
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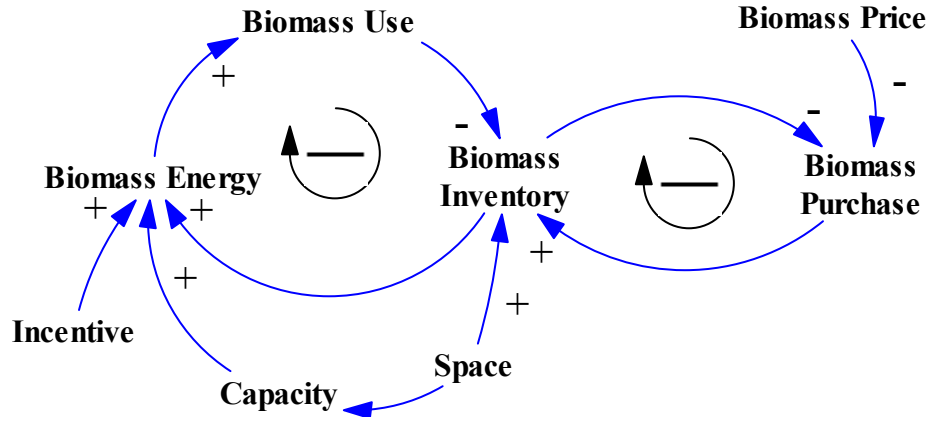
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**Figure 1** – A graphical representation of the proposed model with purchase, capacity, and utilization decision variables governed by biomass inventory and energy demand levels

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**Figure 2** – Asset management and supply chain causal loops governing a biomass boiler’s performance



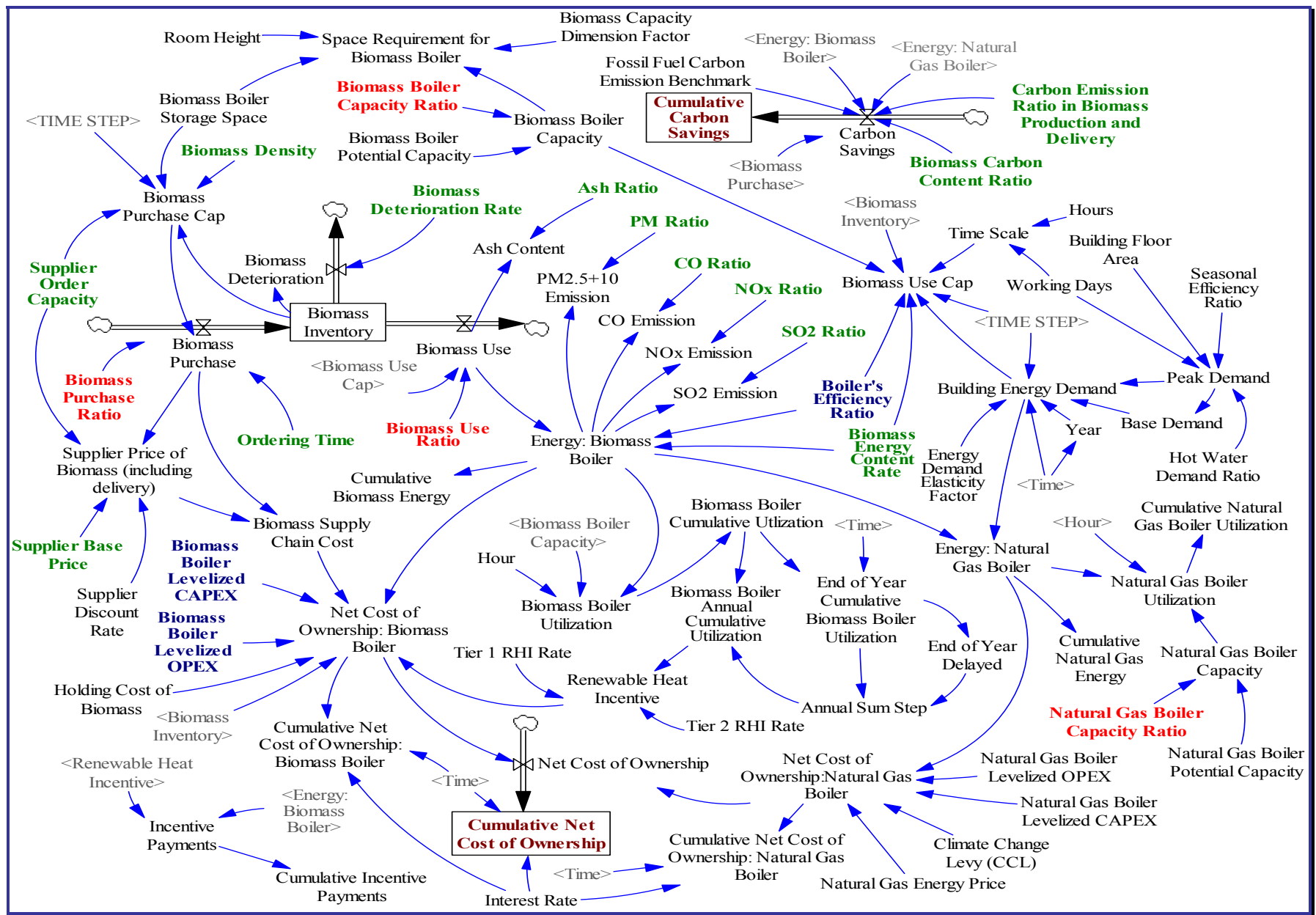
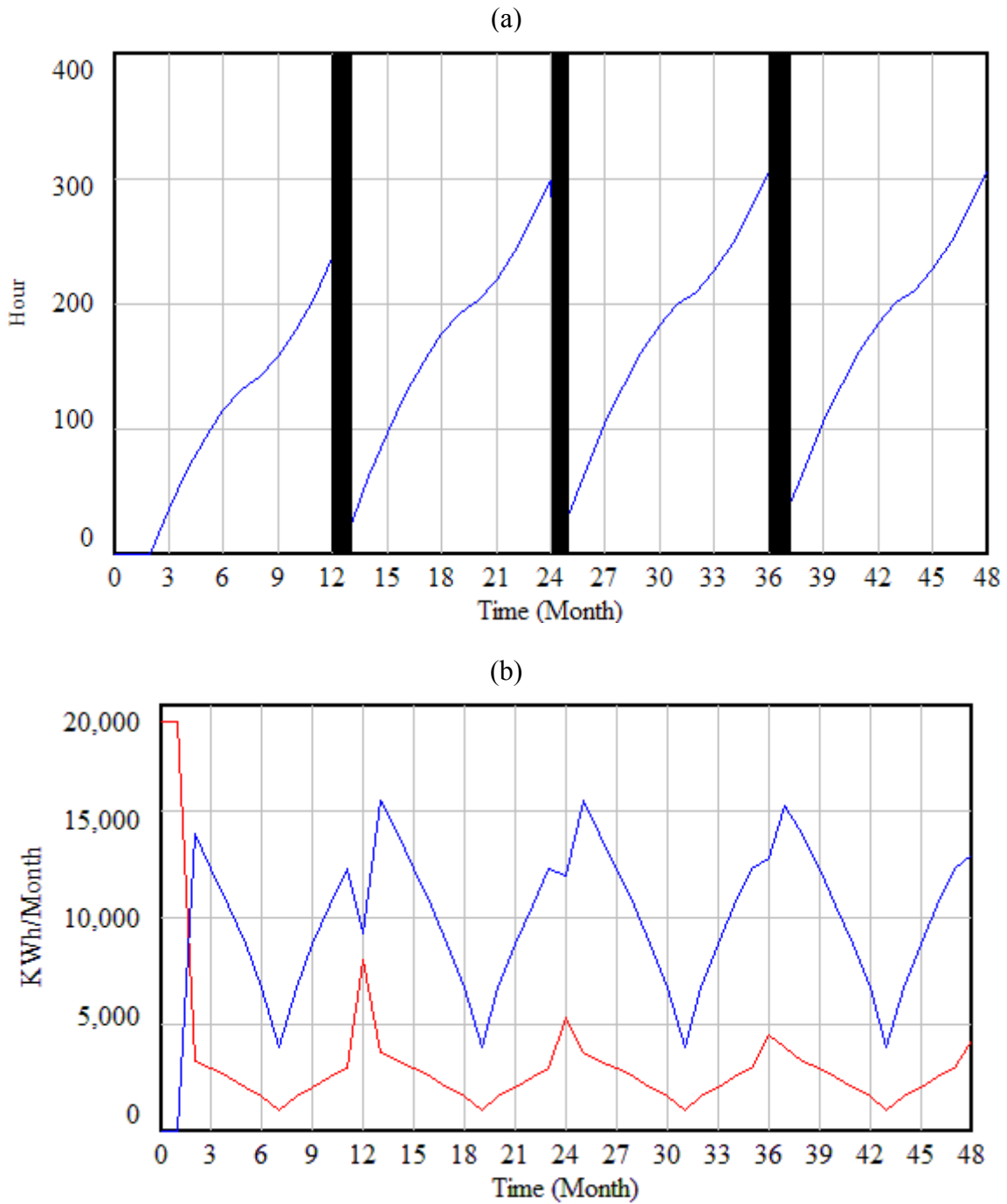
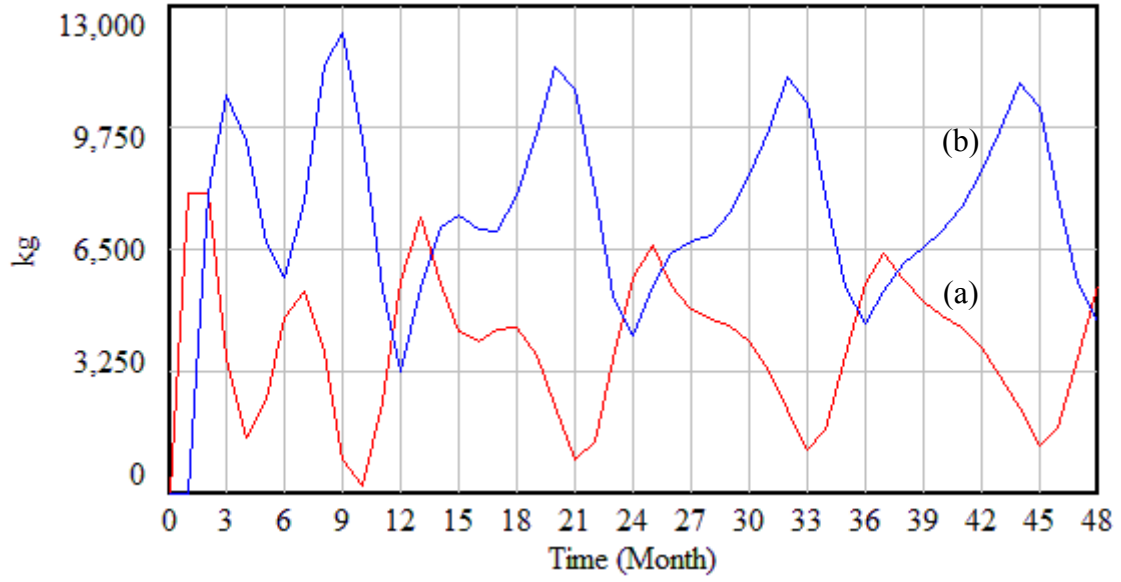


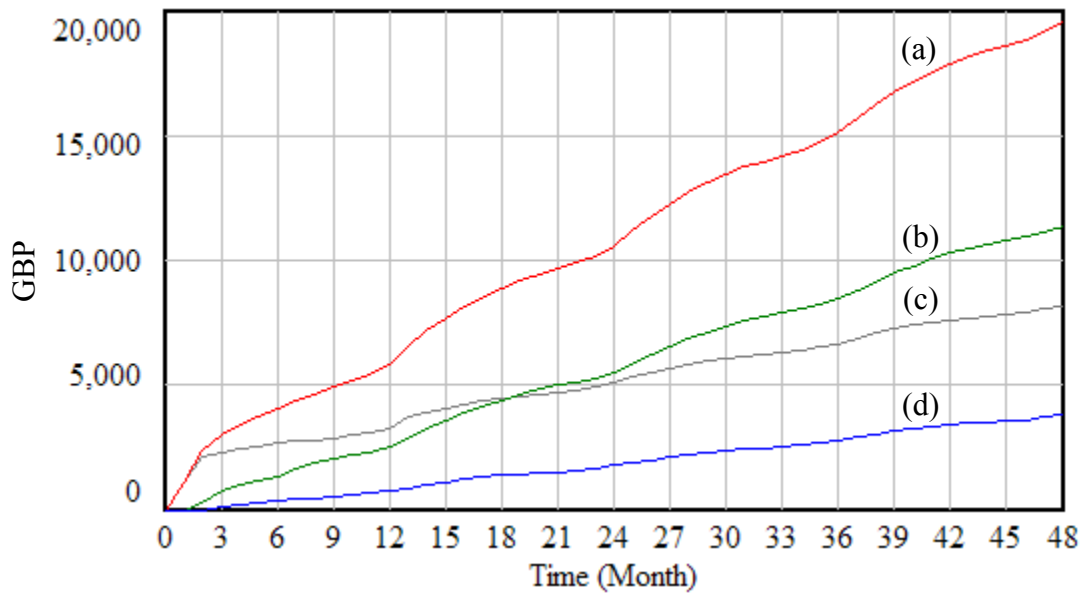
Figure 3 – A whole life supply chain-asset management model for non-domestic biomass boilers



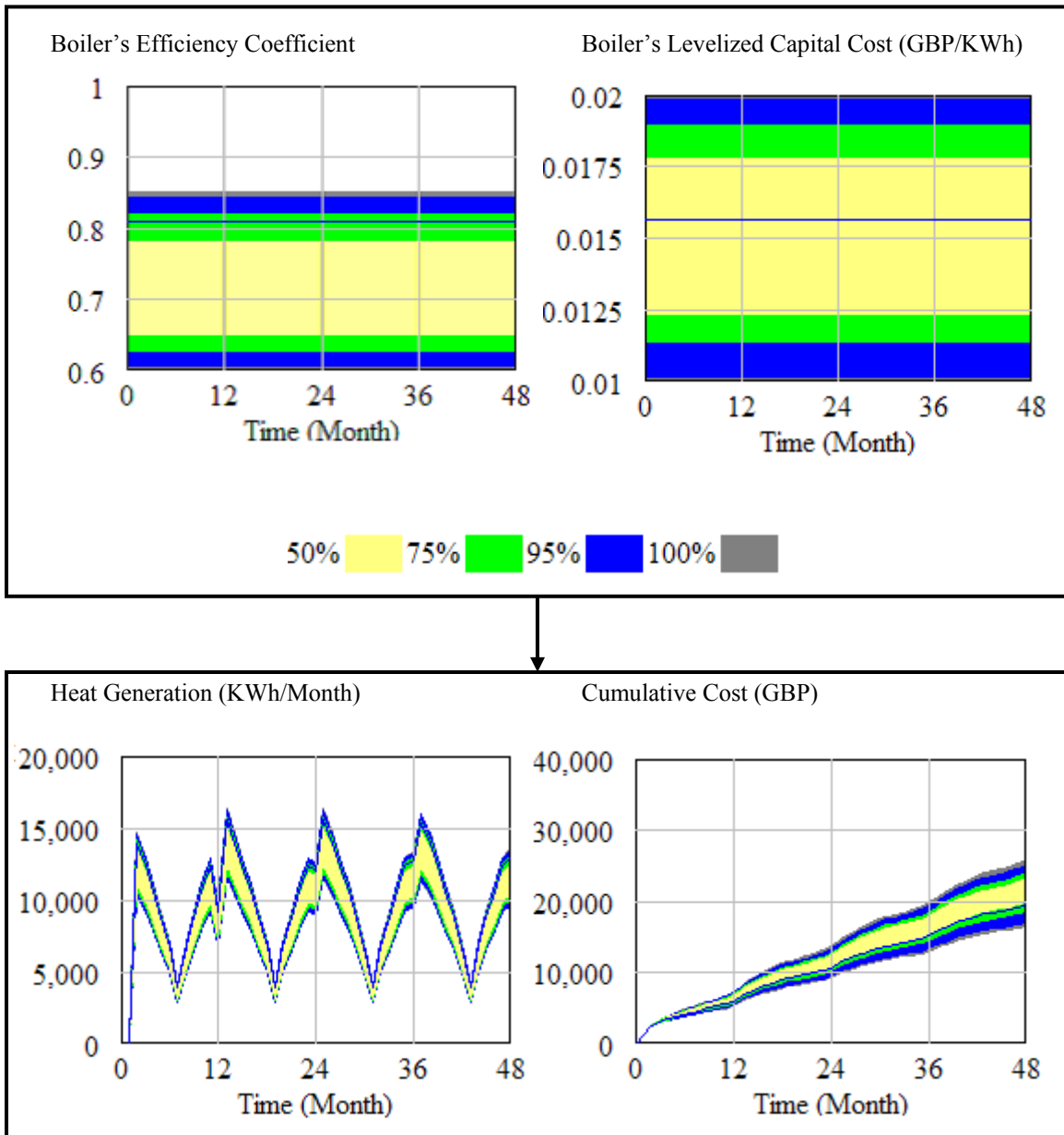
**Figure 4** – Optimal operational plan: (a) cumulative biomass boiler's utilization per year (hour) and (b) energy (heat) generation plan from biomass and back-up boilers (KWh/Month)



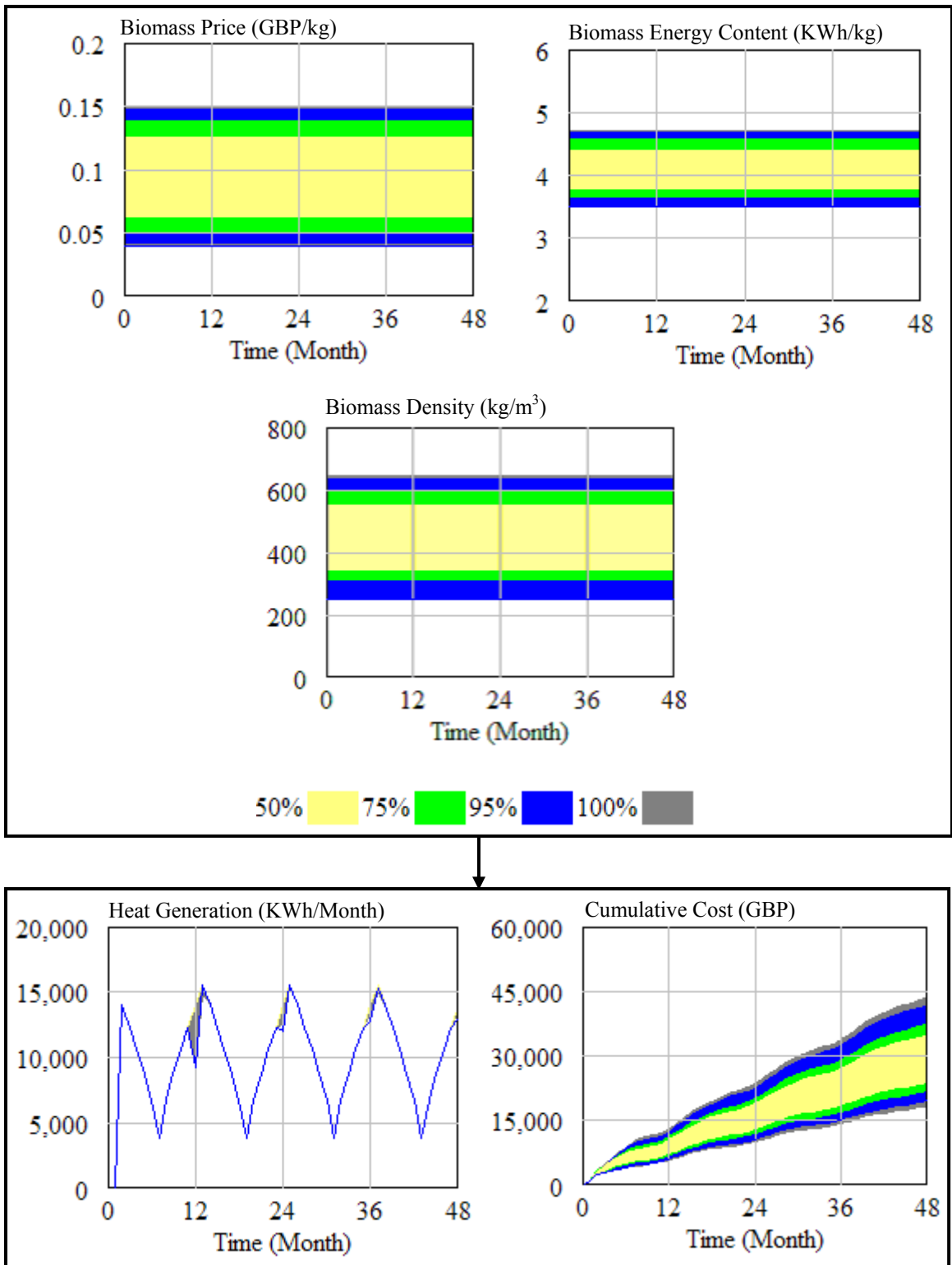
**Figure 5** – Optimal biomass (a) ordering and (b) inventory plans



**Figure 6** – Transition to biomass (a) cumulative net total cost, (b) cumulative net cost of biomass boiler, (c) cumulative net cost of back-up boiler, and (d) cumulative renewable heat incentive payment



**Figure 7** – Sensitivity of biomass energy (heat) generation and cumulative cost to choice of biomass boiler's technology with variations in efficiency and price (capital cost)



**Figure 8** - Sensitivity of biomass energy (heat) generation and cumulative cost to choice of biomass materials with variations in price, energy content and density

## Tables

**Table 1** – Renewable heat incentive structure for non-domestic applications

<b>Technology</b>	<b>Capacity (KW)</b>	<b>Use (Hours)</b>	<b>Incentive (GBP/KWh)</b>
Biomass Boilers	< 200	< 1,314	0.086
		> 1,314	0.022
	200<<1000	< 1,314	0.05
		> 1,314	0.021
	> 1000	-	0.01
Heat Pumps	< 100	-	0.048
	> 100	-	0.035
Solar	-	-	0.092
Biogas	-	-	0.073

**Table 2** – Biomass fuel's range of options

<b>Source</b>	<b>Price (£/kg)</b>	<b>Energy Content (KWh/kg)</b>	<b>Density kg/m<sup>3</sup></b>
Woodchip	0.04	3.5	250
Wood Pellet	0.15	4.7	650



## Appendix

A description of the equations, variables, and parameters as appeared in Vensim platform:

Annual Sum Step= INTEG (End of Year Cumulative Biomass Boiler Utilization-End of Year Delayed,0) Hour Units:

Ash Content= Biomass Use\*Ash Ratio/100 Units: kg/Month

Ash Ratio=4.5 Units: Dmnl

Base Demand=0.25\*Peak Demand Units: KWh/Month

Biomass Boiler Annual Cumulative Utilization=Biomass Boiler Cumulative Utilization-Annual Sum Step Hour Units:

Biomass Boiler Capacity=Biomass Boiler Capacity Ratio\*Biomass Boiler Potential Capacity KW Units:

Biomass Boiler Capacity Ratio=1 Units: Dmnl

Biomass Boiler Cumulative Utilization= INTEG (Biomass Boiler Utilization,0) Units: Hour

Biomass Boiler Levelized CAPEX=0.01562 Units: GBP/KWh

Biomass Boiler Levelized OPEX=0.00259 Units: GBP/KWh

Biomass Boiler Potential Capacity=400 Units: KW

Biomass Boiler Storage Space=50 Units: Cubic Meter

Biomass Boiler Utilization=Hour\*"Energy: Biomass Boiler"/Biomass Boiler Capacity Hour/Month Units:

Biomass Capacity Dimension Factor=1 Units: Square Meter/KW

Biomass Carbon Content Ratio=0.006 Units: kg/KWh

Biomass Density=250 Units: kg/Cubic Meter

Biomass Deterioration=Max(Biomass Deterioration Rate\*Biomass Inventory,0) Units: kg/Month

Biomass Deterioration Rate=0.05 Units: 1/Month

Biomass Energy Content Rate=3.5 Units: KWh/kg

Biomass Inventory= INTEG (Biomass Purchase-Biomass Use-Biomass Deterioration,0) Units: kg

Biomass Purchase= DELAY FIXED (Biomass Purchase Ratio\*Biomass Purchase Cap, Ordering Time , 0) Units: kg/Month

Biomass Purchase Cap=Max(MIN ((Biomass Boiler Storage Space\*Biomass Density-Biomass Inventory)/TIME STEP,Supplier Order Capacity),0) Units: kg/Month

Biomass Purchase Ratio=0.7981 Units: Dmnl

Biomass Supply Chain Cost="Supplier Price of Biomass (including delivery)"\*Biomass Purchase Units: GBP/Month

Biomass Use=Max(Biomass Use Ratio\*Biomass Use Cap,0) Units: kg/Month

Biomass Use Cap=Max(MIN (MIN(Time Scale\*Biomass Boiler Capacity\*Boiler's Efficiency Ratio, Building Energy Demand)/Biomass Energy Content Rate, Biomass Inventory/TIME STEP),0) Units: kg/Month

Biomass Use Ratio=1 Units: Dmnl

Boiler's Efficiency Ratio=0.81 Units: Dmnl

Building Energy Demand=IF THEN ELSE( Time > 0, Base Demand+(Peak Demand-Base Demand)\*ABS((Time-1)/TIME STEP/6-2\*Year+1)^Energy Demand Elasticity Factor, Peak Demand) Units: KWh/Month

Building Floor Area=12000 Units: Square Meter

Carbon Emission Ratio in Biomass Production and Delivery=0.02315 Units: kg/kg

Carbon Savings=(Fossil Fuel Carbon Emission Benchmark-Biomass Carbon Content Ratio)\*"Energy: Biomass Boiler"-Carbon Emission Ratio in Biomass Production and Delivery\*Biomass Purchase-Fossil Fuel Carbon Emission Benchmark\*"Energy: Natural Gas Boiler" Units: kg/Month

"Climate Change Levy (CCL)"=0.00182 Units: GBP/KWh

CO Emission= CO Ratio\*"Energy: Biomass Boiler" Units: kg/Month

CO Ratio=3000/(1000\*277.778) Units: kg/KWh

Cumulative Biomass Energy= INTEG ("Energy: Biomass Boiler",0) Units: KWh

Cumulative Carbon Savings= INTEG (Carbon Savings,0) Units: kg

Cumulative Incentive Payments= INTEG (Incentive Payments,0) Units: GBP  
 Cumulative Natural Gas Boiler Utilization= INTEG (Natural Gas Boiler Utilization,0) Units: Hour  
 Cumulative Natural Gas Energy= INTEG ("Energy: Natural Gas Boiler",0) Units: KWh  
 Cumulative Net Cost of Ownership= INTEG (Net Cost of Ownership/(1+Interest Rate/100)^Time,0)  
 Units: GBP  
 "Cumulative Net Cost of Ownership: Biomass Boiler"= INTEG ("Net Cost of Ownership: Biomass  
 Boiler"/(1+Interest Rate/100)^Time,0) Units: GBP  
 "Cumulative Net Cost of Ownership: Natural Gas Boiler"= INTEG ("Net Cost of Ownership:Natural Gas  
 Boiler"/(1+Interest Rate/100)^Time,0) Units: GBP  
 End of Year Cumulative Biomass Boiler Utilization=IF THEN ELSE(Time/12=INTEGER( Time/12), Biomass  
 Boiler Cumulative Utilization, 0) Units: Hour  
 End of Year Delayed= DELAY FIXED (End of Year Cumulative Biomass Boiler Utilization, 12 , 0)  
 Units: Hour  
 Energy Demand Elasticity Factor=0.8 Units: Dmnl  
 "Energy: Biomass Boiler"=Biomass Use\*Biomass Energy Content Rate\*Boiler's Efficiency Ratio  
 Units: KWh/Month  
 "Energy: Natural Gas Boiler"=Building Energy Demand-"Energy: Biomass Boiler" Units:  
 KWh/Month  
 Fossil Fuel Carbon Emission Benchmark=0.194 Units: kg/KWh  
 Holding Cost of Biomass=0.001 Units: GBP/kg  
 Hot Water Demand Ratio=0.002 Units: KWh/Square Meter  
 Hour=1 Units: Hour\*KW/KWh  
 Hours=24 Units: KWh/KW  
 Incentive Payments="Energy: Biomass Boiler"\*Renewable Heat Incentive Units: GBP/Month  
 Interest Rate=2.5/12 Units: Dmnl  
 Natural Gas Boiler Capacity=Natural Gas Boiler Capacity Ratio\*Natural Gas Boiler Potential Capacity  
 Units: KW  
 Natural Gas Boiler Capacity Ratio=0.934 Units: Dmnl  
 Natural Gas Boiler Levelized CAPEX=0.00607 Units: GBP/KWh  
 Natural Gas Boiler Levelized OPEX=0.00079 Units: GBP/KWh  
 Natural Gas Boiler Potential Capacity=100 Units: KW  
 Natural Gas Boiler Utilization=Hour\*"Energy: Natural Gas Boiler"/Natural Gas Boiler Capacity  
 Units: Hour  
 Natural Gas Energy Price=0.0458 Units: GBP/KWh  
 Net Cost of Ownership="Net Cost of Ownership: Biomass Boiler"+"Net Cost of Ownership:Natural Gas Boiler"  
 Units: GBP/Month  
 "Net Cost of Ownership: Biomass Boiler"=(Biomass Boiler Levelized CAPEX+Biomass Boiler Levelized OPEX-  
 Renewable Heat Incentive)\*"Energy: Biomass Boiler"+Biomass Supply Chain Cost+Holding Cost of  
 Biomass\*Biomass Inventory Units: GBP/Month  
 "Net Cost of Ownership:Natural Gas Boiler"="Energy: Natural Gas Boiler"\*(Natural Gas Boiler Levelized  
 OPEX+Natural Gas Boiler Levelized CAPEX+Natural Gas Energy Price+"Climate Change Levy (CCL)")  
 Units: GBP/Month  
 NOx Emission=NOx Ratio\*"Energy: Biomass Boiler" Units: kg/Month  
 NOx Ratio=150/(1000\*277.778) Units: kg/KWh  
 Ordering Time=1 Units: Month  
 Peak Demand=24\*Hot Water Demand Ratio\*Building Floor Area\*Working Days/Seasonal Efficiency Ratio  
 Units: KWh/Month  
 PM Ratio=76/(1000\*277.778) Units: kg/KWh  
 "PM2.5+10 Emission"=PM Ratio\*"Energy: Biomass Boiler" Units: kg/Month  
 Renewable Heat Incentive=IF THEN ELSE(Biomass Boiler Annual Cumulative Utilization <= 1314, Tier 1 RHI  
 Rate, Tier 2 RHI Rate) Units: GBP/KWh  
 Room Height= 3.9 Units: Meter  
 Seasonal Efficiency Ratio=0.75 Units: Dmnl  
 SO2 Emission=SO2 Ratio\*"Energy: Biomass Boiler" Units: kg/Month  
 SO2 Ratio=20/(1000\*277.778) Units: kg/KWh

Space Requirement for Biomass Boiler= $80.99+31.46*\text{LN}(\text{Biomass Capacity Dimension Factor}*\text{Biomass Boiler Capacity}/1000)+\text{Biomass Boiler Storage Space}/\text{Room Height}$       Units: Square Meter  
 Supplier Base Price=0.04      Units: GBP/kg  
 Supplier Discount Rate=0.1      Units: Dmnl  
 Supplier Order Capacity=10000      Units: kg/Month  
 "Supplier Price of Biomass (including delivery)"= $\text{Supplier Base Price}*(1-\text{Supplier Discount Rate}*(\text{Biomass Purchase}/\text{Supplier Order Capacity}))$       Units: GBP/kg  
 Tier 1 RHI Rate=0.05      Units: GBP/KWh  
 Tier 2 RHI Rate=0.021      Units: GBP/KWh  
 Time Scale= $\text{Working Days}*\text{Hours}$       Units: KWh/(KW\*Month)  
 TIME STEP = 1      Units: Month  
 Working Days=25      Units: 1/Month  
 Year=IF THEN ELSE( Time/12 = INTEGER(Time/12) :AND: Time>0, INTEGER(Time/12),  
 INTEGER(Time/12)+1)      Units: Dmnl